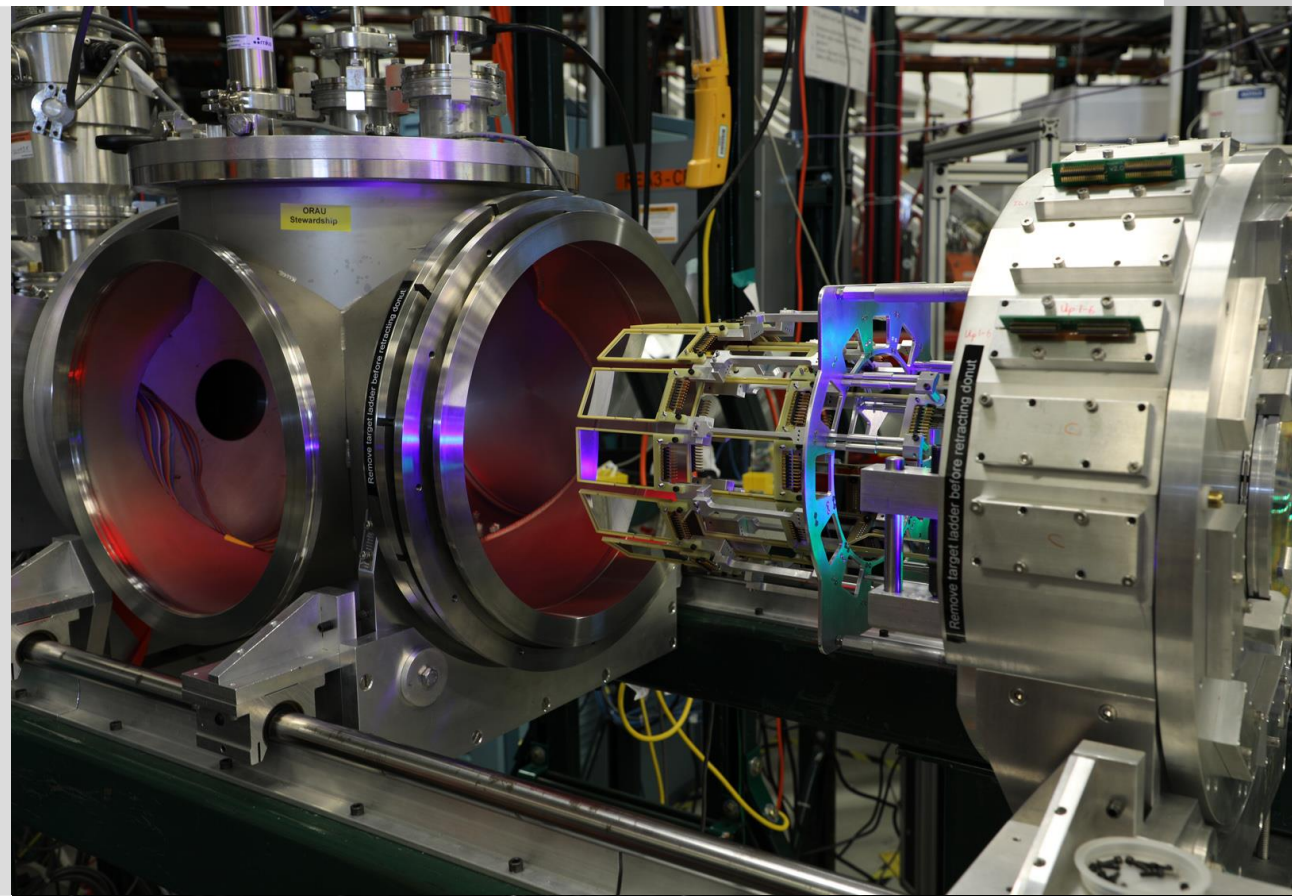


Some (selective) transfer opportunities at FRIB

- Transfer reactions for neutron capture
 - Constraining n-capture/Surrogate reactions with fast beams
- Transfer reactions on isomers
 - sd-shell nuclides
 - Constraining proton capture [(d,p) for (p, γ)]
 - Direct (α ,p)
 - Comparison with SM



Transfer reaction observables

- Level energies (few keV – hundreds keV, depending on reaction, beam and instrumentation)
- (Differential) cross sections
 - transferred orbital angular momenta (parity, some J)
- Decay channels of excited states
 - γ spec
 - γ /particle emission probabilities [discrete, or $P(E_x)$]
- Direct reaction analysis
 - Spectroscopic factors (C^2S)
 - Structure
 - Astrophysics
- Surrogate reactions

Selective of particle/hole states

- Stripping reactions [eg (d,p) (d,n)]
probe of single-particle excitations
- Pickup reactions [eg (p,d) (d, ^3He)]
probe of hole excitations
- Spin through momentum matching
(choice of probe, and beam energy)

Astrophysics

Level energies (exp. affect rates)

Spins (barrier penetrabilities – ell, not J, most important)

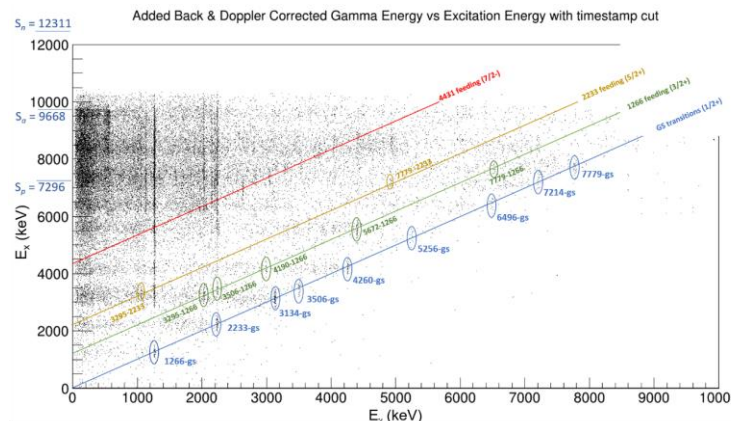
C^2S

Constraints on LD/GSF – eg SRM

Preferentially populates particle excitations (depending on WF, may or may not see via other probes – beta decay, KO, etc)

Branching ratios

Though direct measurements are goal, need to discover important states first by some other means



Transfer reactions at FRIB

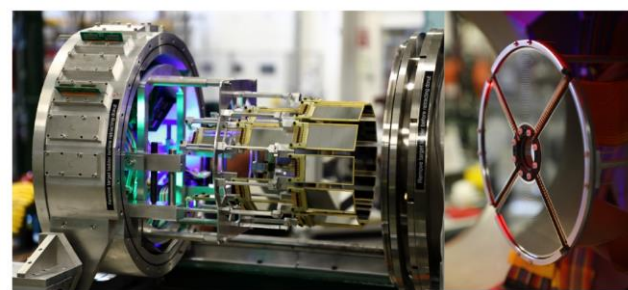
Beam energy $\sim 3\text{-}50$ MeV/A

- Cross sections (absolute and differential)
- Beam intensity
- Kinematic compression
- Beam optics
- Special cases...

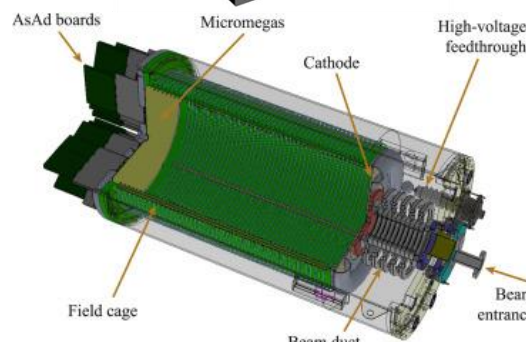
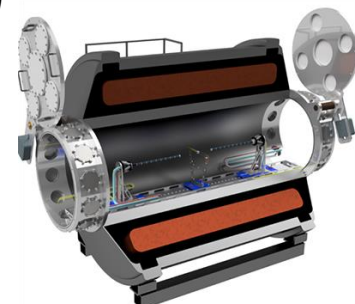
Cannot cover all – restrict to few examples of FRIB specific opportunities

