



A Quick Overview of Some Microscopic Approaches to Nuclear Reactions

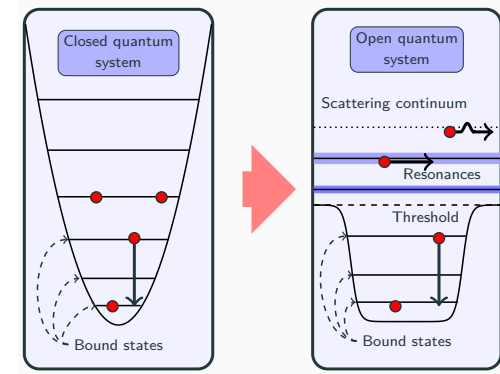
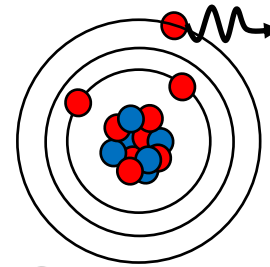
**Alexis Mercenne
Louisiana State University**

Theoretical Description of Exotic Nuclei

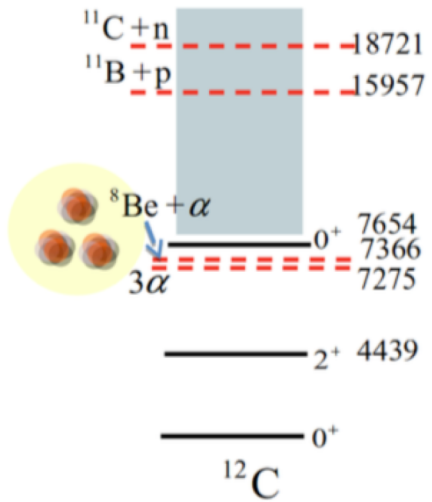
D. Bazin et al., *arXiv:2211.06281*

New features:

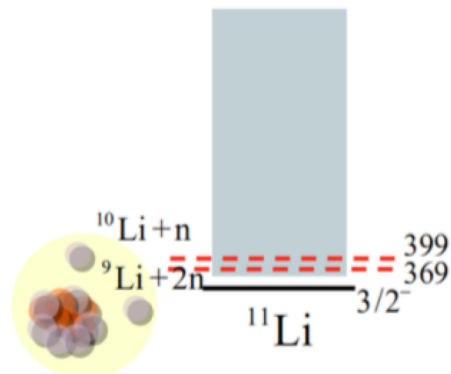
- Open quantum systems.
- Unstable: short life time, decay through nucleon emission.
- Threshold emissions.
- Loosely bound states.
- Resonances.



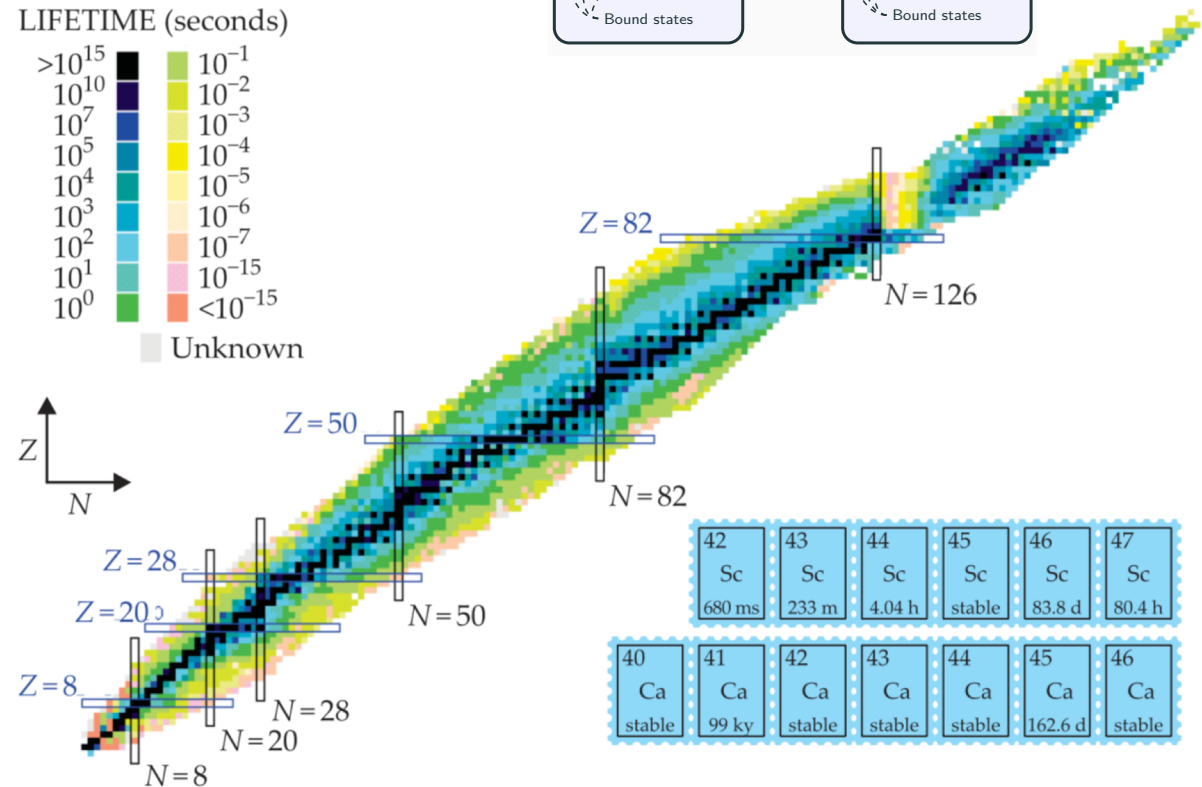
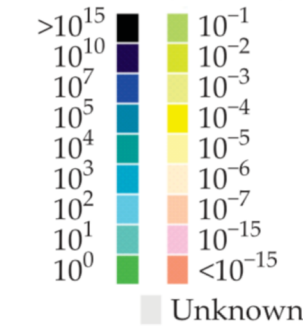
α - cluster state



halo state



LIFETIME (seconds)

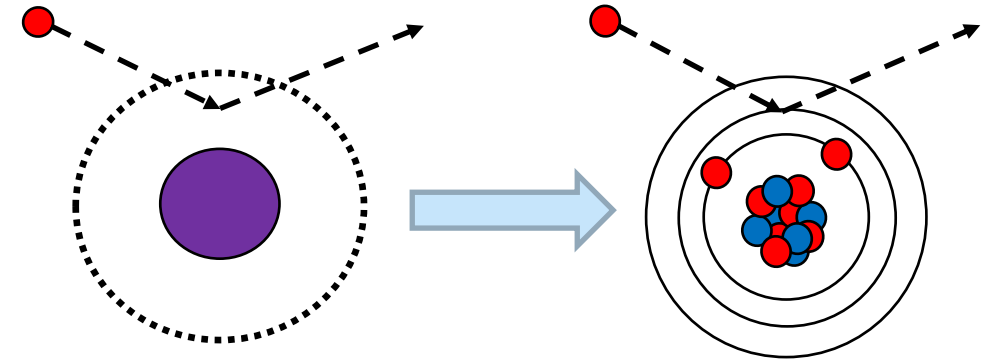


Few-body vs Many-body approaches: Unification of Structure and Reactions

Few-body approach:

- Simpler calculations: two- or three-body generally.
- Optical potentials: imaginary part to mimic the effect of inelastic channels; parameters are fitted on data.
- Allows to study many types of reaction across the nuclear chart.
- Many approaches are now developing optical potentials from microscopic calculations.

