

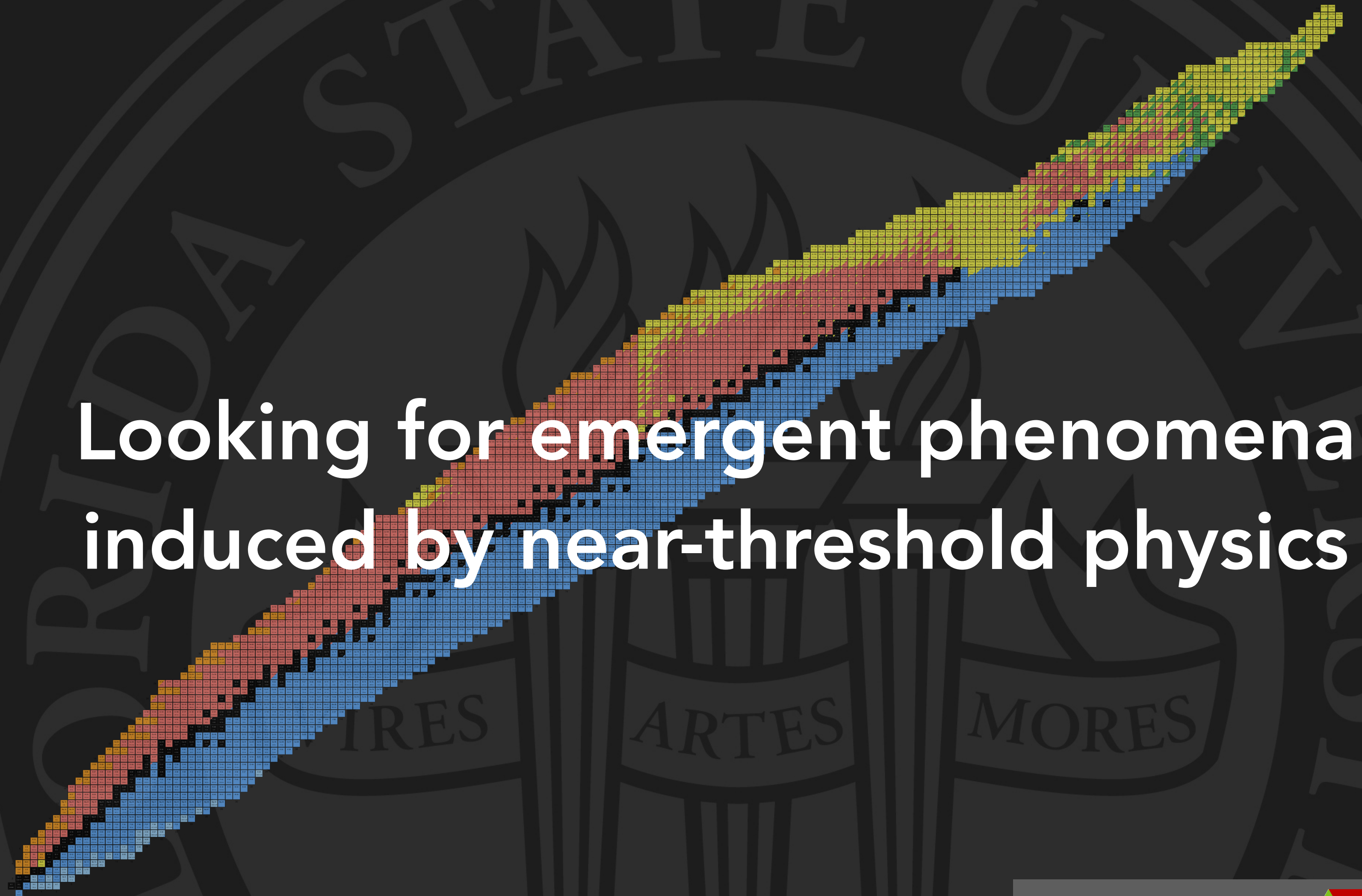


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May 17, 2023

# Looking for emergent phenomena induced by near-threshold physics



U.S. DEPARTMENT OF ENERGY  
**ENERGY**

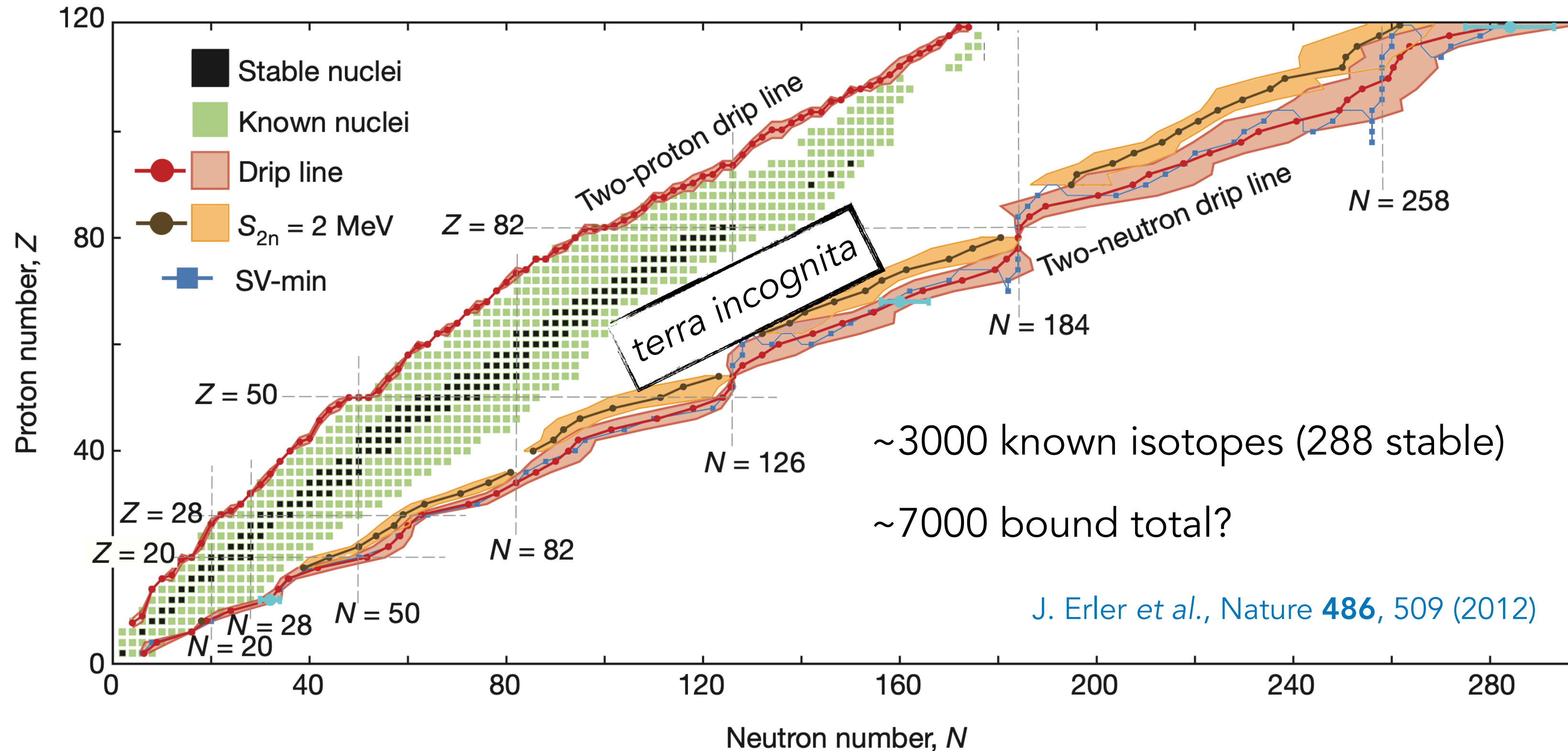
Office of Science



DOE: DE-SC0013617 (Office of Nuclear Physics, FRIB Theory Alliance)

# The exploration of the drip lines

Established at  $N = 9$  and  $Z = 13$ . Many new isotopes to discover on the neutron-rich side.

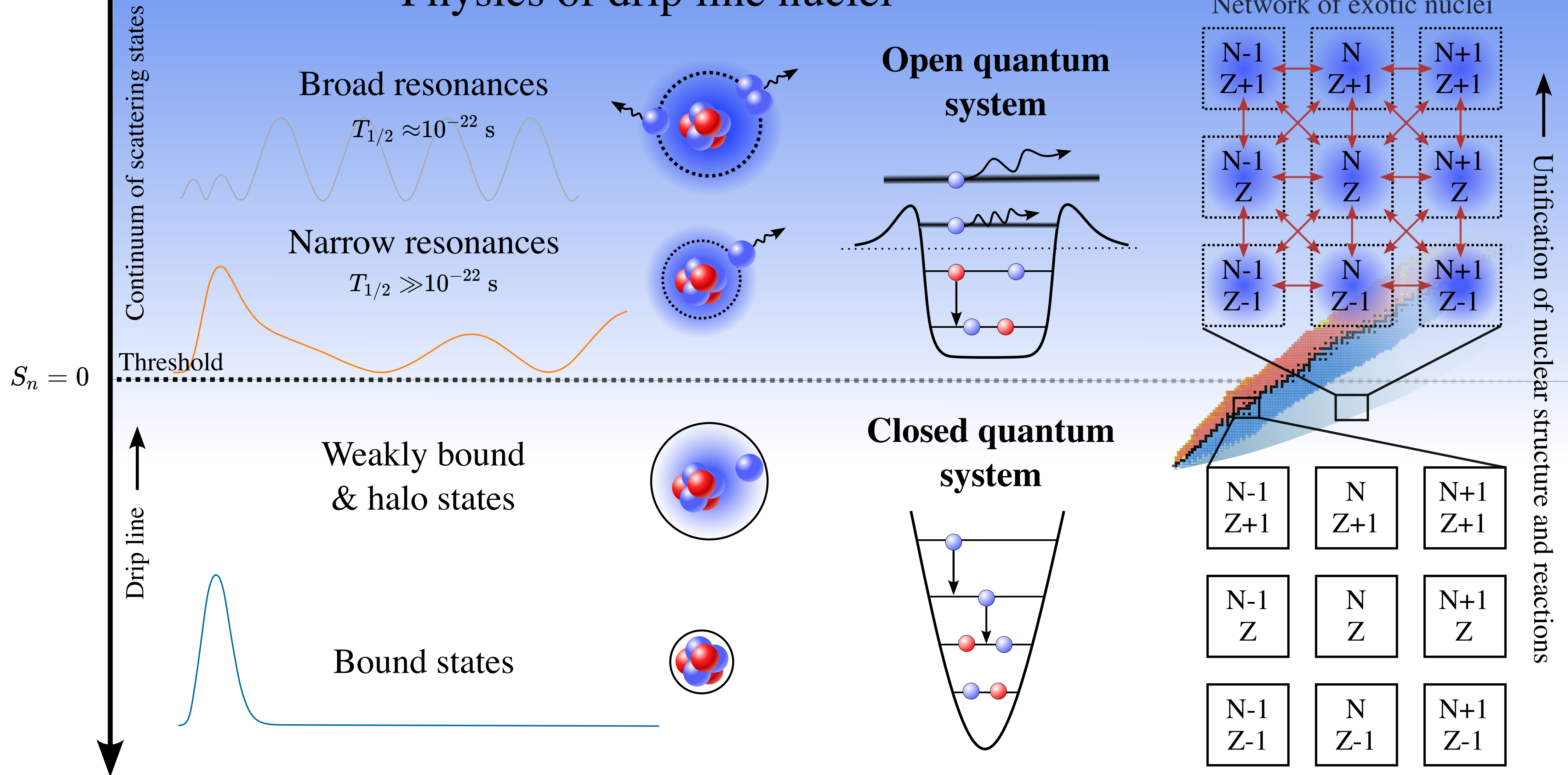


## Some opportunities:

- Test of nuclear forces in extreme  $N/Z$  conditions.
- Strong constraints: an isotope exists or it does not.
- Finding new phenomena induced by near-threshold effects.