Detectors at FRIB

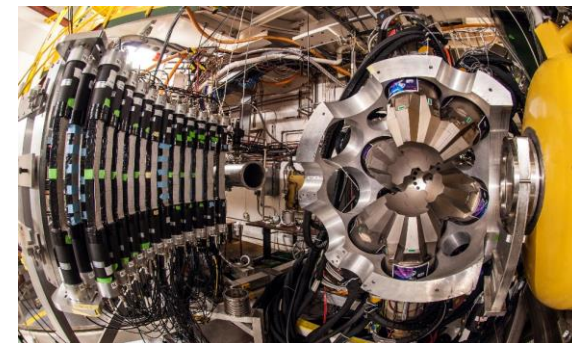
Si+Solenoid arrays (*SOLARIS, HELIOS, ISIS*)



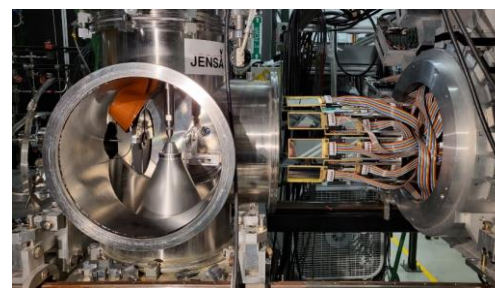
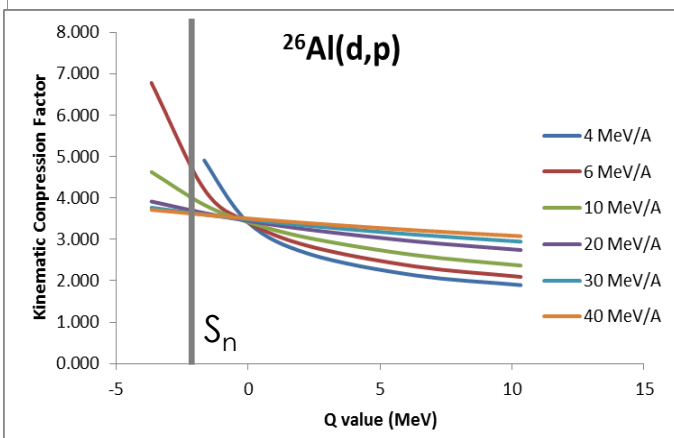
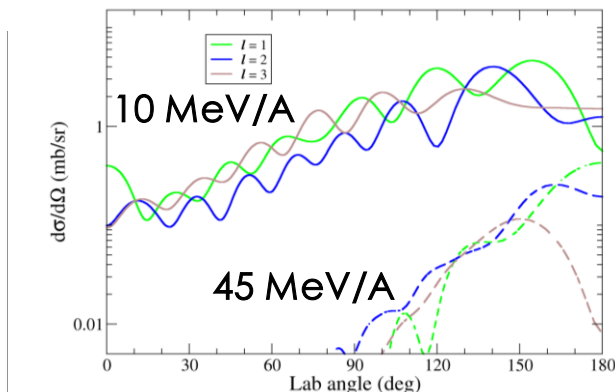
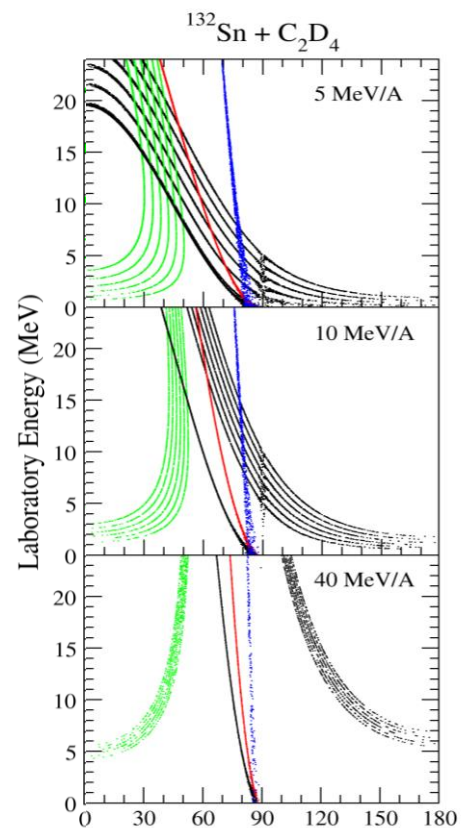
Charged-particle arrays (*HiRA, ORRUBA, ...*)



Active targets (*ATTPC*)

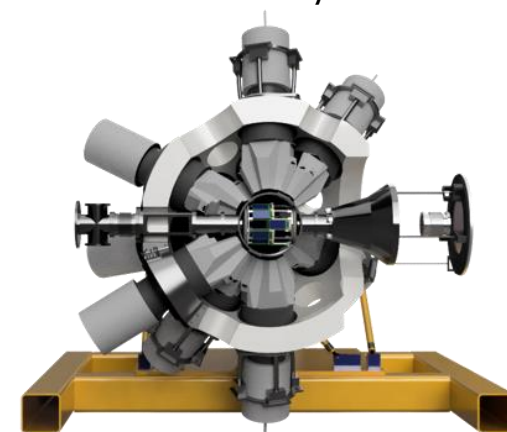


n arrays (*VANDLE, LENDA, NEXT, ODeSA, ...*)



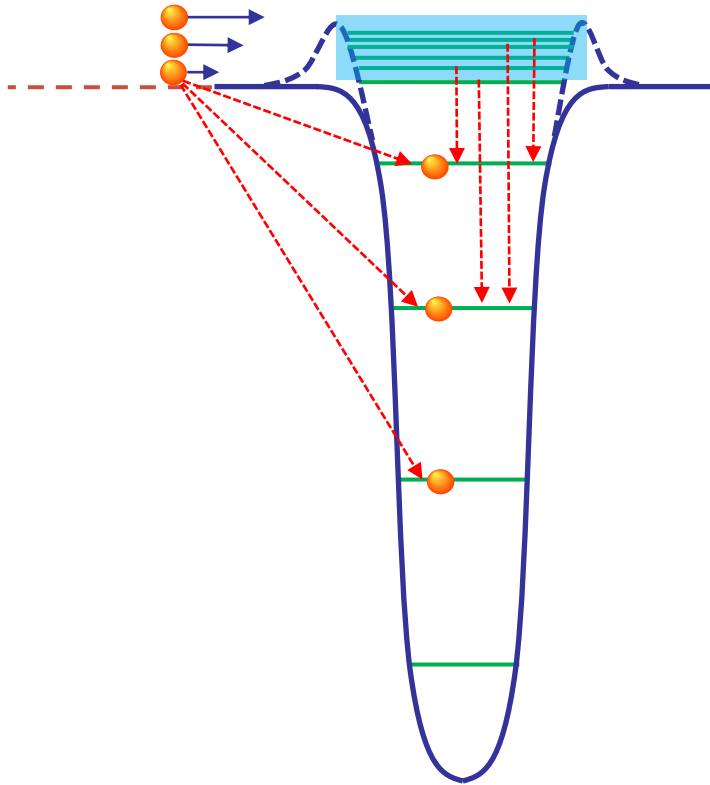
Gas jet targets (*JENSA*)

Devices often coupled to recoil separators (*S800, SECAR, ISLA*)



Ge arrays (*GRET(IN)A, SeGA, Clovers, ...*)

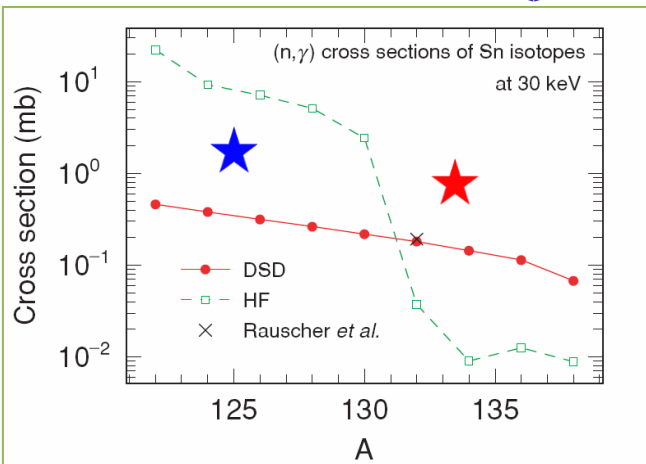
Constraining neutron-capture cross sections



- Neutron capture can occur via resonances (eg compound nucleus formation), and direct capture to bound states
- Depending on neutron level density/strong resonances, one or other may be dominant
- In general, need methods to constrain *both* mechanisms