C. Hebborn et al., *J. Phys. G: Nucl. Part. Phys.* **50** 060501 (2023)



We eventually want to implement reactants wave functions

$$C_1 \text{ [Diagram 1]} + C_2 \text{ [Diagram 2]} + C_3 \text{ [Diagram 3]} + \dots$$

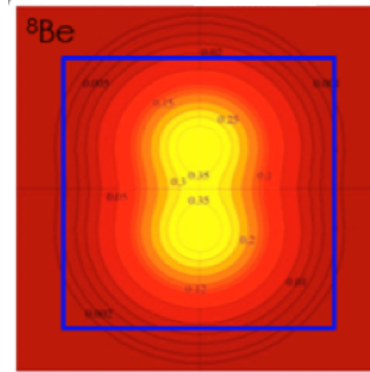
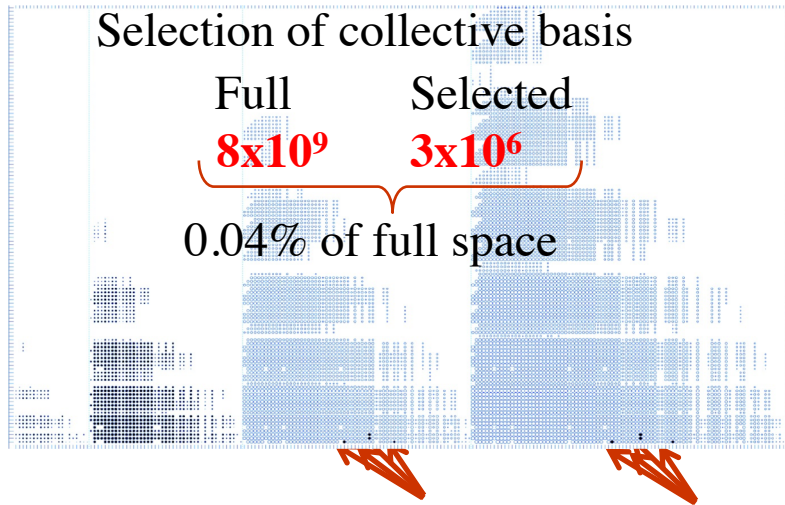
The diagram shows three potential wells, each containing a different configuration of red and blue nucleons. The first well has a small cluster of nucleons at the bottom. The second well has a larger cluster. The third well has a cluster with more nucleons. The coefficients C_1 , C_2 , and C_3 are placed to the left of each well, and an ellipsis follows the third well.

Many-body approach:

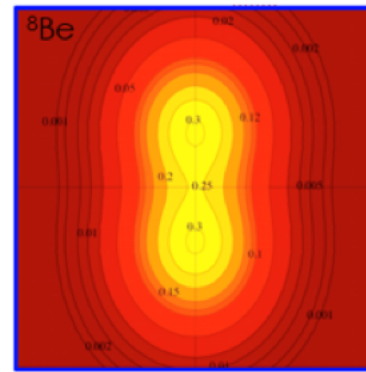
- Structure of reactants play an important role.
- Complexity increases fast with light projectile and multi-partition calculations.

Ab Initio Wave Functions for Nuclear Reactions

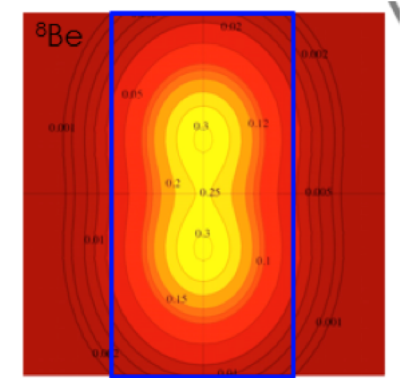
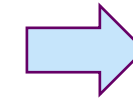
Symmetry-adapted No-core Shell Model



Small model space



Large model space



Selected model space

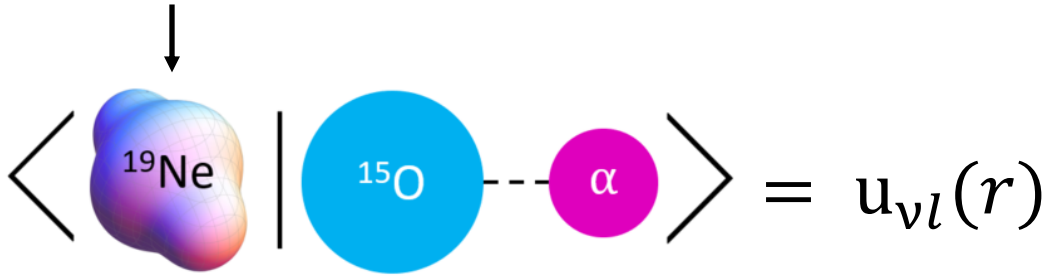
- *Ab initio*: no-core shell model calculations, chiral EFT interactions.
- Physically relevant basis states: better captures collectivity.
- Selection of the most important basis states: capture relevant correlation.
- Manageable model space, can push further the limit of *ab initio* calculations.

$$C_1 \begin{array}{c} \cup \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \cup \end{array} + C_2 \begin{array}{c} \cup \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \cup \end{array} + C_3 \begin{array}{c} \cup \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \cup \end{array} + \dots$$

$$B_1 \begin{array}{c} \cup \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \cup \end{array} + B_2 \begin{array}{c} \cup \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \cup \end{array} + B_3 \begin{array}{c} \cup \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \cup \end{array} + \dots$$