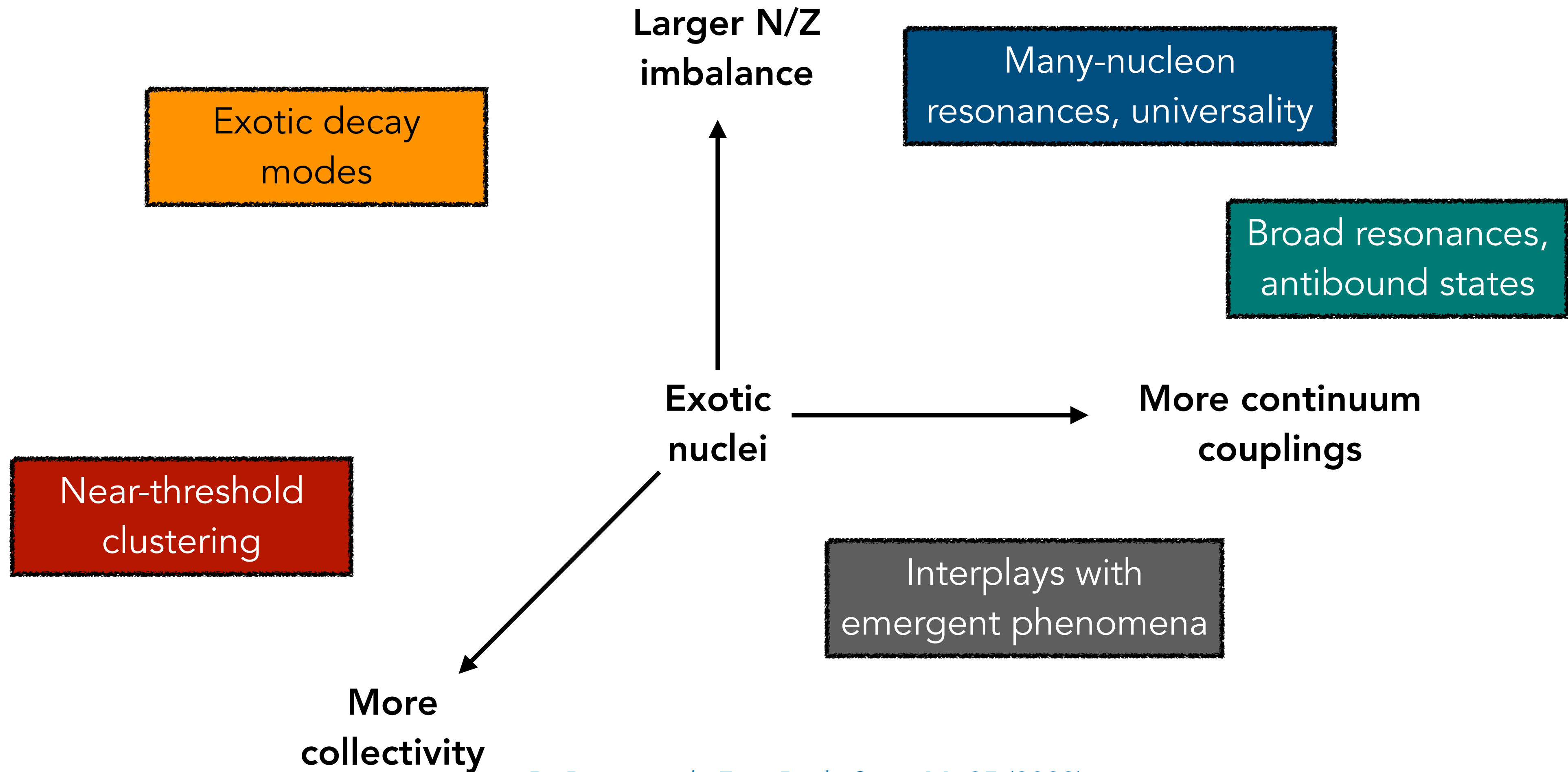
Where should we look first and why?

# Physics of drip line nuclei



# Theoretical challenges in near-threshold physics

Drip lines, higher excitation energies.



D. Bazin *et al.*, *Few-Body Syst.* **64**, 25 (2023)

# Theoretical approaches for near-threshold physics

Many methods developed over time, but in practice, only **a few methods** can go beyond 2 nucleons in the continuum.

## Feshback projection formalism:

CSM, SMEC

## Complex-scaling techniques:

Faddeev-Yakubowsky, lattice



Limited to 5 particles (need further development to go beyond)

## Berggren basis:

GSM, NCGSM, G-DMRG, CCT, IM-SRG, GCC, PRM

## Resonating group method (reactions with structure):

NCSM+RGM, NCSMC, (NC)GSM-CC, Symplectic-NCSM

**And more...**

In theory, the GSM can have all nucleons in the continuum, but in practice it needs truncations beyond ~4-5 nucleons.

The (current) G-DMRG code can handle Hamiltonians of theoretical dimension up to  $\dim = 10^{11}$ .

So far up to 9 particles in the continuum.

# Gamow density matrix renormalization group

Configuration interaction + renormalization group.

S. R. White, *Phys. Rev. Lett.* **69**, 2863 (1992)

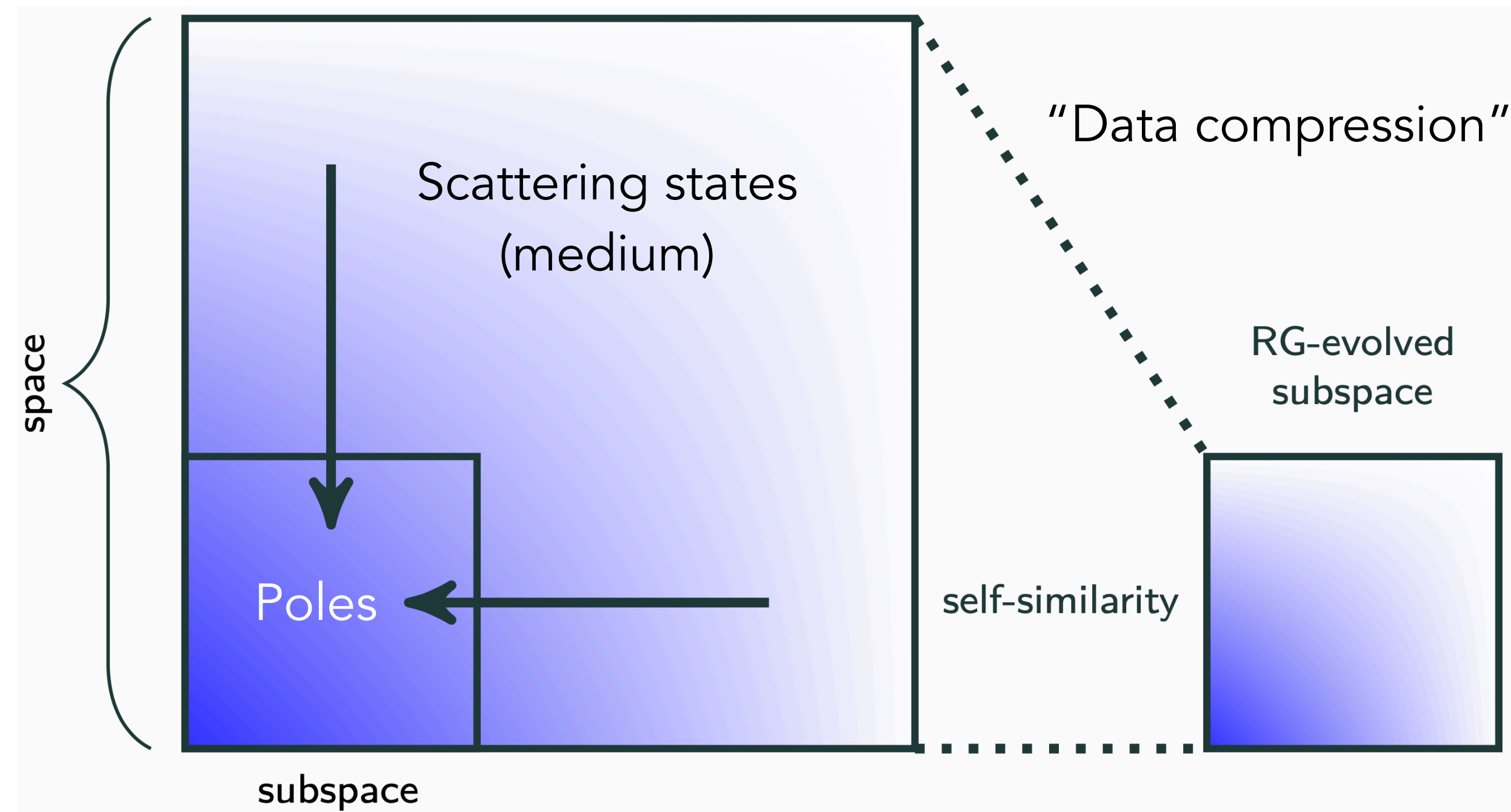
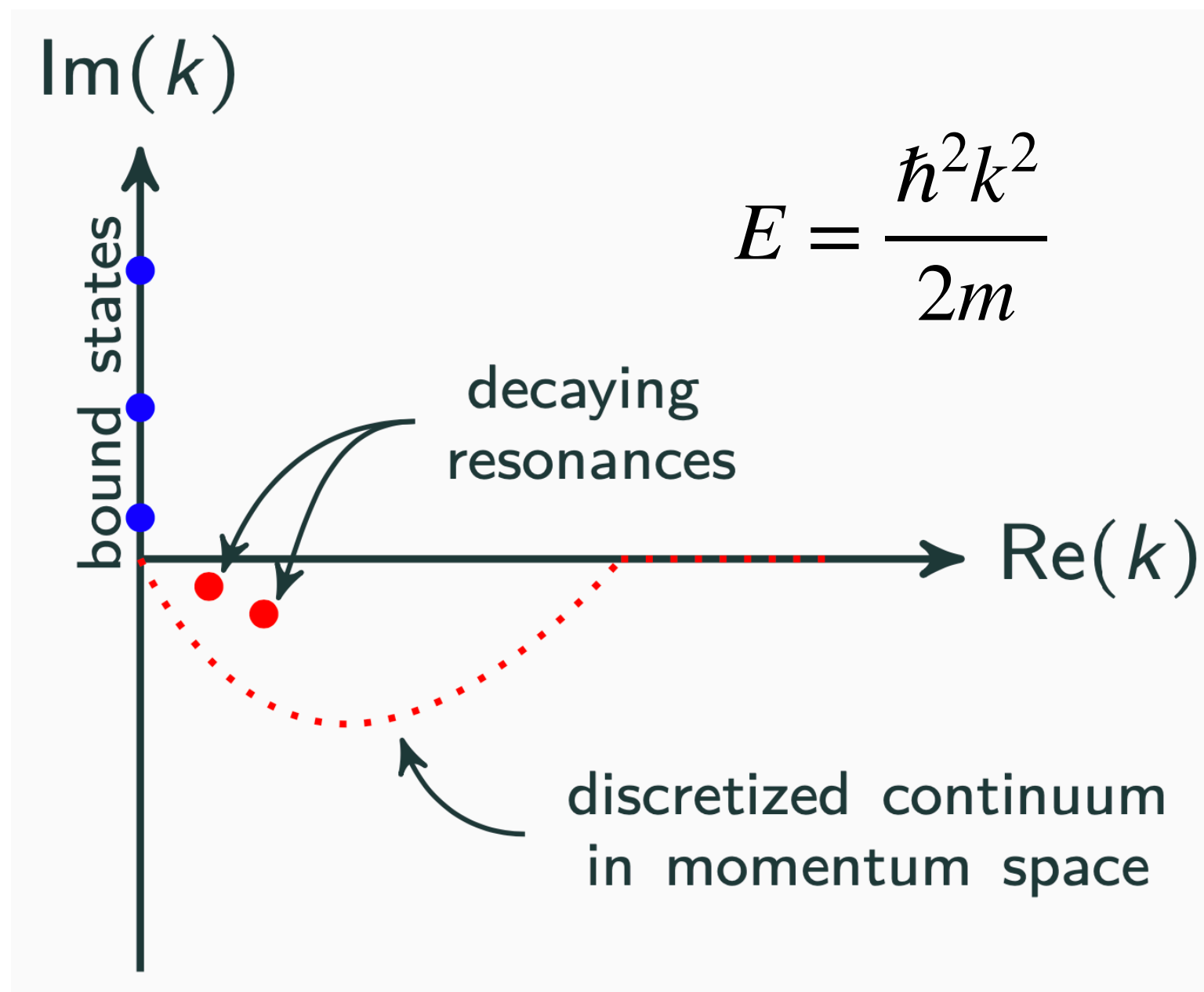
$$\sum_{i=(b,r)} |k_i\rangle\langle\tilde{k}_i| + \int_{L^+} dk |k\rangle\langle\tilde{k}| = \hat{1}$$