Neutron transfer reactions

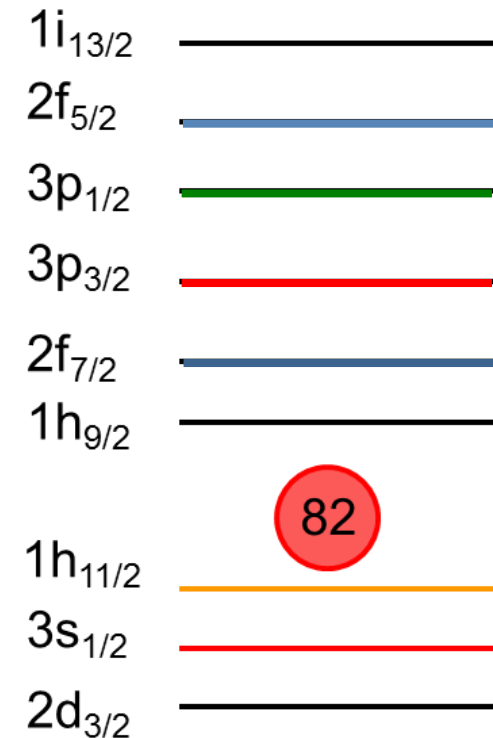
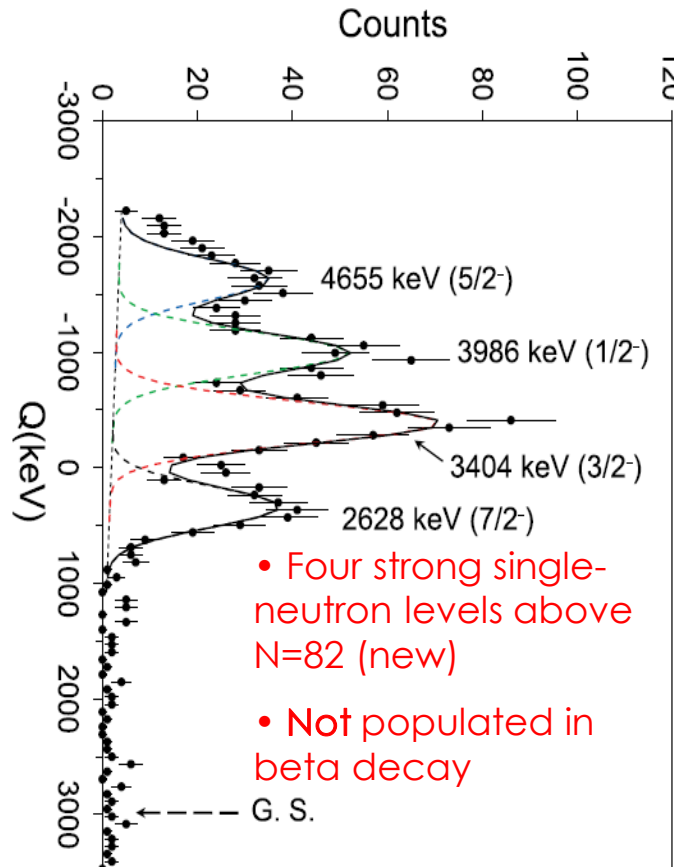
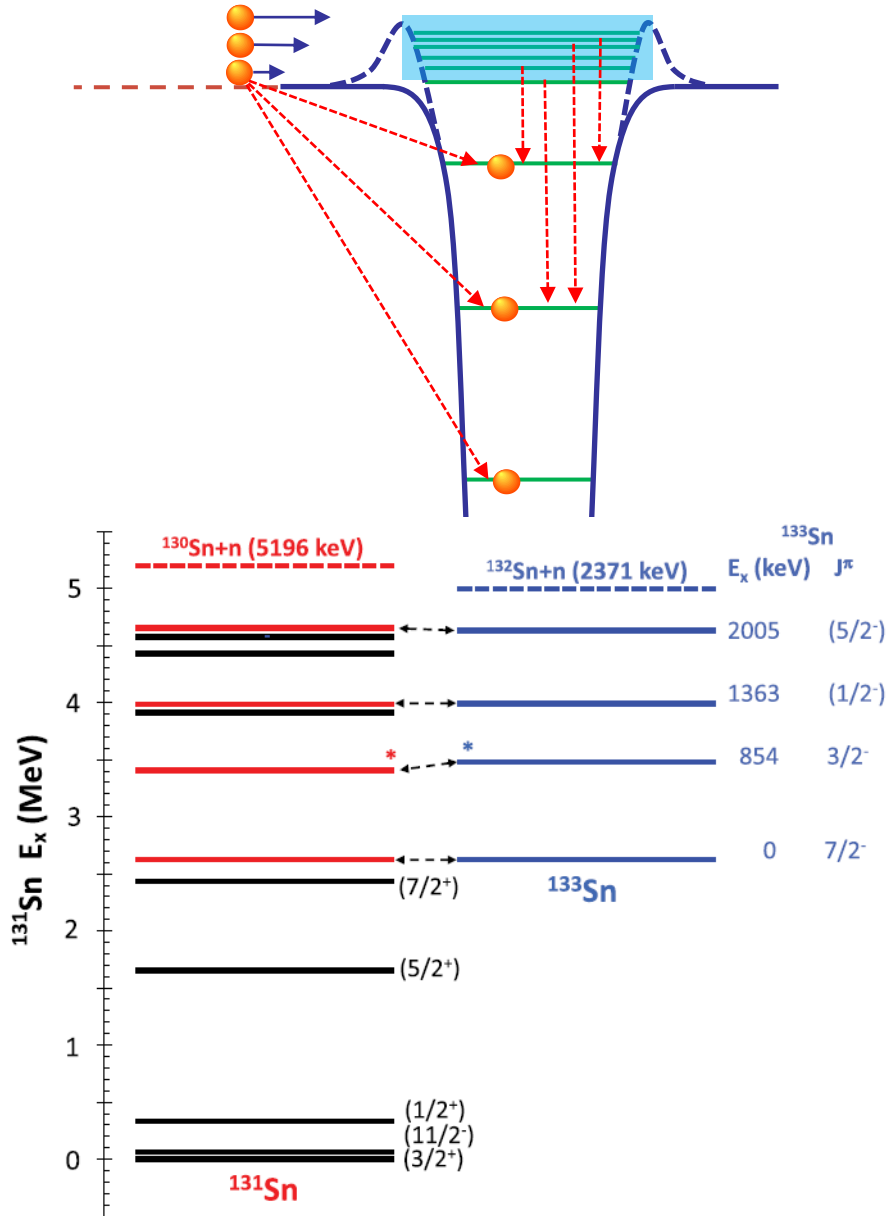
- Selective (states with target+n wavefunctions)
- Give properties of bound states and isolated resonances (E, J^π, C^2S)
 - for DSD
 - Constrain structure models
- Can be used as surrogate for CN capture (SRM)



Constraining neutron-capture cross sections

- Neutron capture can occur via resonances (eg compound nucleus formation), and direct capture to bound states
- Depending on neutron level density, one or other may be dominant
- Ideally need methods to constrain *both* mechanisms