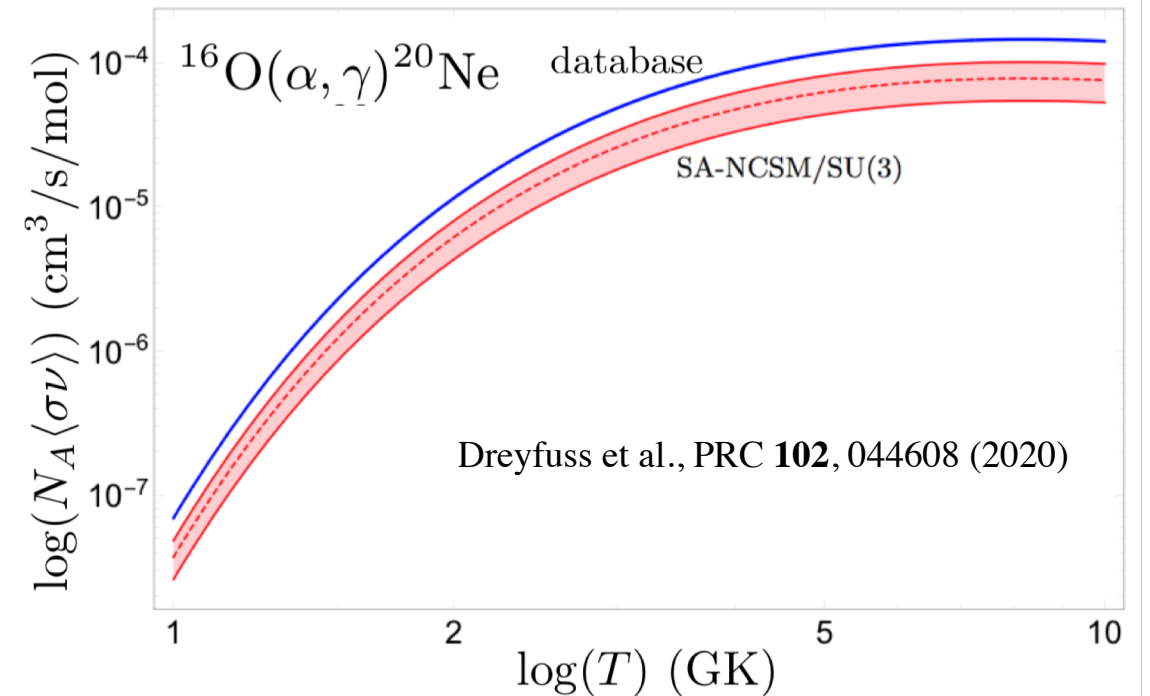
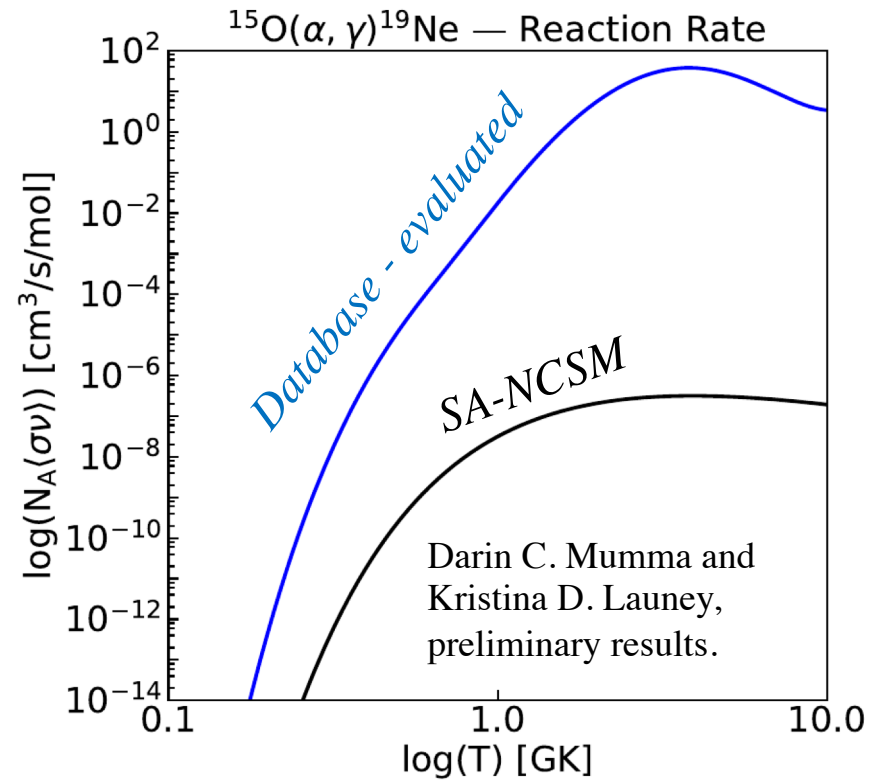
SA-NCSM wave function

Ab Initio Overlap Functions



- Relevant for astrophysics: Triggers CNO-cycle breakout.

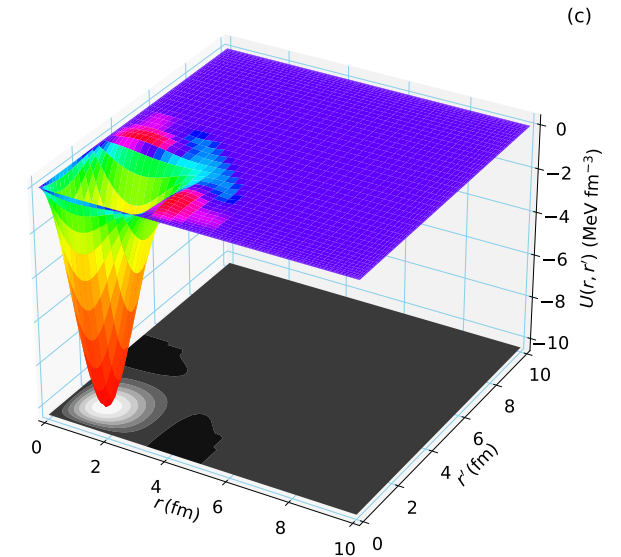
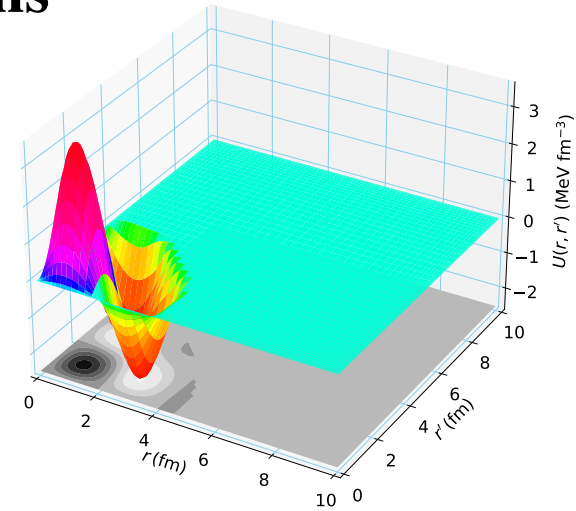
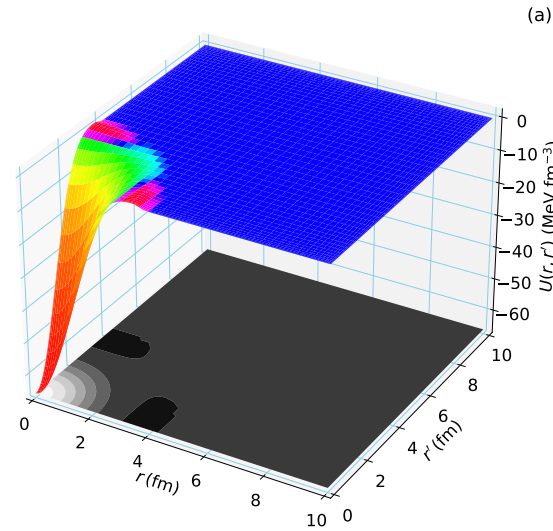
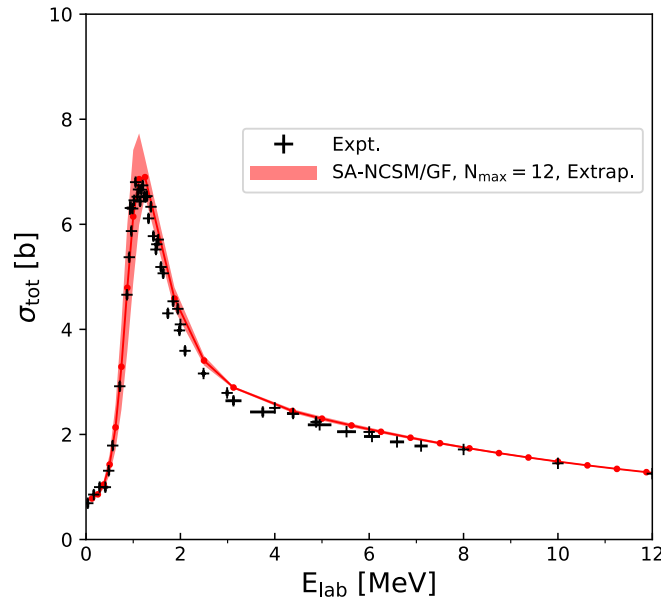
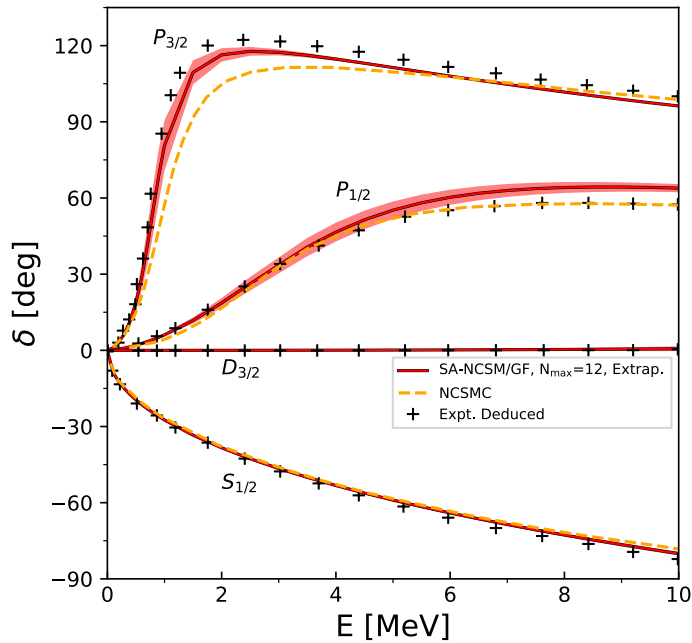
- Rate uses narrow-resonance formula, deduced the matching with asymptotic scattering w.f.
- Calculated rate is a many order of magnitude smaller than evaluated.