T. Berggren, *Nucl. Phys. A* **109** 265 (1968)

$$|\Psi^{A,J^\pi}\rangle_1 = \sum_{a,b} C_{b,i=1}^a \{ |SD_a^{f_{\mathcal{A}}}\rangle_0^{\mathcal{A}} \otimes |SD_b^{f_{\mathcal{B}}}\rangle_1^{\mathcal{B}} \}^{A,J^\pi}$$

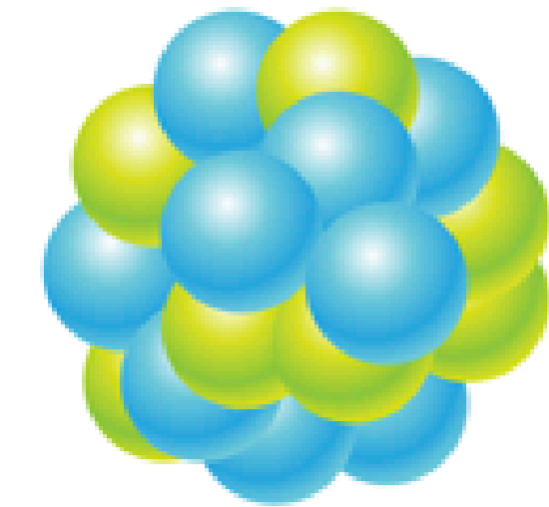
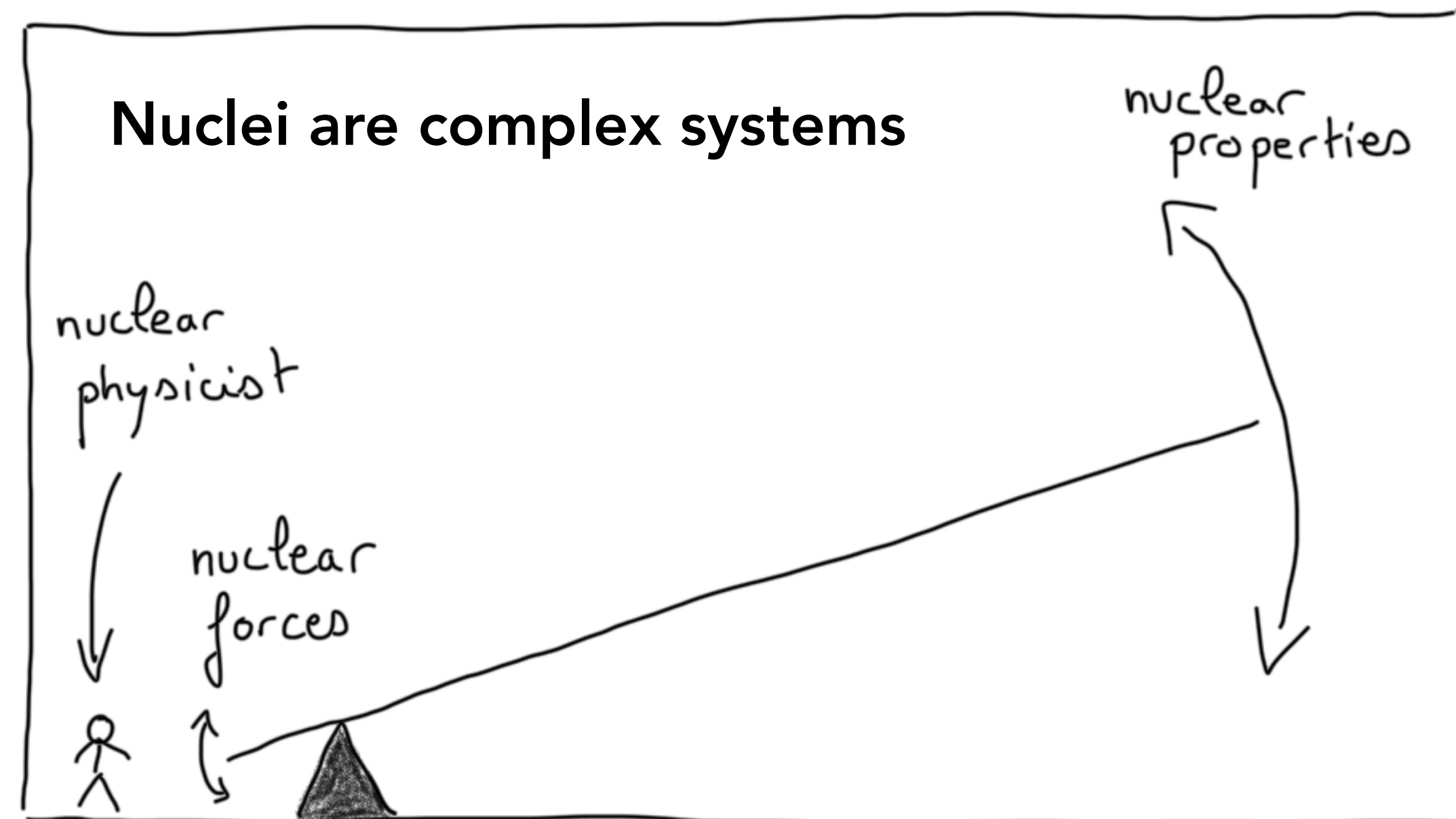
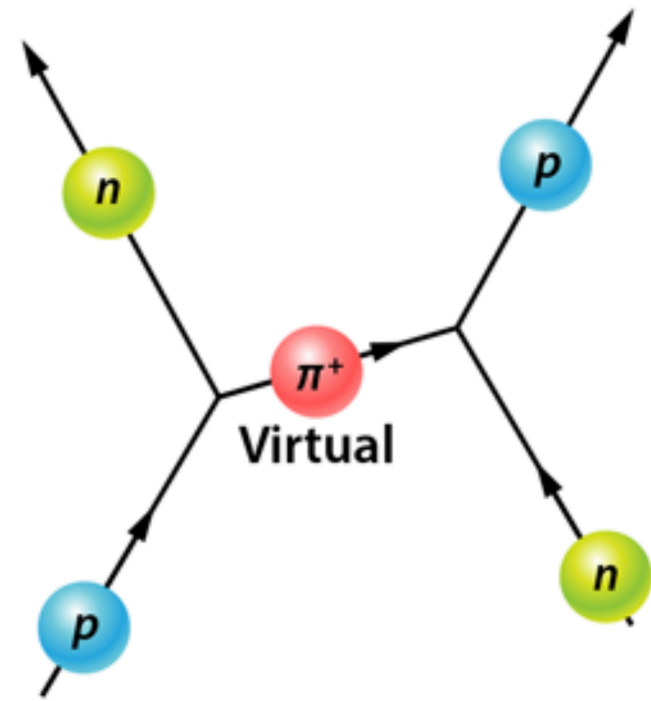
Reference space
Medium

J. Rotureau et al., *Phys. Rev. Lett.* **97**, 110603 (2006)



# Studying drip line nuclei in practice

We want to have **predictive power** and to make **usable predictions (= precise enough)**.