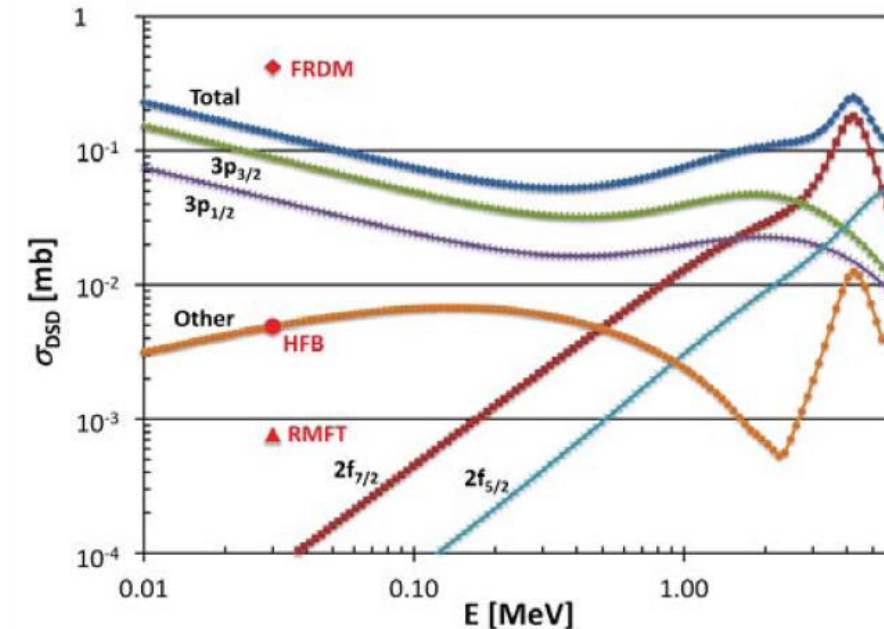
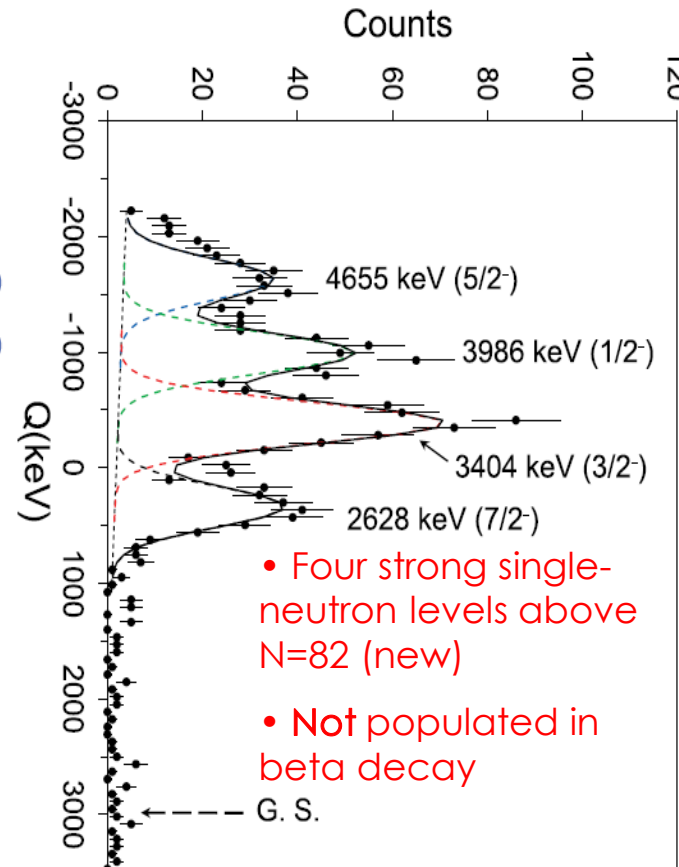
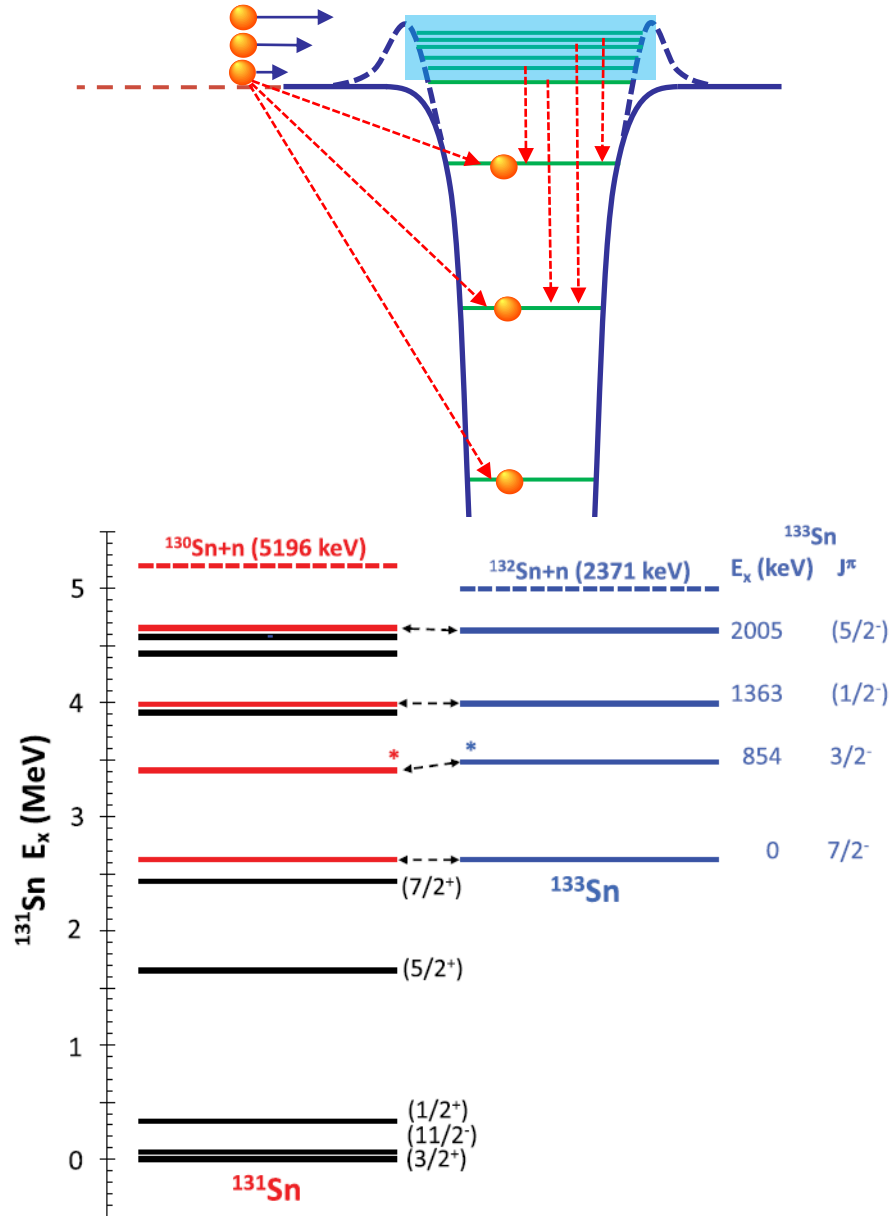
R.L. Kozub *et al*, PRL 109 172501 (2012)