Optical Potential Derived from *Ab Initio* Calculations

- ^4He wave function calculated with SA-NCSM.
- Optical potential describing neutron scattering on ^4He constructed with Green's function method.

Matthew Burrows and Kristina Launey, preliminary results



Coupled-channels Framework for Nuclear Reactions

Everything starts here:

$$(T_c - (E - E_c))u_c(r) + \sum_{c'=1}^{N_c} \int dr' V_{cc'}(r', r)u_{c'}(r') = 0$$

Kinetic part

Scattering energy
Threshold energy

Coupling potential

Solution

Can be solved with calculable R-matrix.

a.k.a optical potential, inter-cluster interaction, nucleon-nucleus potential ...etc

A basis for reactions: channel index gathers partitions, quantum numbers of projectile and target, total angular momentum of composite ...etc

$$c = \{A I_T; a I_p; n\ell j; J\}$$

Low Energy Reactions With the Resonating Group Method (RGM)

- $u_c(r)$ describes the relative motion between the two clusters.
- Asymptotic of $u_c(r)$ gives cross section for specific channel.
- Requires internal wave functions and NN interaction.
- Microscopic: full antisymmetrization + cluster correlations.
- Can be generalized to any number of clusters.

$$|\Psi\rangle = \sum_c \int dr \frac{u_c(r)}{r} r^2 \mathcal{A} \left\{ \left[\text{cluster} \right] - \vec{r} - \left[\text{cluster} \right] \right\}$$

$$|\Phi\rangle = \sum_i C_i \left[\text{cluster} \right]_i$$

$$c = \{A I_T; a I_p; n\ell j; J\}$$

$$\left\{ \left[\text{cluster} \right]_{c'} - \vec{r}' - \left[\text{cluster} \right] \right\} \hat{H} \left\{ \left[\text{cluster} \right] - \vec{r} - \left[\text{cluster} \right] \right\}$$

$$(T_c - (E - E_c))u_c(r) + \sum_{c'=1}^{N_c} \int dr' V_{cc'}(r', r)u_{c'}(r') = 0$$

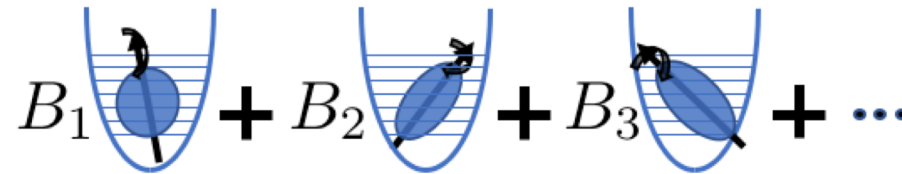
Implementing Shell-model Wave Functions into Reactions

$$V_{cc'}(r, r') \equiv \left\{ \begin{array}{c} \vec{r}' \\ \text{Core} \\ c' \end{array} \right\} \hat{H} \left\{ \begin{array}{c} \vec{r} \\ \text{Core} \\ c \end{array} \right\}$$



Symmetry-adapted No-core Shell-model

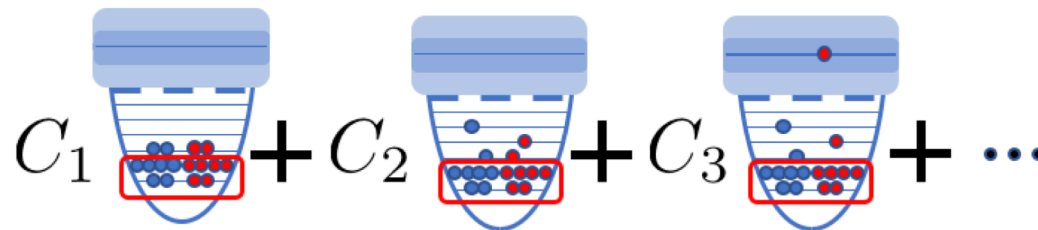
- All nucleons are active.
- Chiral EFT interaction.



SA-NCSM+RGM = SA-RGM

Gamow Shell Model

- Core + valence nucleons.
- Schematic interaction.



GSM+RGM = GSM-CC

Ab Initio Nuclear Reactions with Nuclei Up to Medium-mass Region

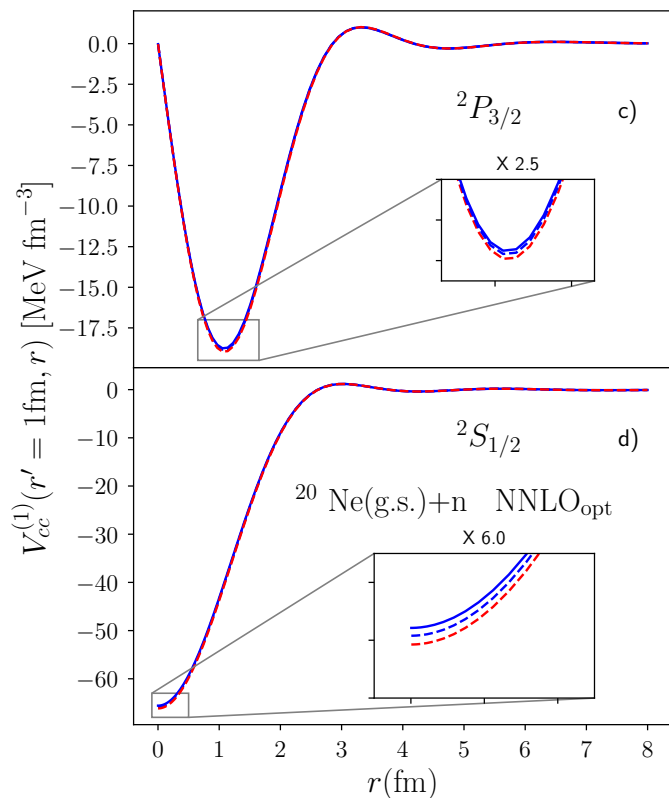
Symmetry-adapted RGM:

- *Ab initio* single-nucleon projectile reactions in a coupled-channel framework.
- First results studied the influence of selected model space on non-local potentials.