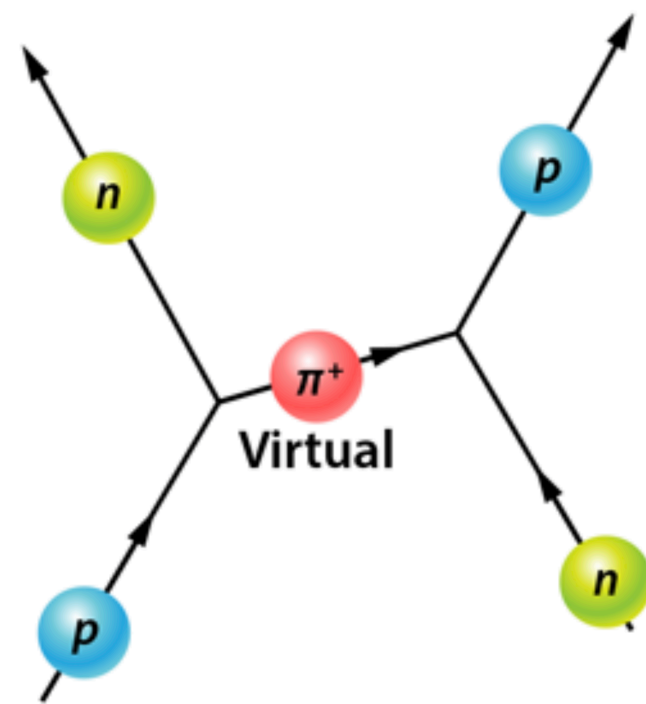
Small change in the input  
↓  
Large change in the output

Even if we had exact *ab initio* solutions including 1-, 2-, ...,  $A$ -body continua, our representation of nuclear forces will always have some error that will be magnified in the many-body problem → **Emergent phenomena**.

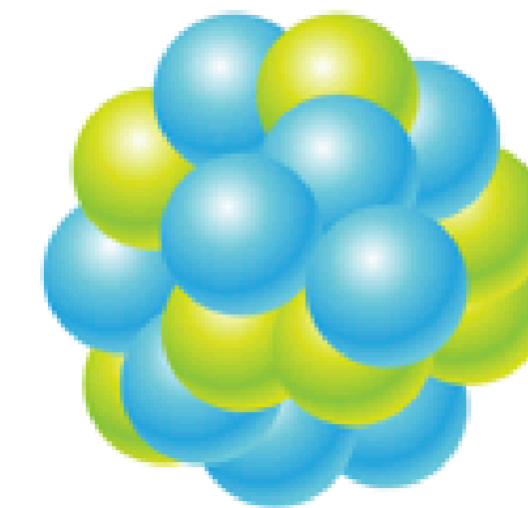
Current *ab initio* methods precise within  $\sim 1.0$  MeV at best on binding energies → **We need EFTs**.

# Nuclei are complex systems

Small change in the input  $\rightarrow$  large change in the output.

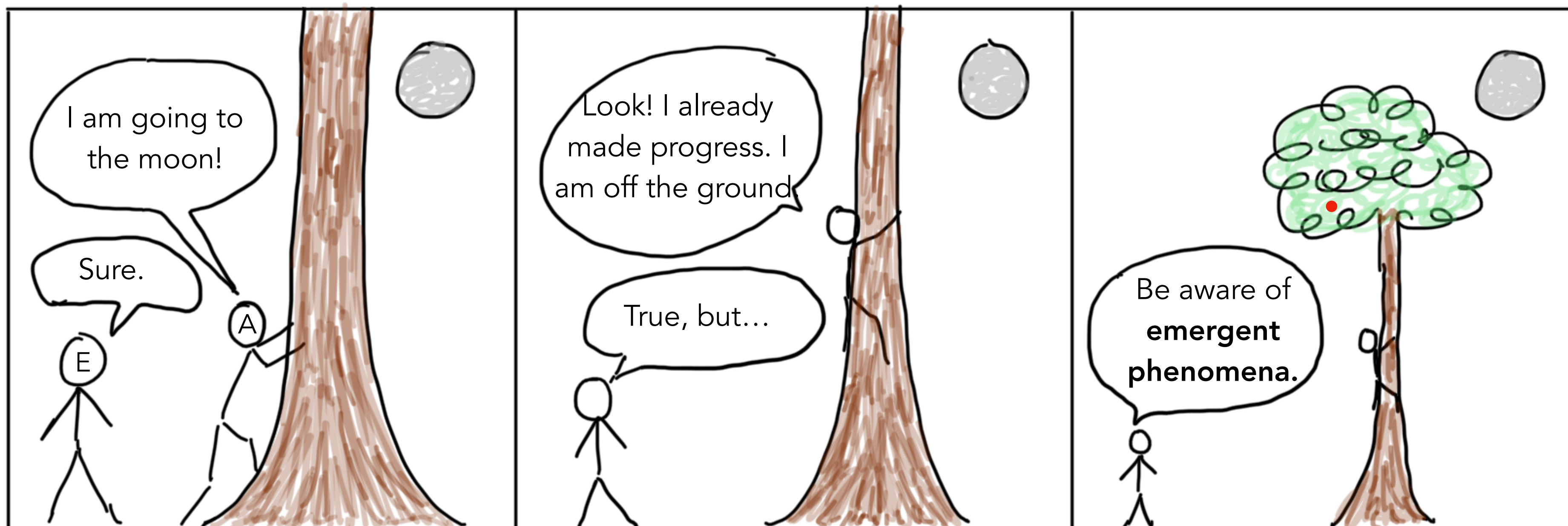


How do we go from nuclear forces to exotic nuclei?



The "moon"

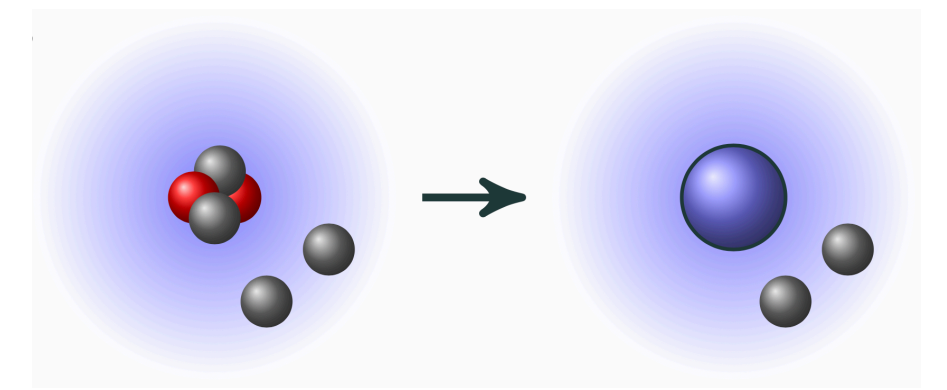
Ms. EFT and Mr. Ab initio



We need EFTs for precision!