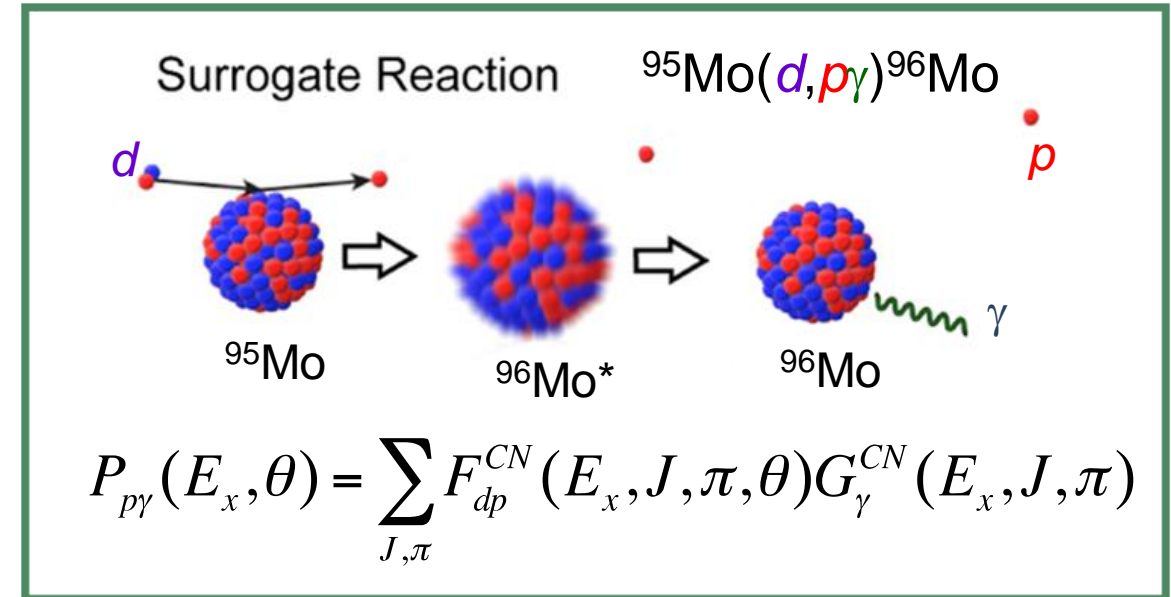
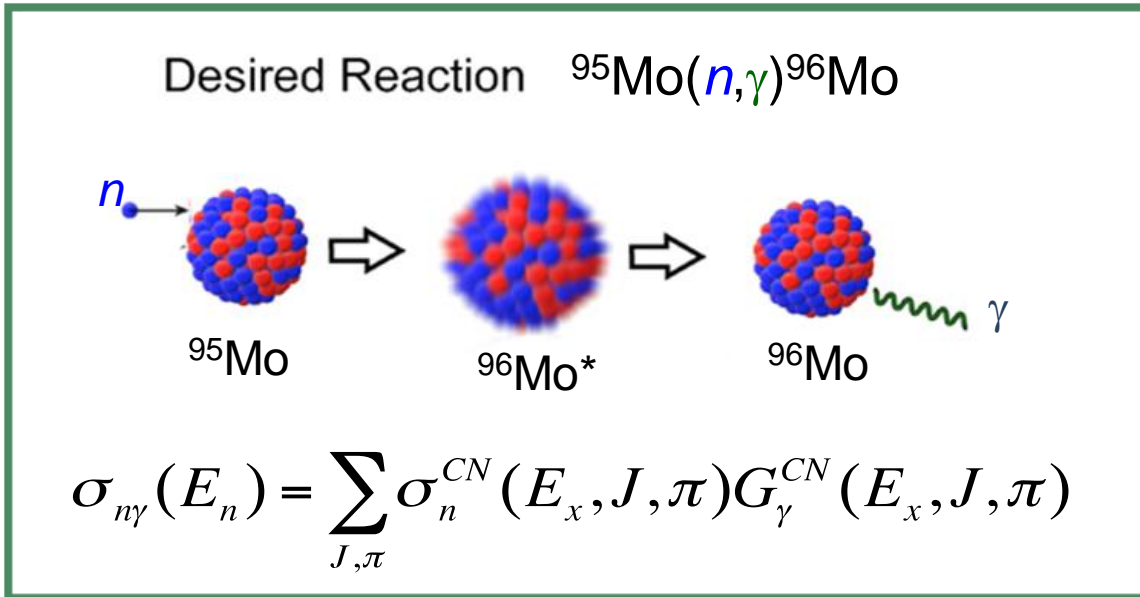
Constraining n-capture cross sections - DSD

- Neutron capture can occur via resonances (eg compound nucleus formation), and direct capture to bound states
- Depending on neutron level density, one or other may be dominant
- Ideally need methods to constrain *both* mechanisms

R.L. Kozub *et al*, PRL 109 172501 (2012)



Constraining CN n-capture cross sections - SRM



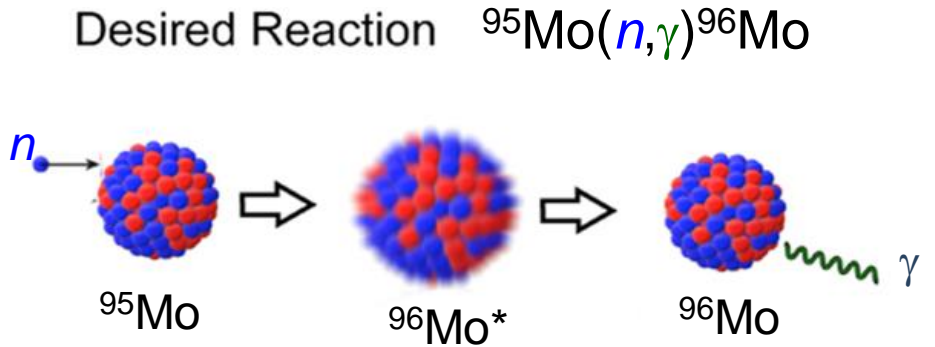
- Model reaction in HF formalism
- Essential theory components:
 - Formation of CN (σ^{CM}) – simple
 - Decay of CN (G^{CM}) – complicated (Escher)
 - *Need to place experimental constraints on G^{CN}*

A surrogate reaction forms the “same”* compound nucleus as the desired reaction

- Model experimentally-determined $P_{p\gamma}(E_{ex})$ in HF formalism to constrain G^{CN}
- Essential theory components:
 - Decay of CN (G^{CM}) – complicated (Escher)
 - *Entry spin distribution (F^{CM}) – complicated (Potel)

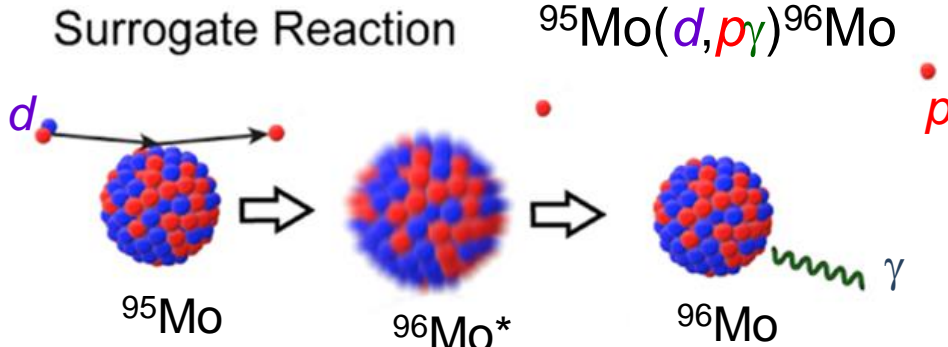
Constraining CN n-capture cross sections - SRM

Desired Reaction $^{95}\text{Mo}(n,\gamma)^{96}\text{Mo}$



$$\sigma_{n\gamma}(E_n) = \sum_{J,\pi} \sigma_n^{CN}(E_x, J, \pi) G_\gamma^{CN}(E_x, J, \pi)$$

Surrogate Reaction $^{95}\text{Mo}(d,p\gamma)^{96}\text{Mo}$



$$P_{p\gamma}(E_x, \theta) = \sum_{J,\pi} F_{dp}^{CN}(E_x, J, \pi, \theta) G_\gamma^{CN}(E_x, J, \pi)$$

Core experimental technique

- Measure outgoing particles, using kinematics to determine entrance E_x above S_n
- Measure γ rays to determine $P_{p\gamma}$
- Typically requires either a collecting transition, or an understanding of the γ decay scheme

- Model reaction in HF
- Essential theory components:
 - Formation of CN (σ^{CM})
 - Decay of CN (G^{CM}) - **complicated** (Escher)
 - *Need to place experimental constraints on G^{CN}*