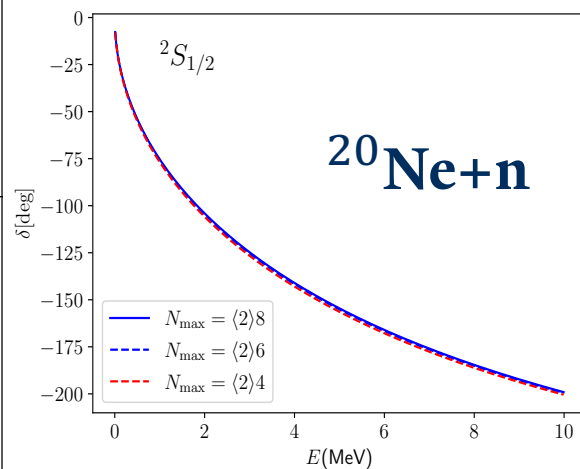
$$|\Psi\rangle = \sum_{\nu} \int dr \frac{g_{\nu}(r)}{r} r^2 \mathcal{A} \left\{ \left(\text{cluster} \right) - \text{nucleon} \right\}$$



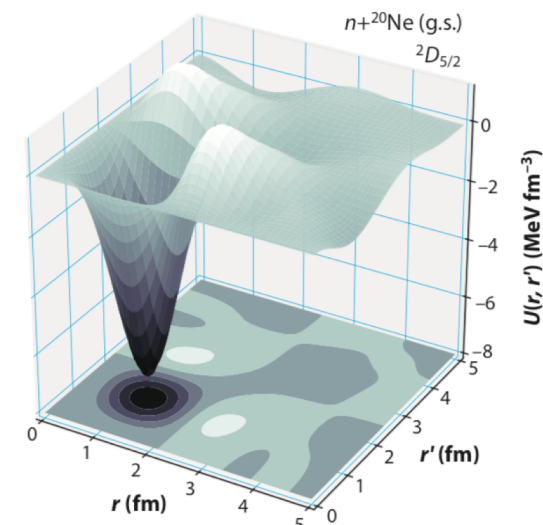
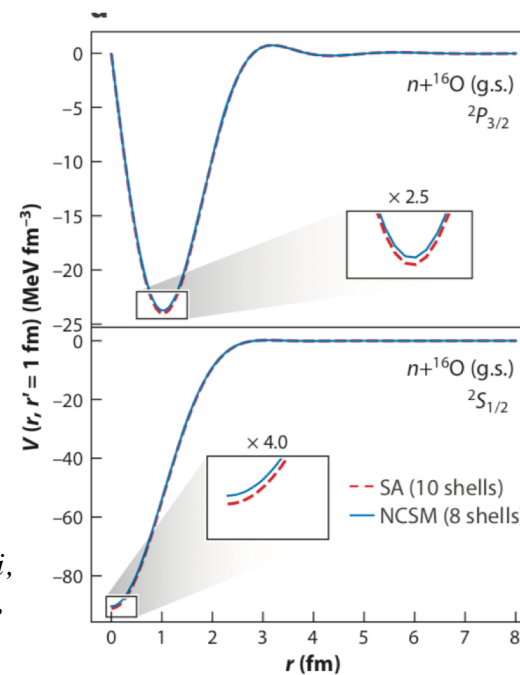
$$|\Phi\rangle = \sum_i C_i \left(\text{cluster} \right)$$



- More to come ...



Mercenne, Launey, Dytrych, Escher, Quaglioni, Sargsyan, Draayer *Comput. Phys. Comm.* **280**, 108476 (2022)

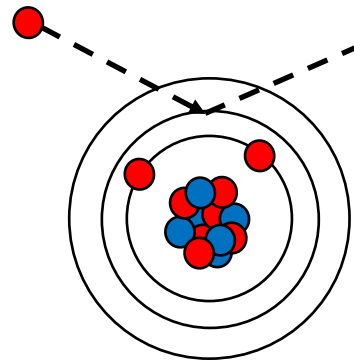


Launey, Mercenne, Dytrych *Ann. Rev. Nucl. Part. Sci.* **71**, 253 (2021)

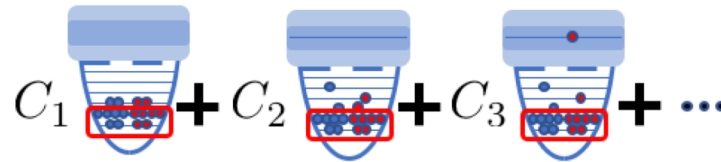
Exotic ^{15}F Studied Through $p + ^{14}\text{O}$ With Gamow Shell Model Coupled Channel

Goal : Study the structure of ^{15}F through the elastic cross section $p + ^{14}\text{O}$

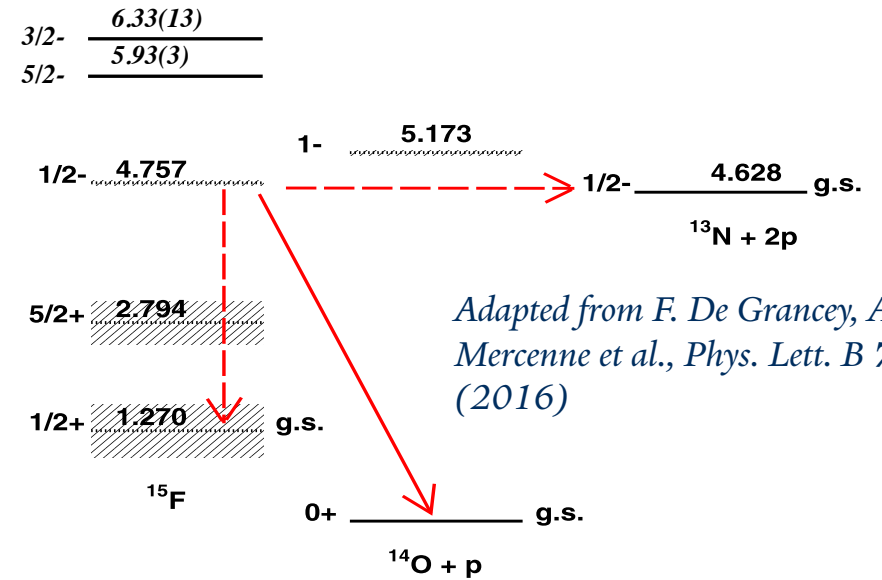
Motivation: ^{15}F is unbound, several measured narrow resonances located well above the Coulomb plus centrifugal barrier.