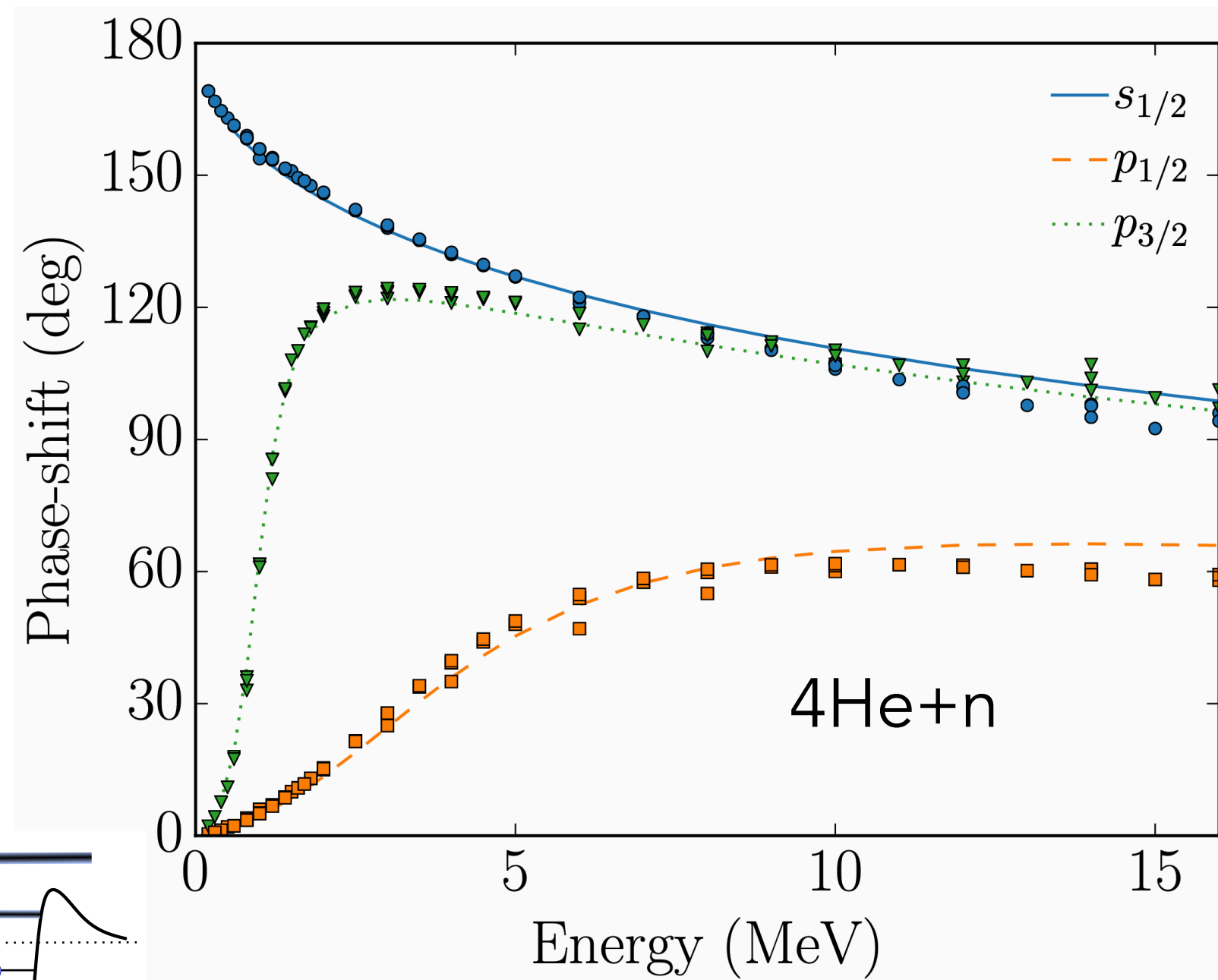
# Studying drip line nuclei in practice



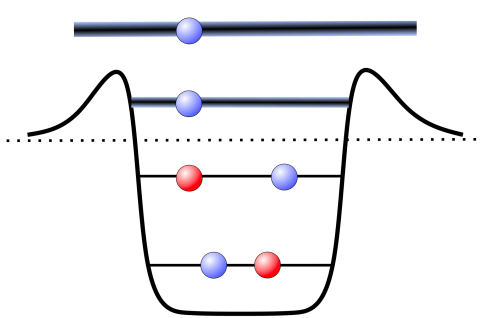
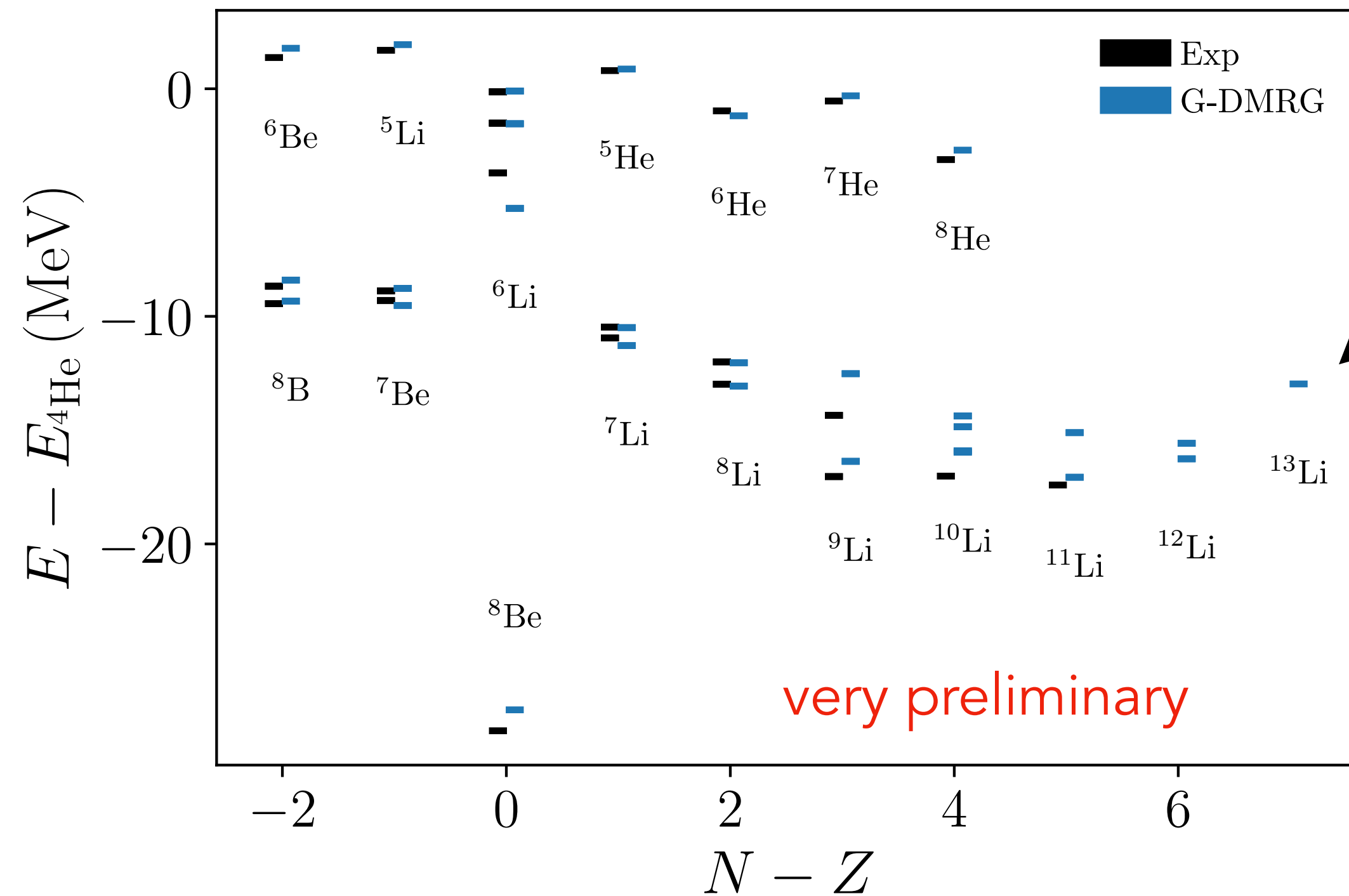
Building an EFT for the shell model appears to be the best compromise to deal with drip line nuclei.

Still working on the details, but adjusting a phenomenological contact interaction in the EFT spirit promising.

Core-nucleon interaction must reproduce core-nucleon phase shifts.

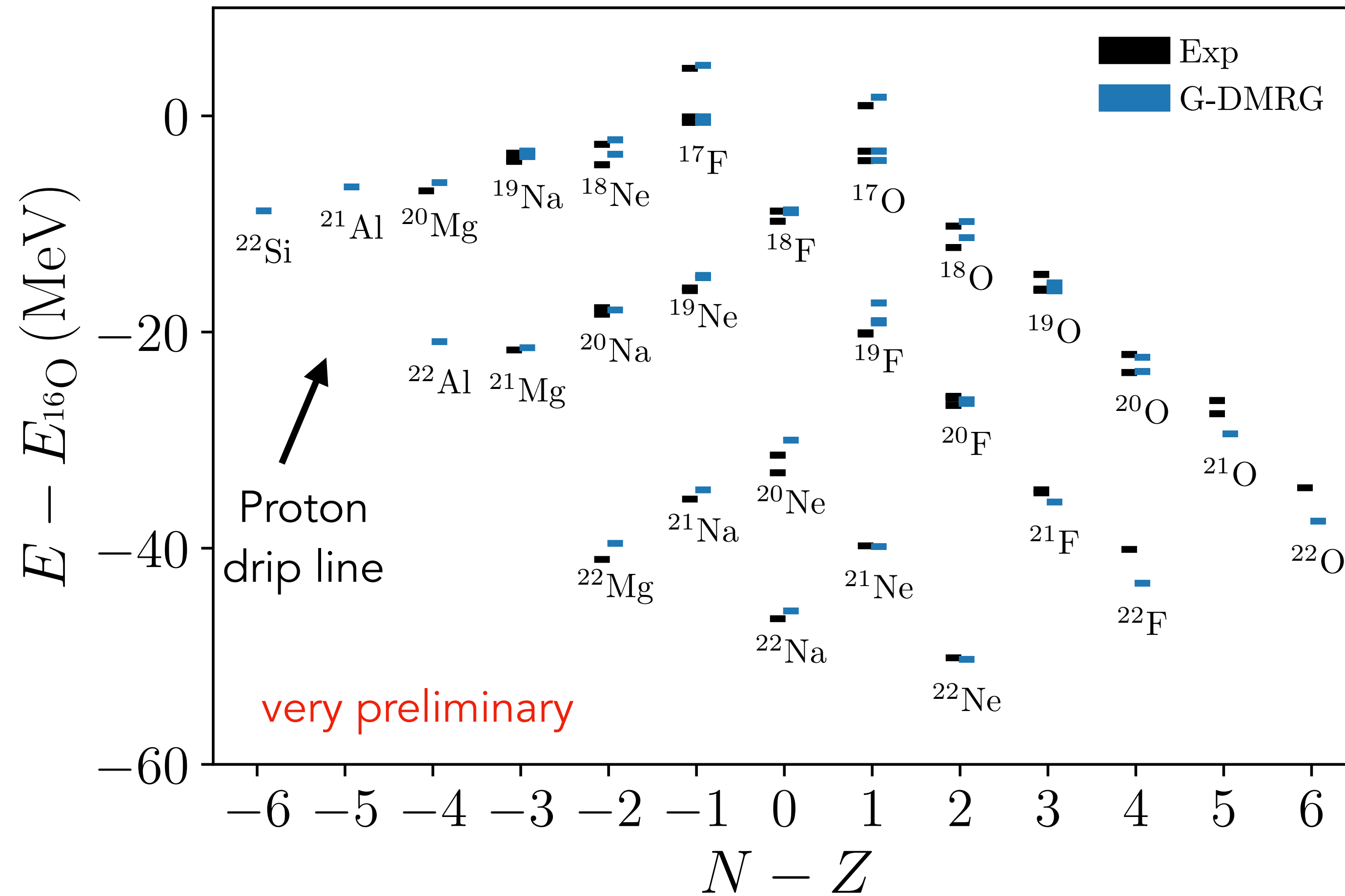


Then, nucleon-nucleon interaction adjusted on  $A+2,3$  systems only.



# Studying drip line nuclei in practice

Similar results form an effective core of  $^{16}\text{O}$  in  $sd$  space with continuum (very preliminary):



Far from USDB but approaching current *ab initio* precision.

All nucleons can couple to the continuum ( $s_{1/2}$ ,  $d_{5/2}$ ,  $d_{3/2}$ ).

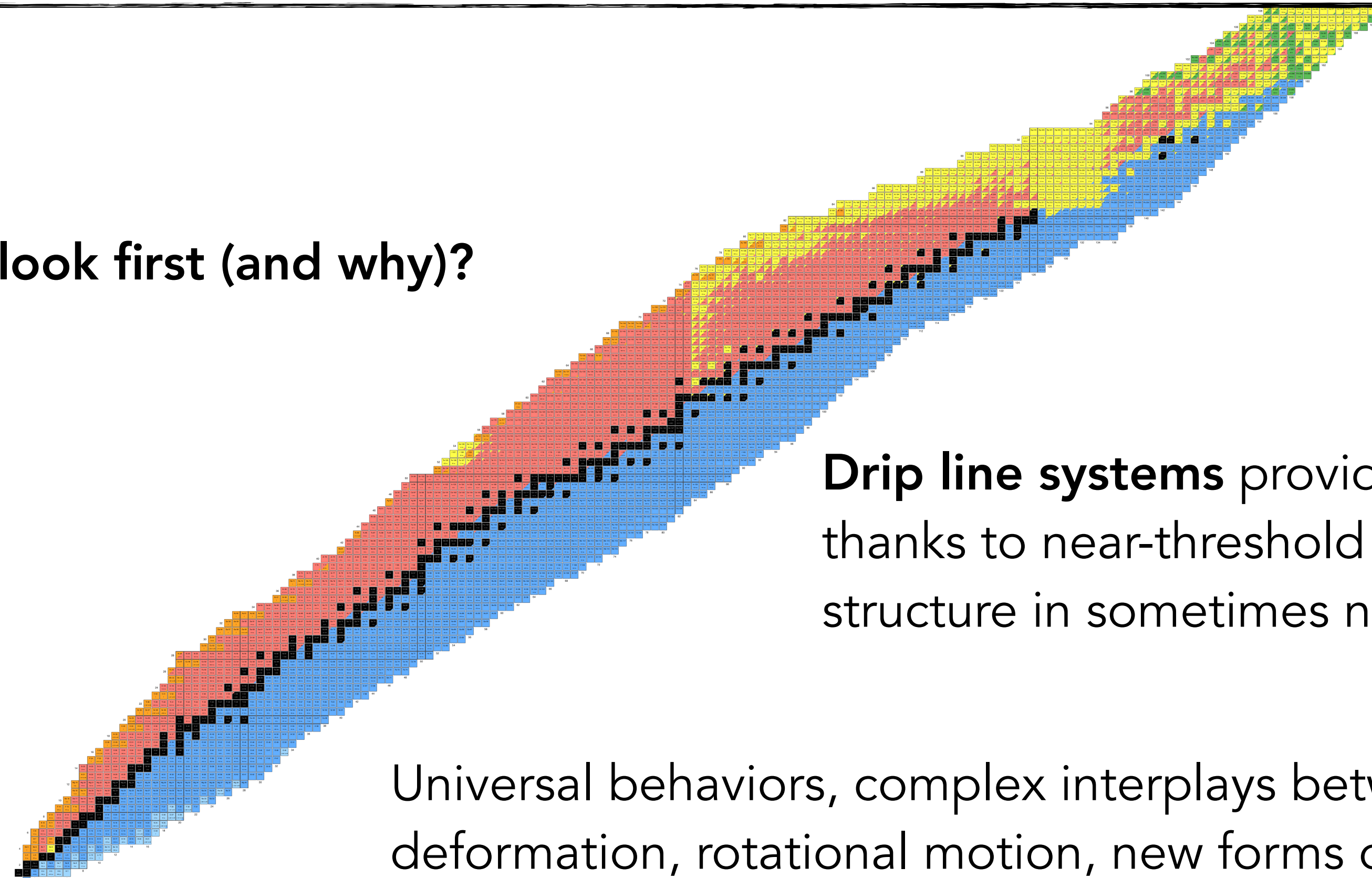
Extension to a core of  $^{40}\text{Ca}$  possible.