forms the "same"* as the desired reaction

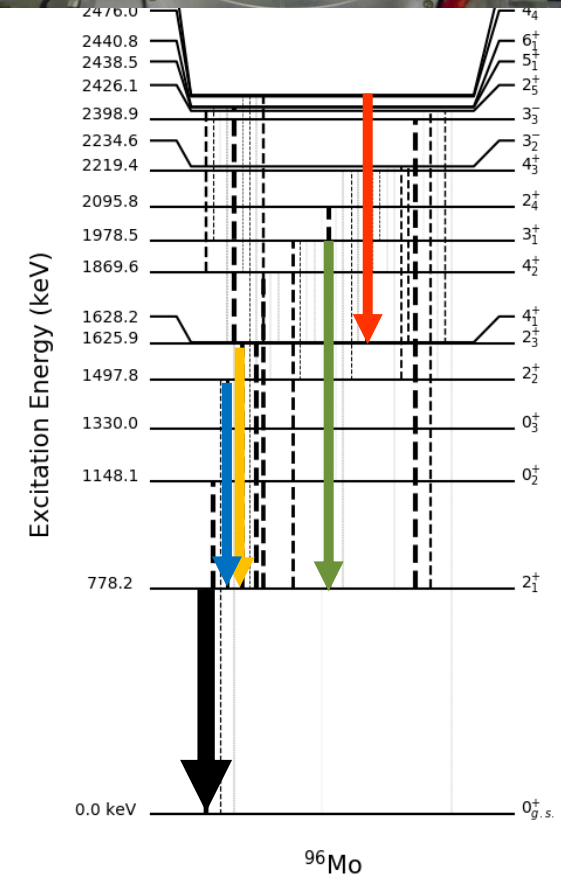
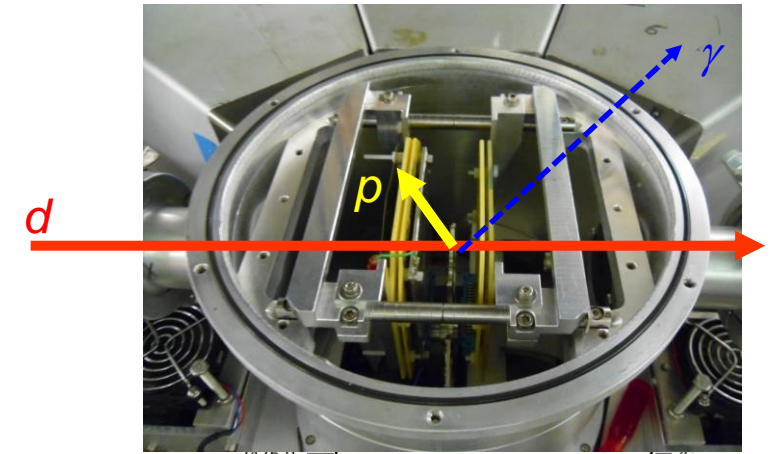
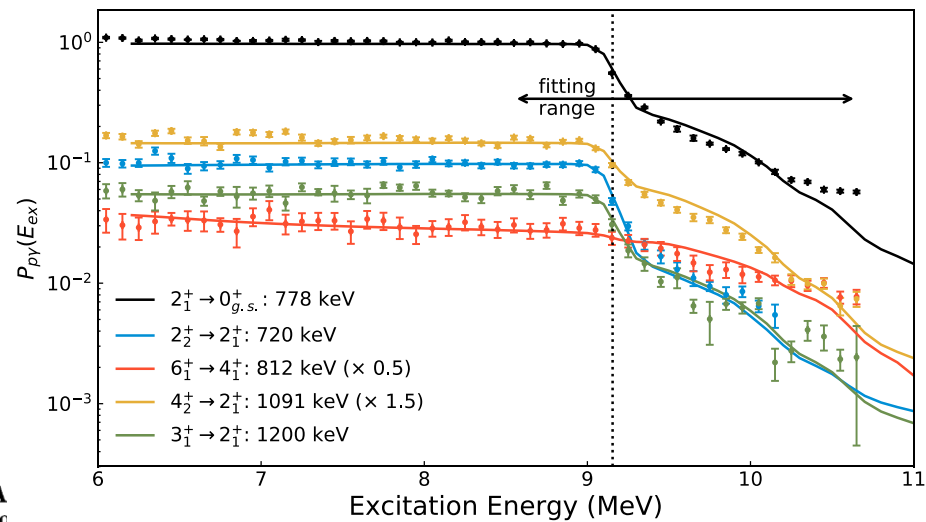
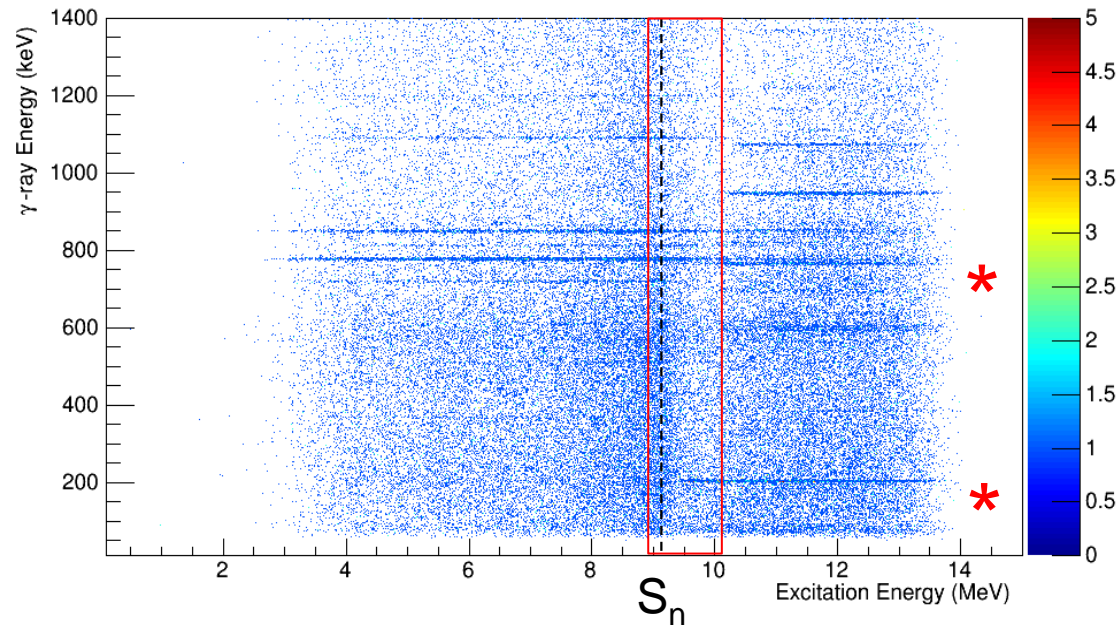
experimentally-determined formalism to constrain G^{CN}

components:

- **complicated** (Escher)
- F^{CM} - **complicated**

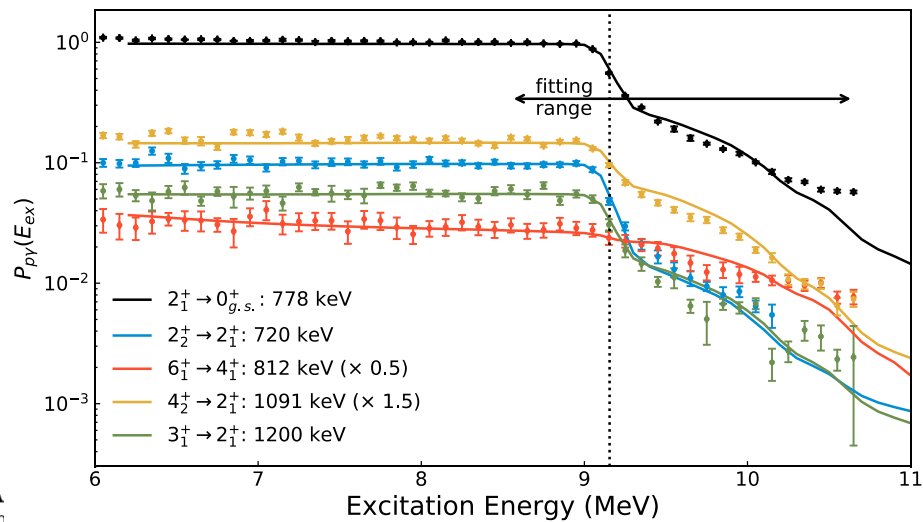
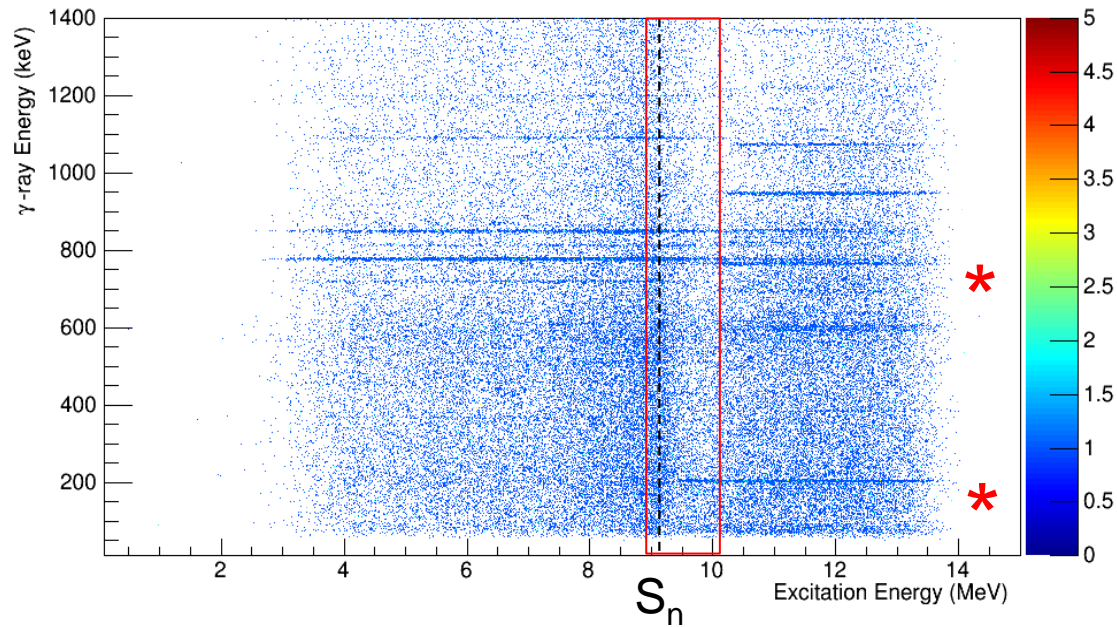
(d,p) as surrogate for (n, γ)