- Core ^{12}C , 3 valence protons.
- Many channels: 8 states of ^{14}O



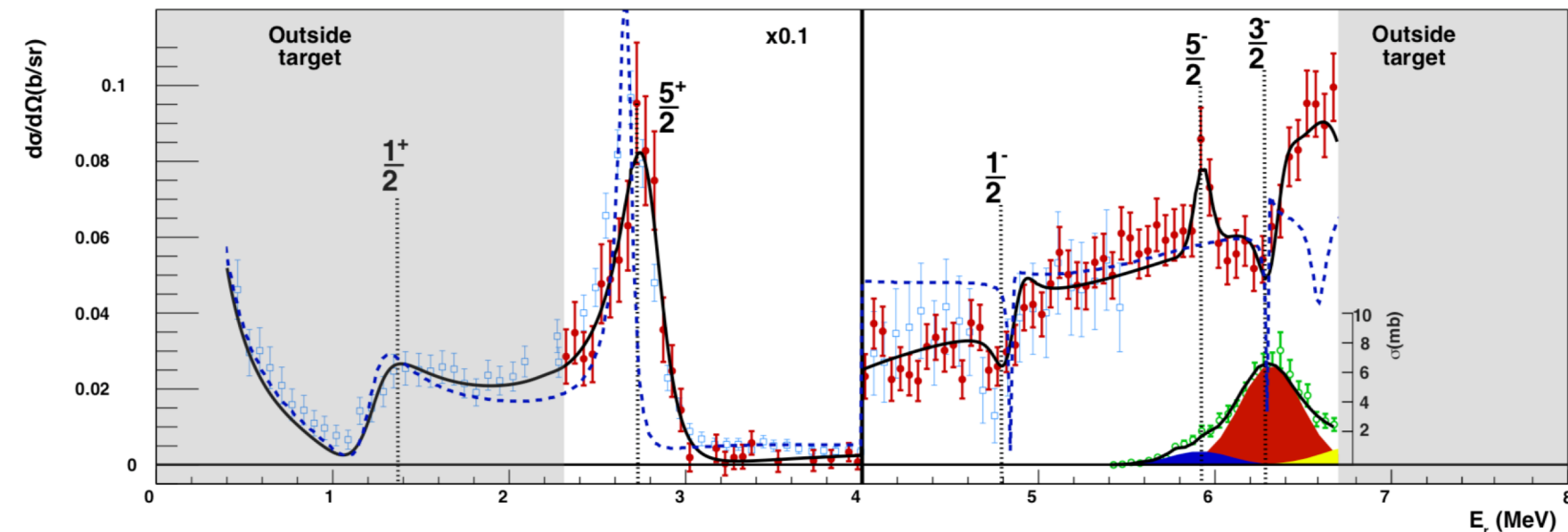
Schematic interaction (FHT) is fitted using GSM to reproduce the low lying states of ^{14}O and ^{15}F



Astrophysics: Properties of ^{15}F , and proton rich systems in general, play an important role in rp-process .

Exotic ^{15}F Studied Through $p+^{14}\text{O}$ With Gamow Shell Model Coupled Channel

V. Girard-Alcindor, A. Mercenne et al., *PRC 105*, L051301 (2022)



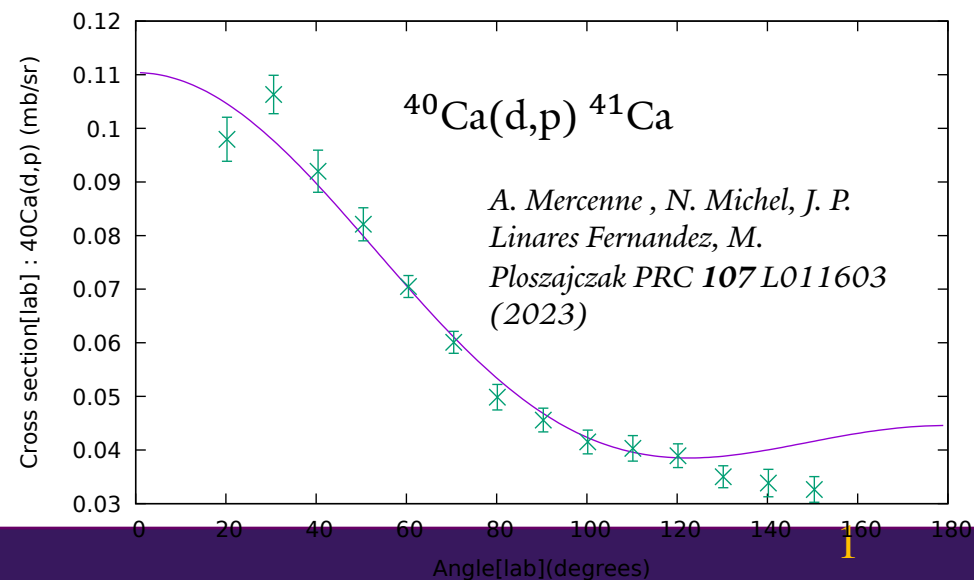
- Collaboration with different experimental team to analyze their results: spin-parity assignment.
- More to come ... Higher resonances detected in another experiments (B. Charity, L. Sobotka et al.)

Manifestation of continuum couplings effect.

Shell-model framework tells us about competition between two decay modes.