(The emergence of universality might make it possible to reach  $^{60}\text{Ca}$ .)

# An (old?) idea for future high-impact FRIB experiments

Find the systems or areas of the nuclear chart where new/unique/sensitive emergent phenomena magnify less known aspects of nuclear forces.

Where should we look first (and why)?



**Drip line systems** provide excellent opportunities thanks to near-threshold physics modifying nuclear structure in sometimes new and various ways.

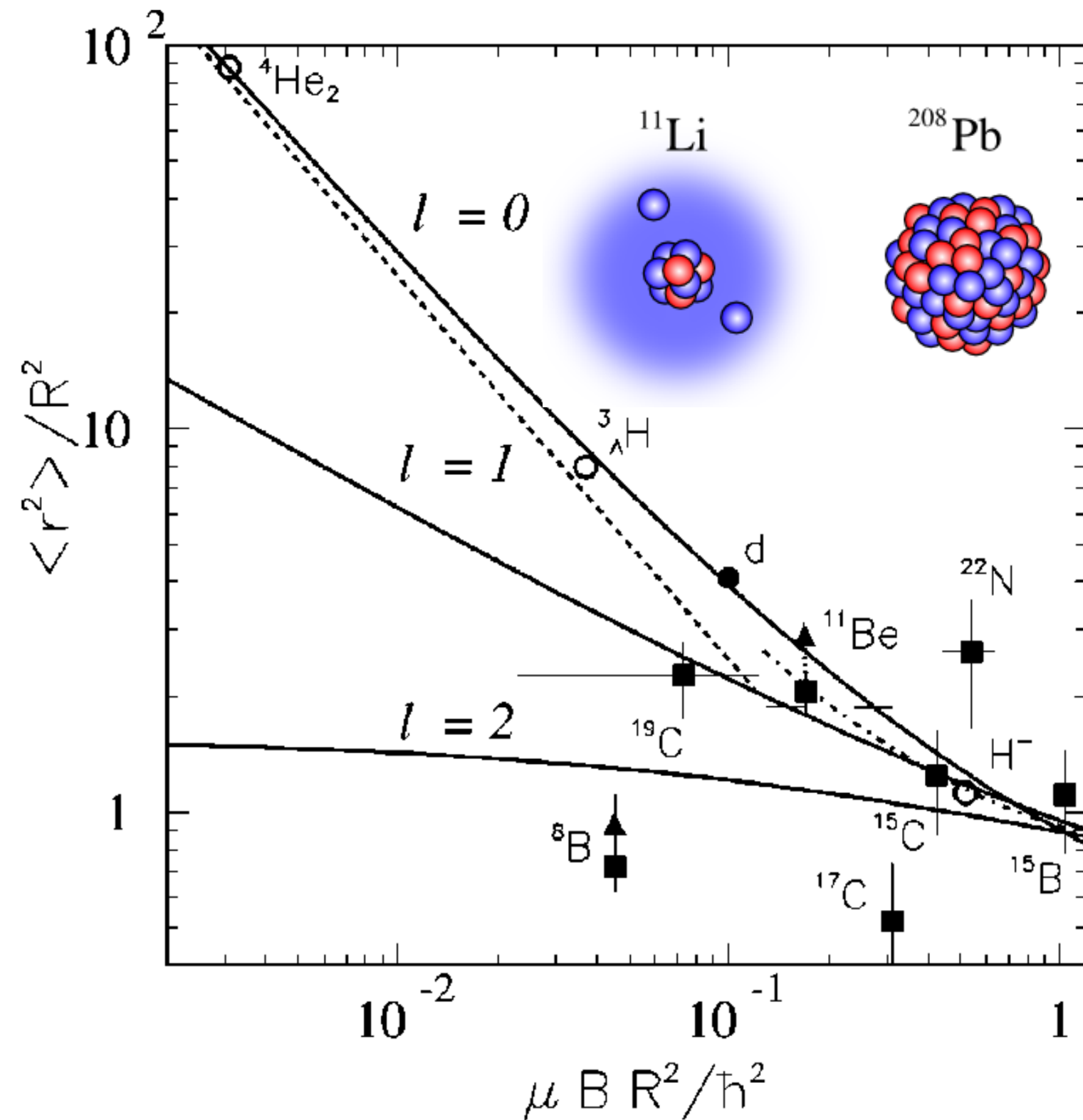
Universal behaviors, complex interplays between decay and clustering, deformation, rotational motion, new forms of radioactivity...

# Known examples

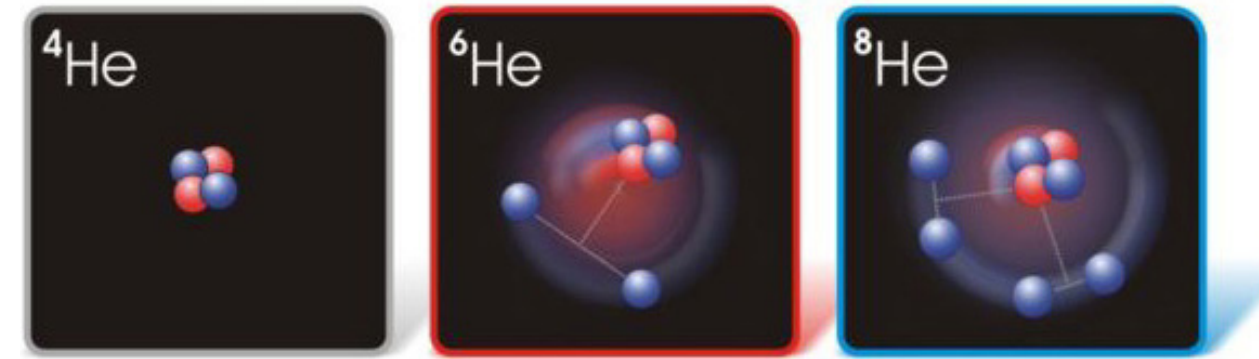
Halo structures

I. Tanihata *et al.*, *Phys. Rev. Lett.* **55**, 2676 (1985)

A. S. Jensen *et al.*, *Rev. Mod. Phys.* **76**, 215 (2004)

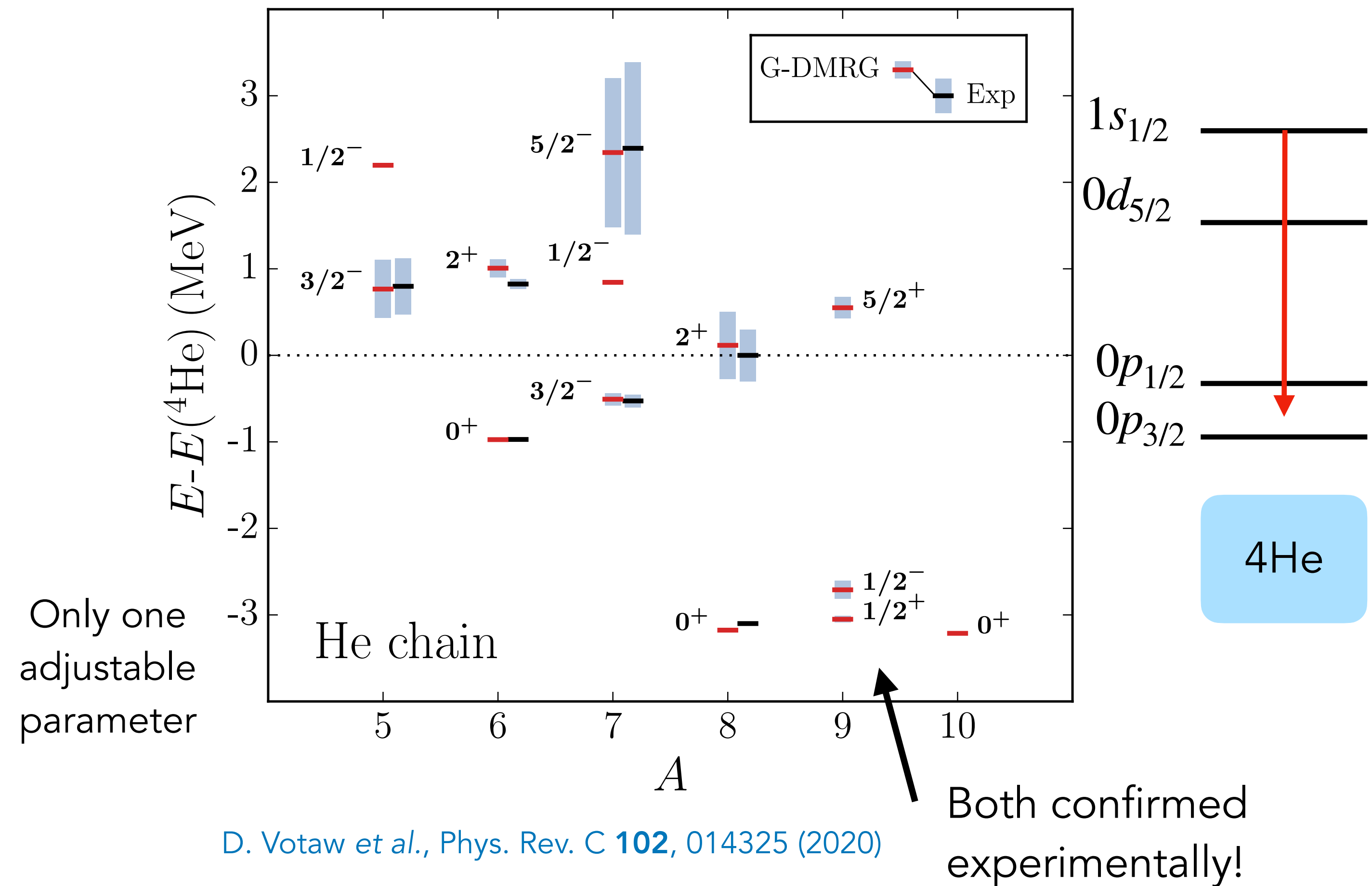
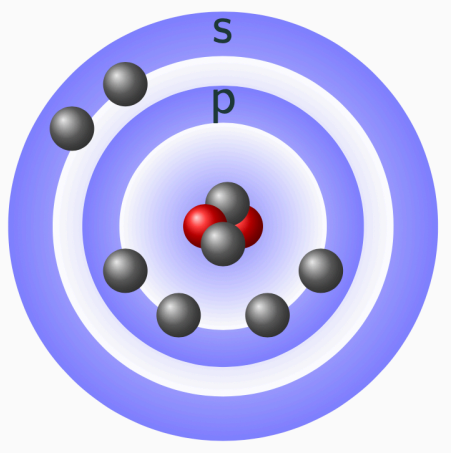


K. Fosse, FSU - FRIB Bridge



Many-body dynamic in the  $6n$ -continuum:  
toward universal behaviors.