Experimental signature

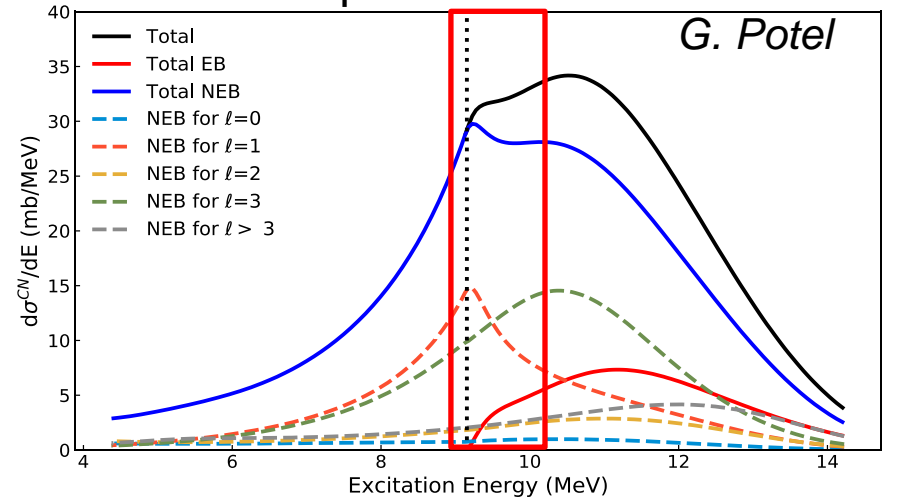


(d,p) as surrogate for (n,γ)

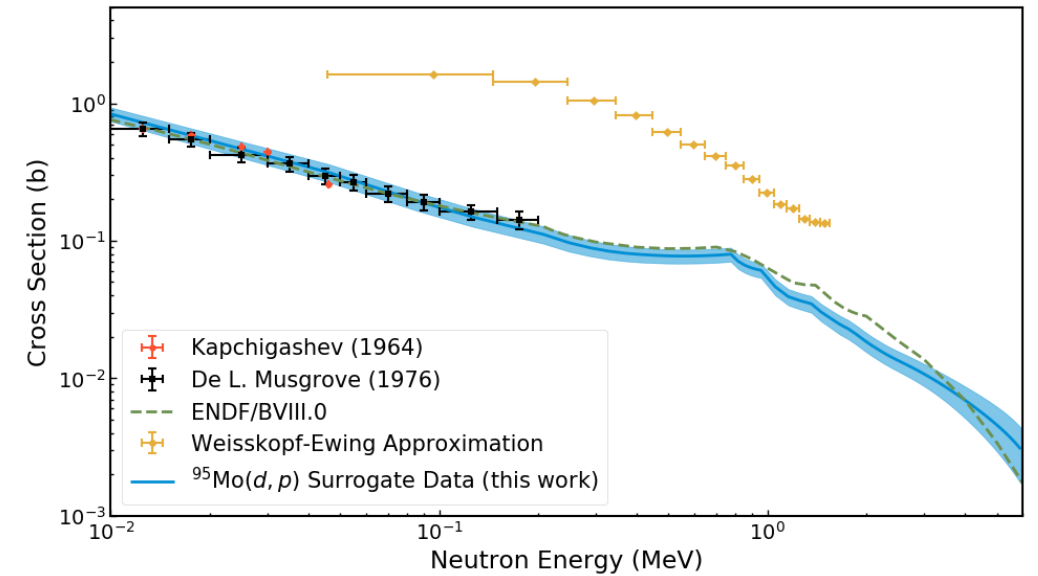
Experimental signature



Spin distributions



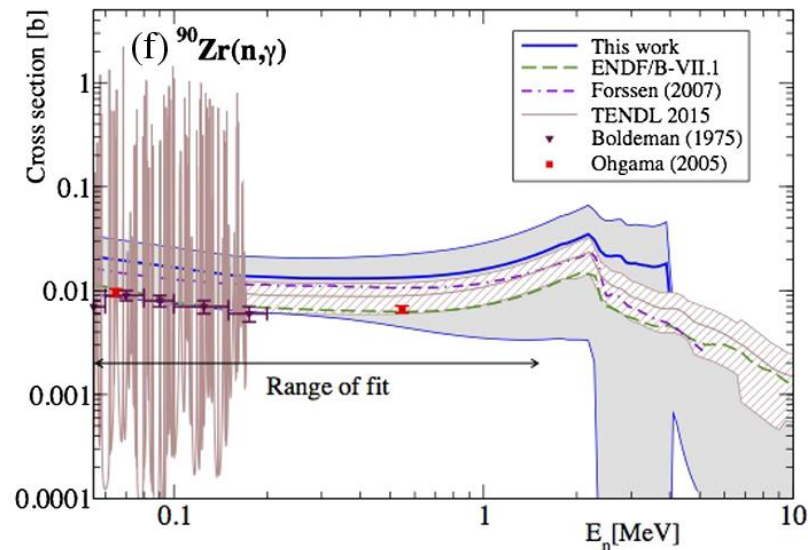
$$P_{p\gamma}(E_x, \theta) = \sum_{J, \pi} F_{dp}^{CN}(E_x, J, \pi, \theta) G_{\gamma}^{CN}(E_x, J, \pi)$$



SRM outlook...

- SRM Progress
 - Validation of $(d,p\gamma)$ as surrogate for (n, γ)
 - understanding J^π formation distributions key ingredient
 - Development of (p,d) as (n, γ) surrogate

J.E. Escher *et al.*, PRL 121 052501 (2018)



- Ongoing development of (p,p') as (n, γ) surrogate
- What are the limits of the statistical approach...
- More from Jutta next week...

Expt. challenges moving to RIB experiments

- Resolution (target thickness, kinematic compression) (~ 100 keV \rightarrow 500-1000 keV)
- Contaminants (eg carbon in target – however, only need to address this ‘once’ – not a surprise every time)
- Luminosity (beam intensity) – statistics-limited measurements
- Limitation on nuclides that can be practically studied
 - Nuclides without a reasonably-collecting transitions are very challenging - complex γ decay schemes disperses strength over numerous γ transitions
 - Isomers (moving with beam) lead to unobserved gamma emissions

An alternative technique – uniquely suited to FRIB...

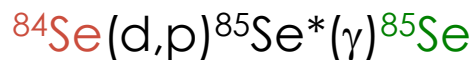
A new technique with RIBs

Developed in NSCL
 $^{84}\text{Se}(d,p)^{85}\text{Se}$ experiment

...detect the recoiling nucleus to determine if decayed by n or γ

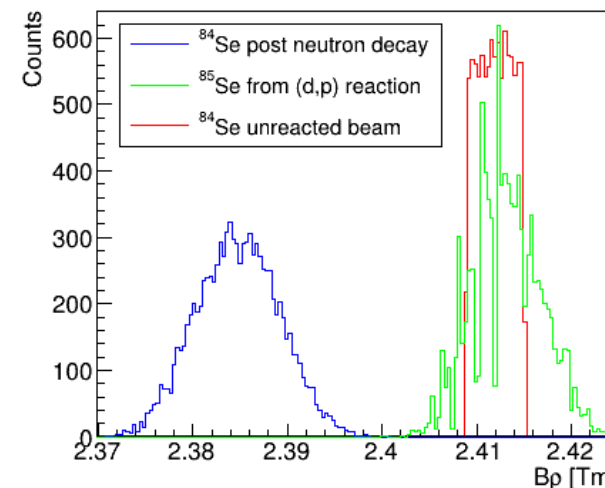
Use charged-particle [e.g (d,p)] to determine the formation E_x (as before)

To bound states



To unbound states

- $^{84}\text{Se}(d,p)^{85}\text{Se}^*(\gamma)^{85}\text{Se}$
- $^{84}\text{Se}(d,p)^{85}\text{Se}^*(n)^{84}\text{Se}$