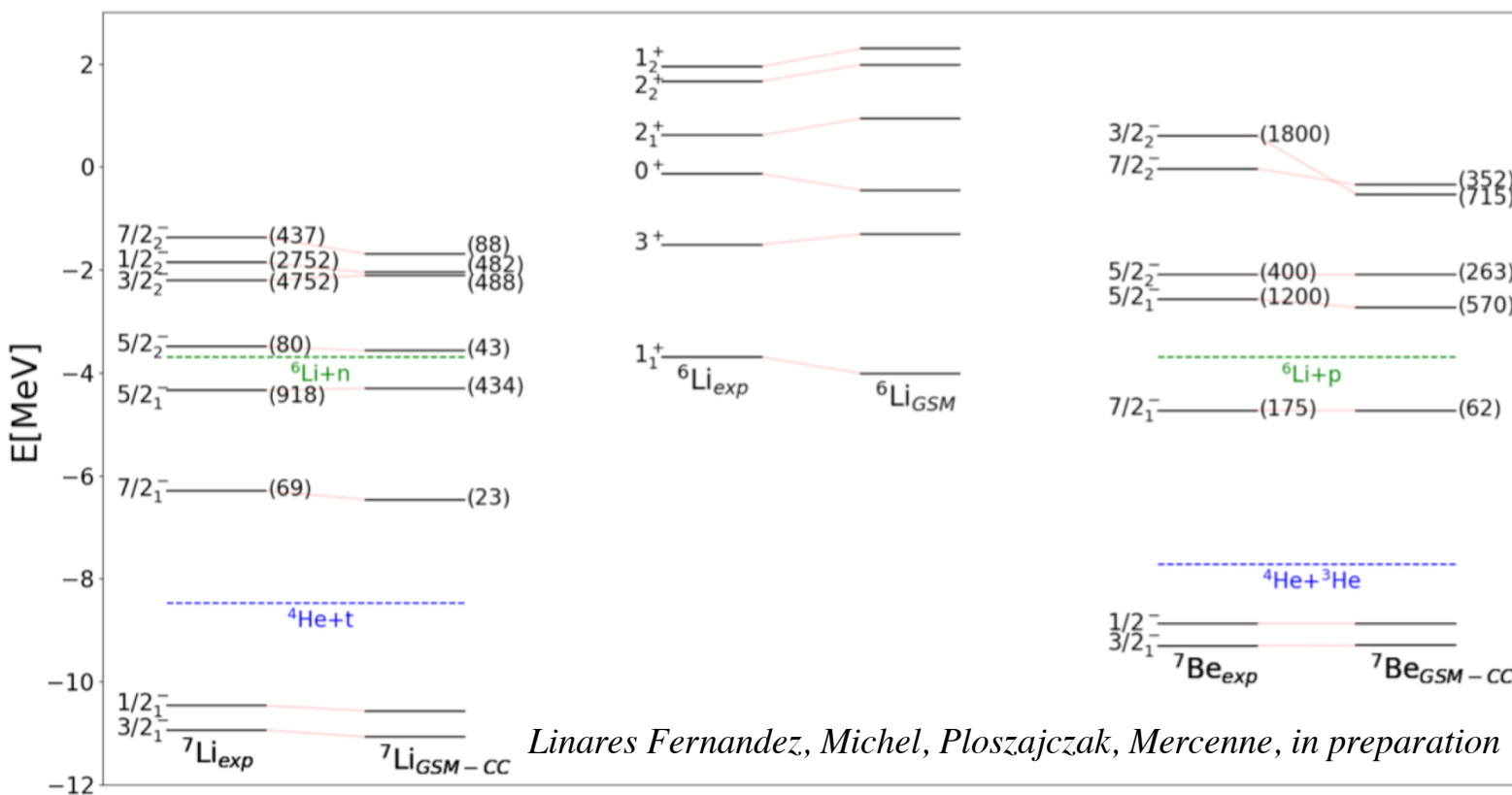
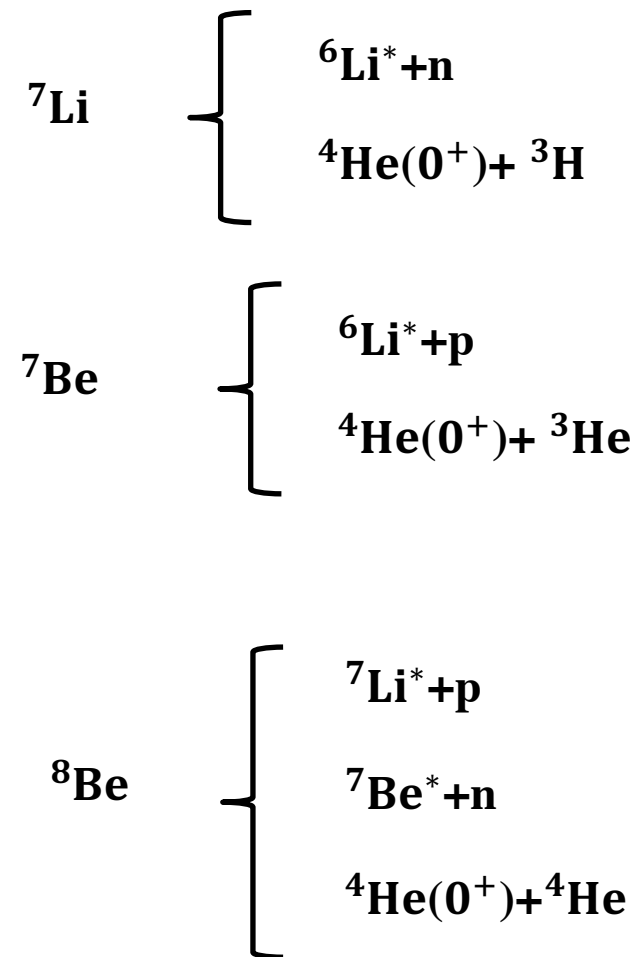
Beyond single-nucleon projectile:

- Generalization of the formalism to complex projectile (deuteron, alpha ...etc) Mercenne, Michel, Ploszajczak, *PRC 99*, 0044606(2019)



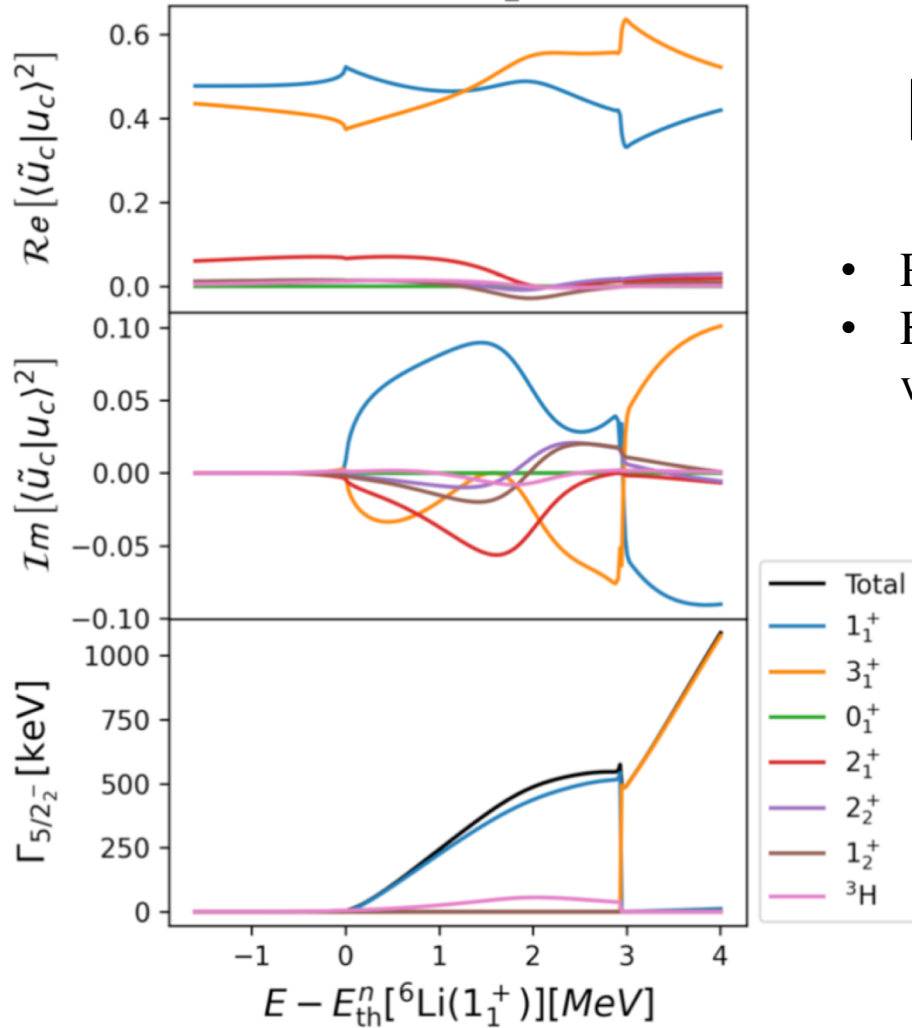
Multi-partition Reactions for ${}^7\text{Li}$, ${}^7\text{Be}$ and ${}^8\text{Be}$ With GSM-CC

${}^4\text{He}$ core + valence particles. Same Hamiltonian to describe ${}^7\text{Be}$ and ${}^7\text{Li}$. Performed GSM (Slater determinant basis) and GSM-CC (channel basis) calculations. Schematic interaction fitted to reproduced low-lying spectra of reactants.