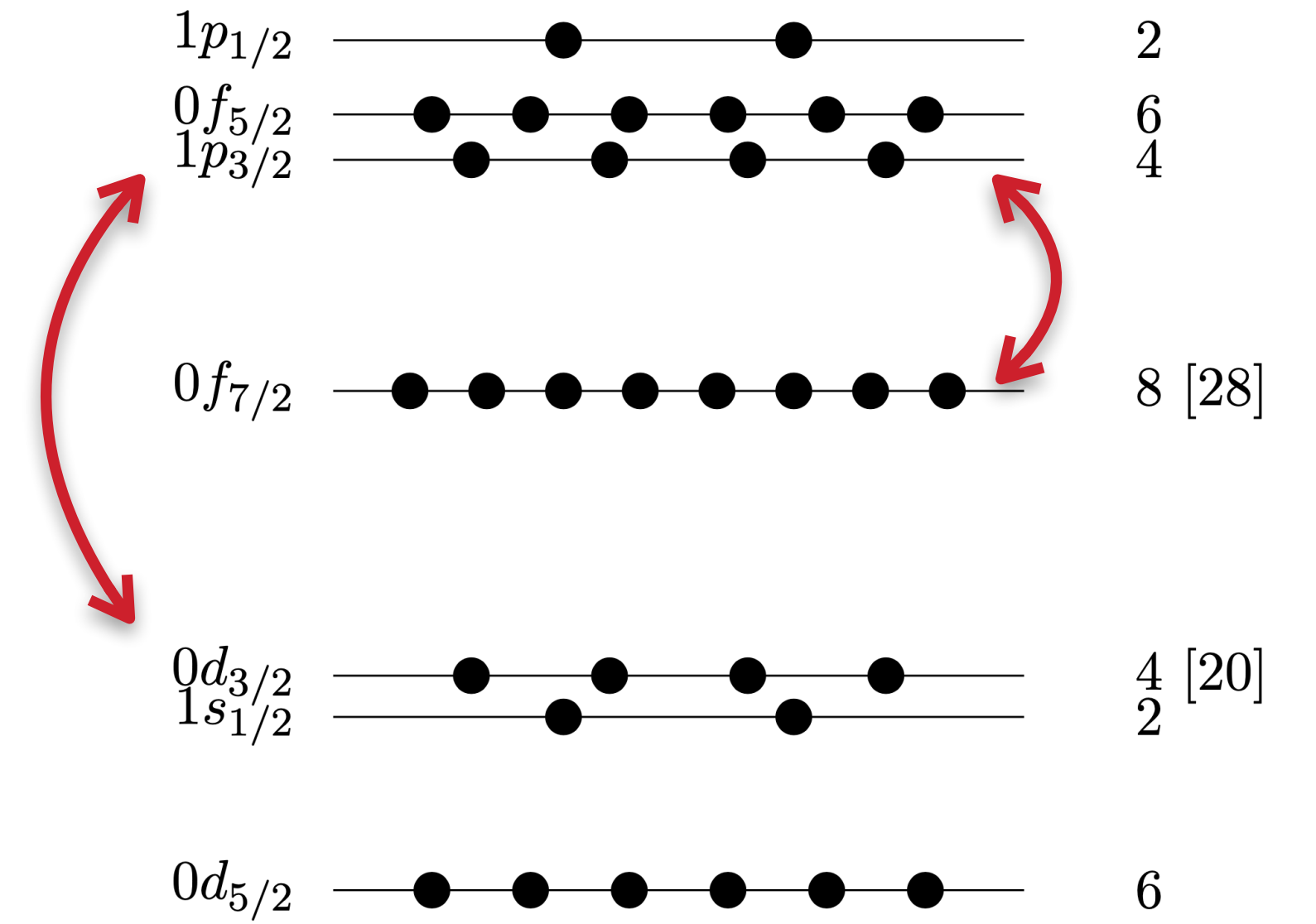
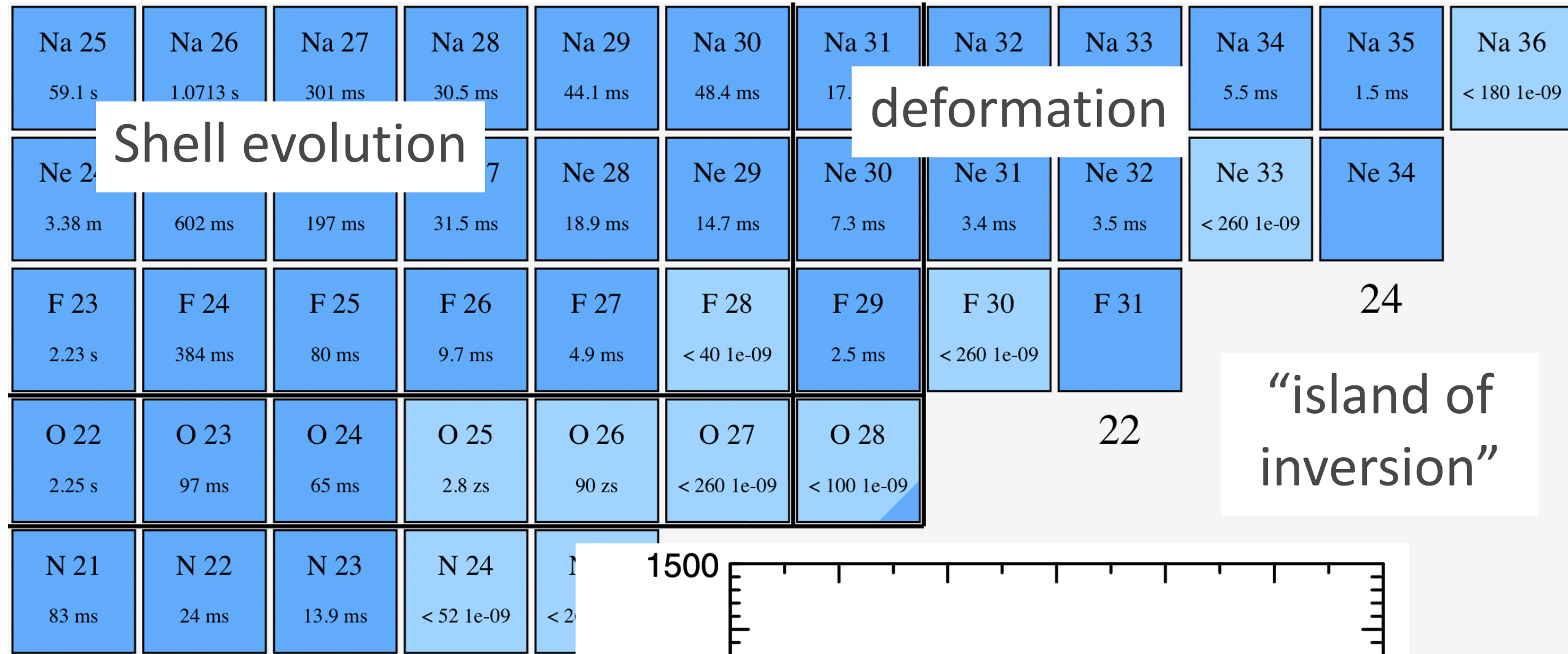
K. Fosse, *Phys. Rev. C* **98**, 061302(R) (2018)



D. Votaw *et al.*, *Phys. Rev. C* **102**, 014325 (2020)

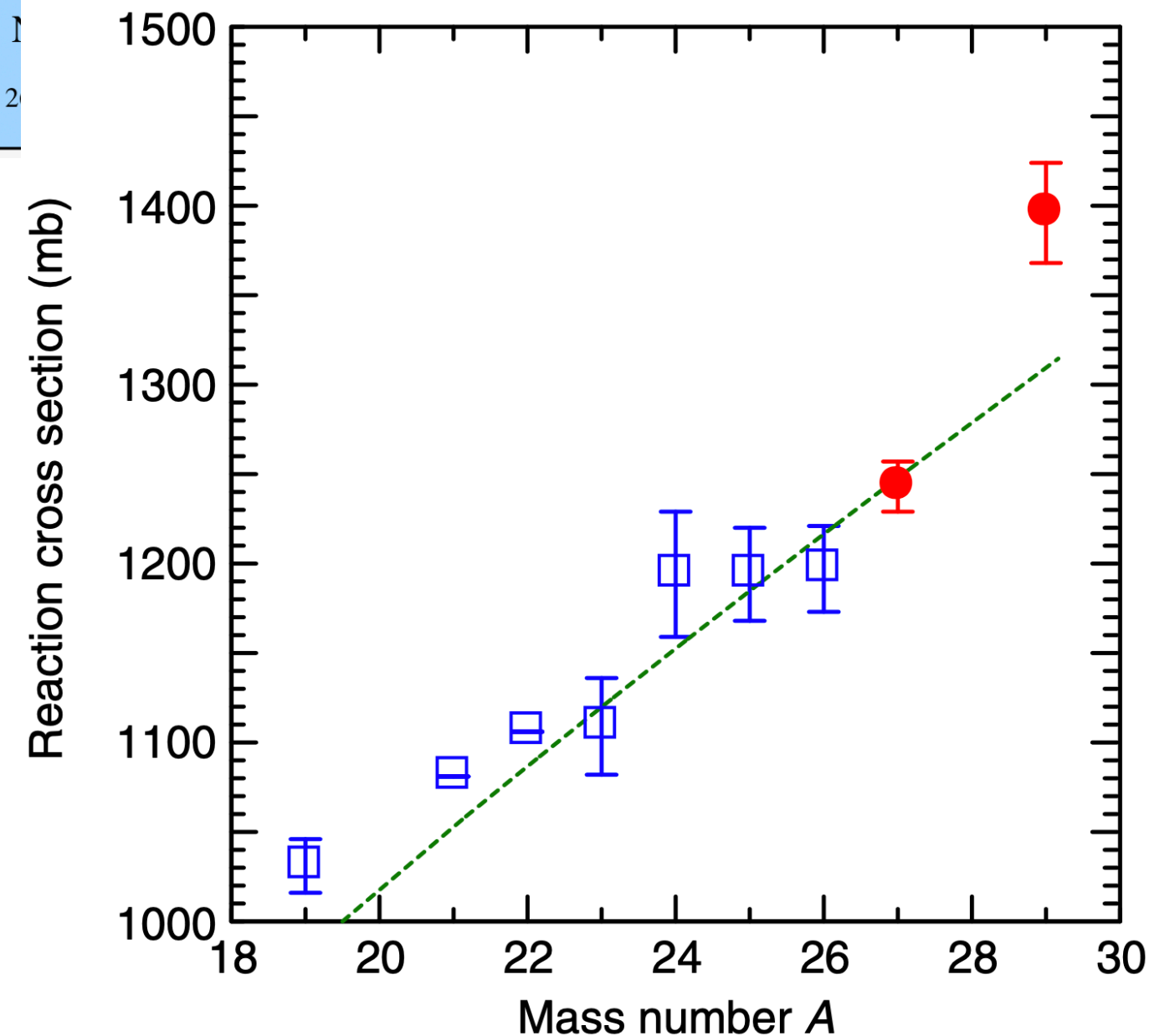
# Continuum inducing deformation?

Continuum couplings decrease the  $\nu 1p_{3/2} - \nu 0f_{7/2}$  gap.

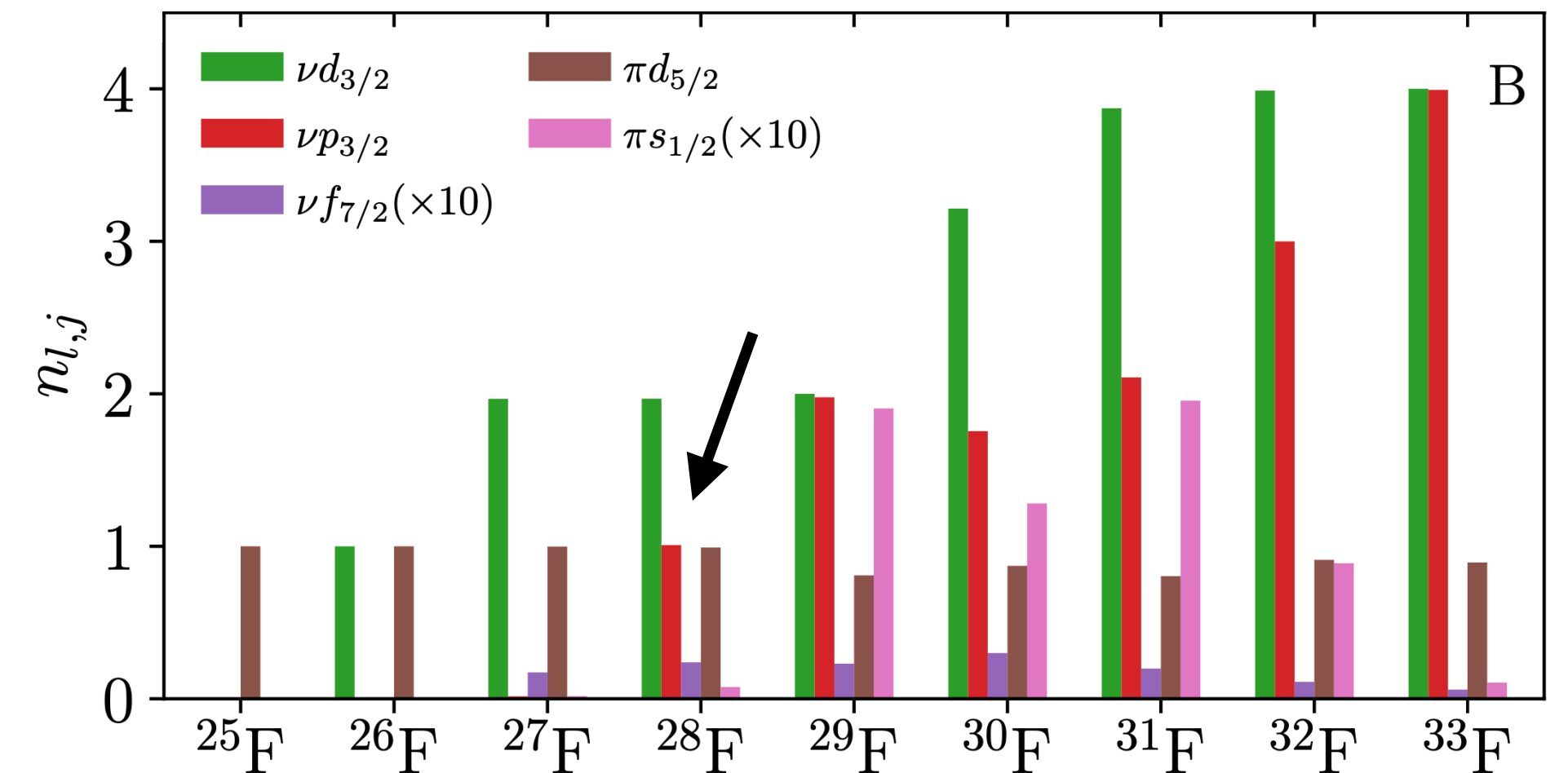


A. Revel et al., Phys. Rev. Lett. **124**, 152502 (2020)

S. Bagchi et al., Phys. Rev. Lett. **124**, 222504 (2020)



K. Fosse et al., PRC **106**, 034312 (2022)



# Suggestion for finding interesting mechanisms

**Continuum-induced deformation:** Look for areas where s/p-waves come down (neutron).

See H. Iwasaki's talk

→  $^{38}\text{Ne}$ ,  $^{39}\text{Na}$  ( $N=20$ ) fill the  $0f_{7/2}$ , the  $1p_{3/2}$  might go down as in 28-31F.

[D. S. Ahn et al., Phys. Rev. Lett. \*\*123\*\*, 212501 \(2019\)](#)

→  $^{22}\text{Si}$  ( $Z=14$ ,  $N=8$ ), should fill the  $0d_{5/2}$  but the  $1s_{1/2}$  might go down. Similar in neutron-rich N isotopes.

**Universality:** Look for situations with a well-bound spherical core + many neutrons like in neutron-rich He and O, and compare with their mirrors.

→ systematic of masses in neutron-rich C ( $Z=6$ ), Ca ( $Z=20$ ), and proton-rich  $N=6, 8, 20$  chains.

→ correlations between the valence nucleons.

→ multi-neutron/proton decay (neutron-rich Be, O).

See D. Lee's talk

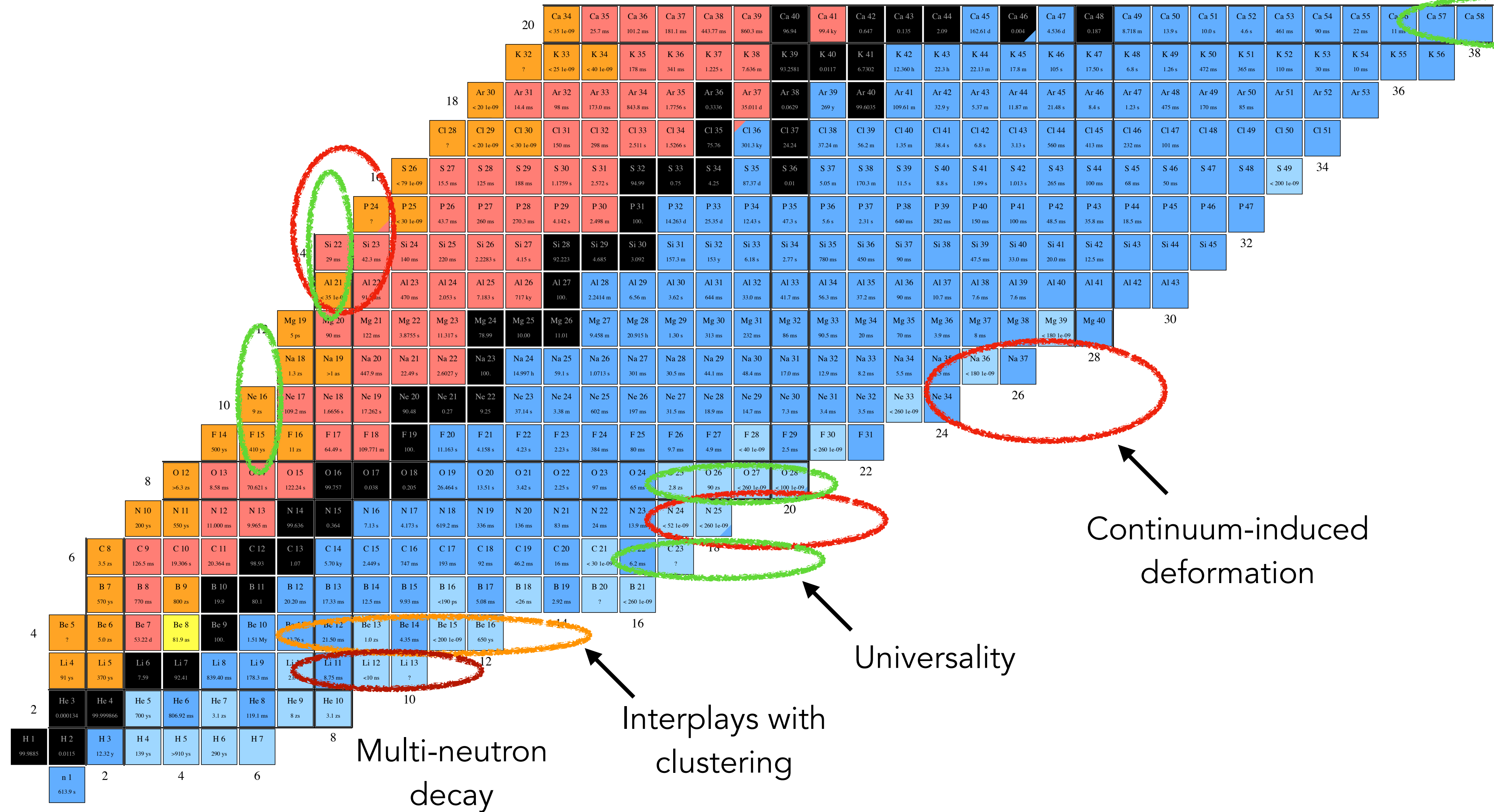
**Interplays between weak binding/decay and clustering:**

→ radii/moments =  $f(N/Z)$  in deformed/clustered + weakly bound/unbound n/p (neutron-rich Li, Be).

→ look for systems with nearby proton, neutron, and cluster decay channels and search for new states.

See A. Volya's talk

# Suggestion for finding similar mechanisms



Thank you for your attention!

DOE: DE-SC0013617 (Office of Nuclear Physics, FRIB Theory Alliance)