Multi-partition Reactions for ${}^7\text{Li}$, ${}^7\text{Be}$ and ${}^8\text{Be}$ With GSM-CC

${}^7\text{Li}(5/2_2^-)$

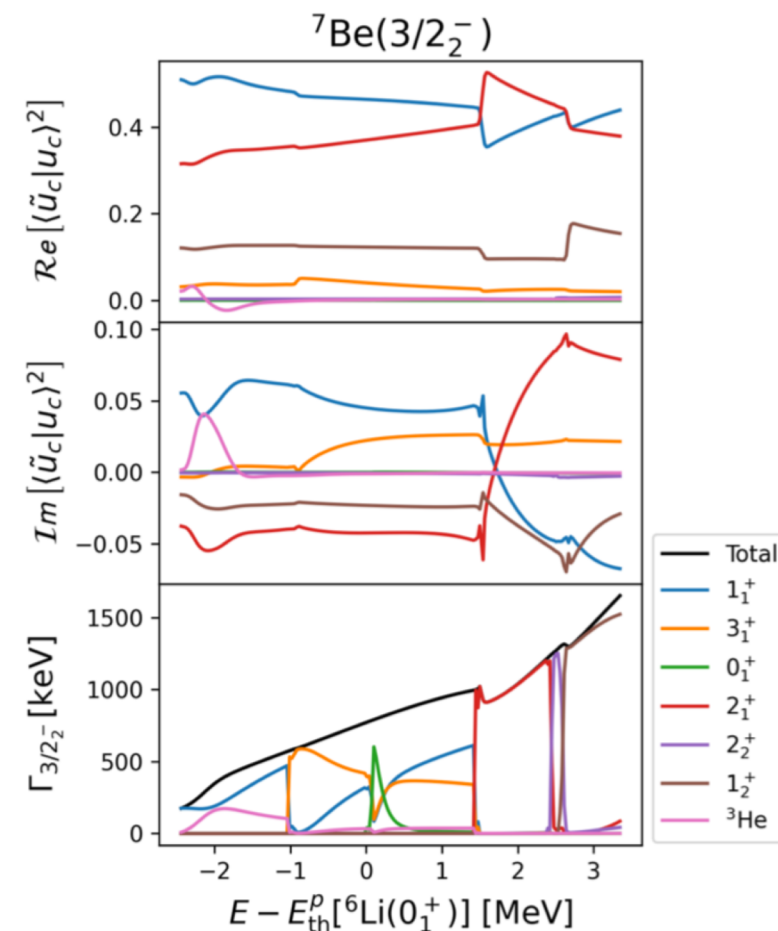
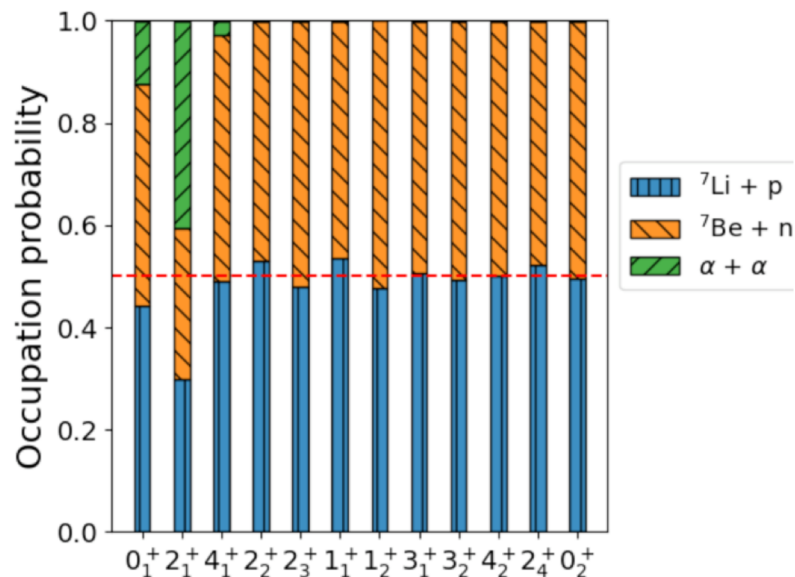
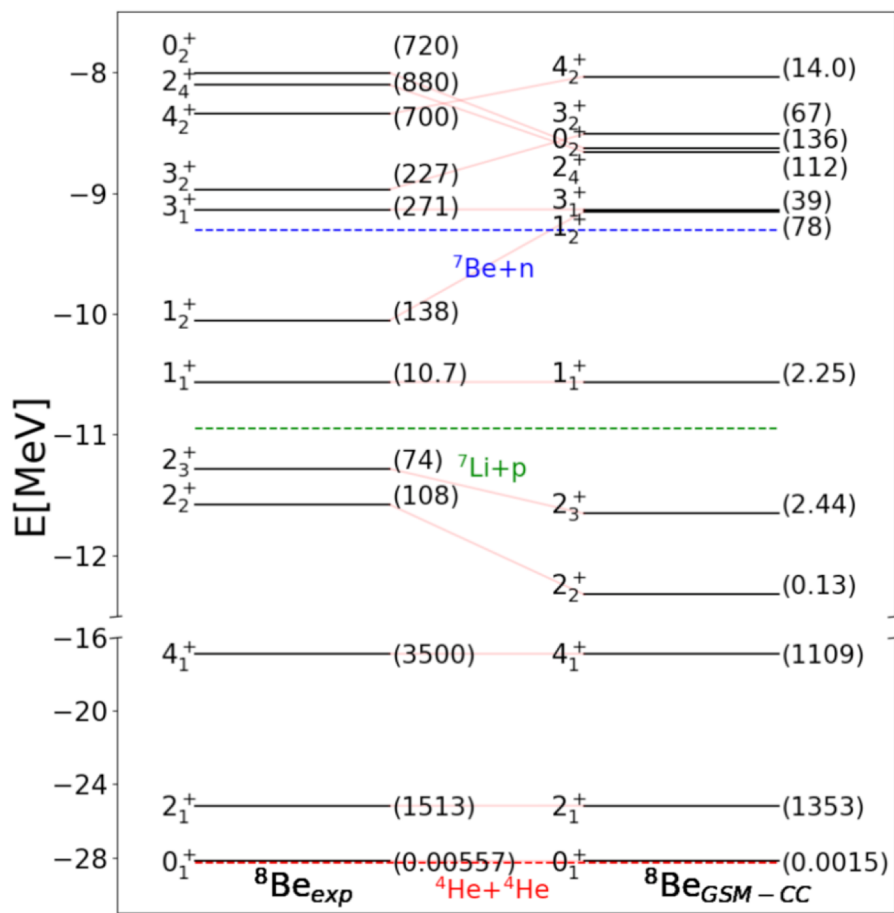


$$|\Psi\rangle = \sum_c \int dr \frac{u_c(r)}{r} r^2 \mathcal{A} \left\{ \left(\begin{array}{c} \text{Cluster} \\ \text{---} \\ \text{Particle} \end{array} \right) \right\}$$

- RGM can tell us more than cross sections.
- Enhancement of the scattering cross section at the threshold energies where new channels open: Wigner cusps.

Linares Fernandez, Michel, Ploszajczak, Mercenne, in preparation

Multi-partition Reactions for ${}^7\text{Li}$, ${}^7\text{Be}$ and ${}^8\text{Be}$ With GSM-CC



Linares Fernandez, Michel, Ploszajczak, Mercenne, in preparation

Summary

- You can already do “reactions” with a structure approach: overlap function can help to calculate reaction rates.
- Structure wave functions are becoming a necessary ingredient for low energy nuclear reactions:
 - To construct optical potentials (i.e. with Green’s function method)
 - For RGM-based approach to coupled-channel calculations.
- Cross sections are the observables that will have the most impact for advancing the science in connection with these theoretical methods.
- Future advances:
 - Uncertainty quantification, especially on models that depend upon fitting an interaction.
 - Pushing further *ab initio* reactions with multi-partition calculations.