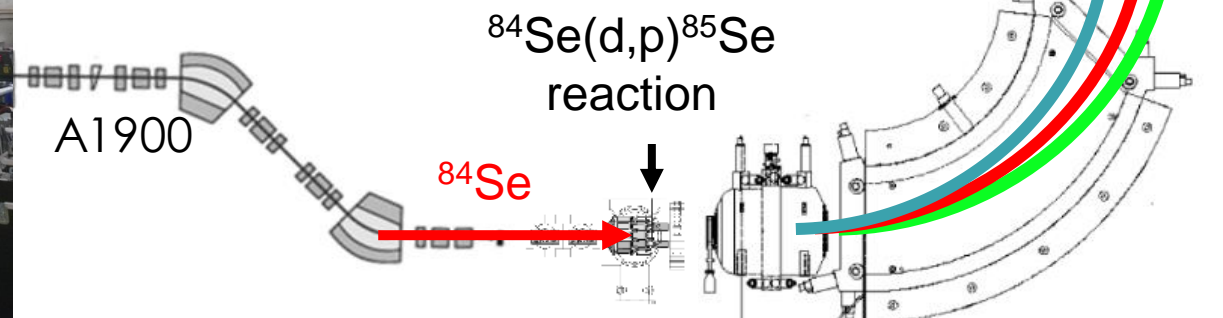
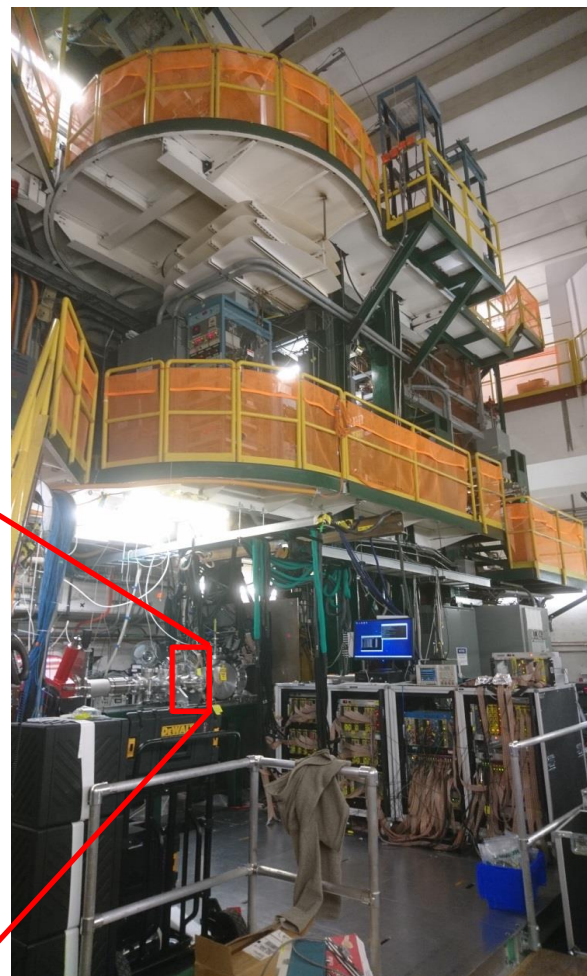
H. Sims, S.D.Pain, J.A. Cizewski, A. Ratkiewicz, et al.,



Focal plane position

Three responses in the FP

1. ^{84}Se unreacted beam
2. ^{85}Se recoils from (d,p)
3. ^{84}Se after n emission from ^{85}Se recoil



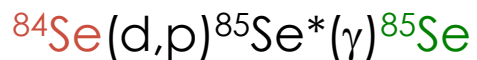
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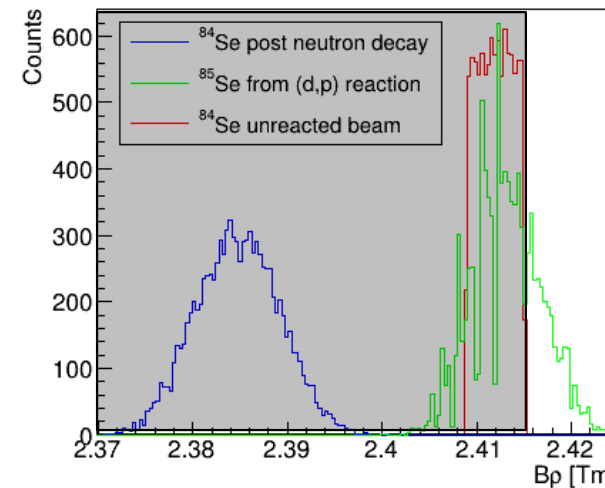
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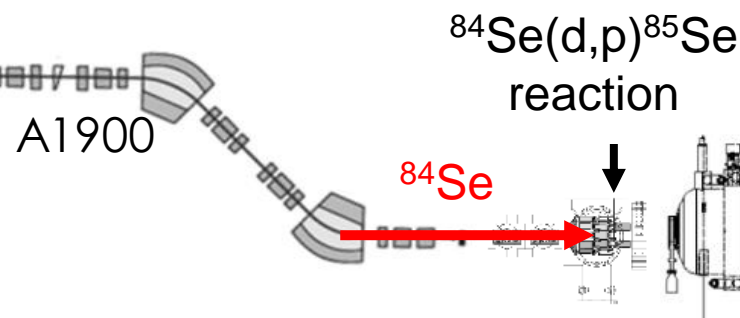
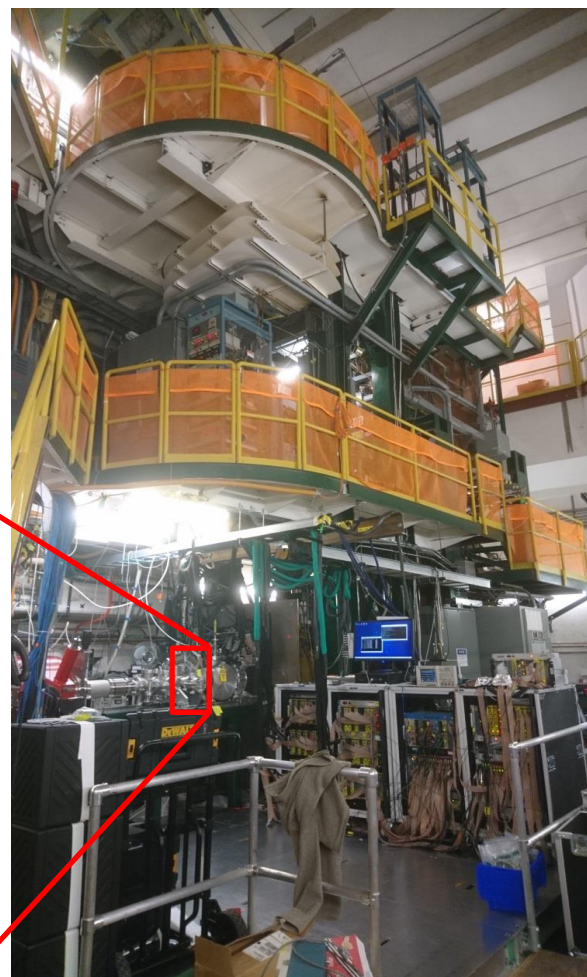
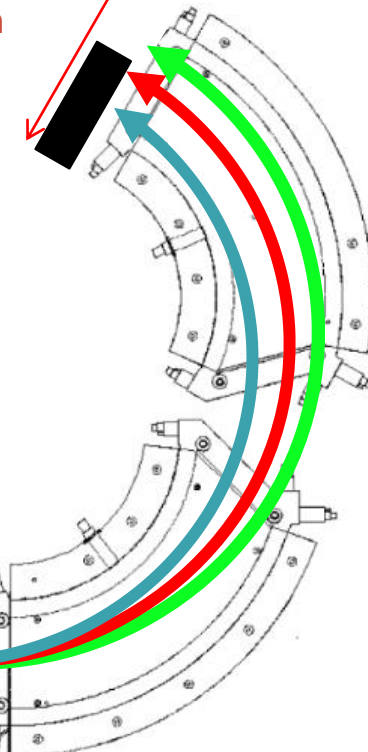
H. Sims, S.D.Pain, J.A. Cizewski, A. Ratkiewicz, et al.,



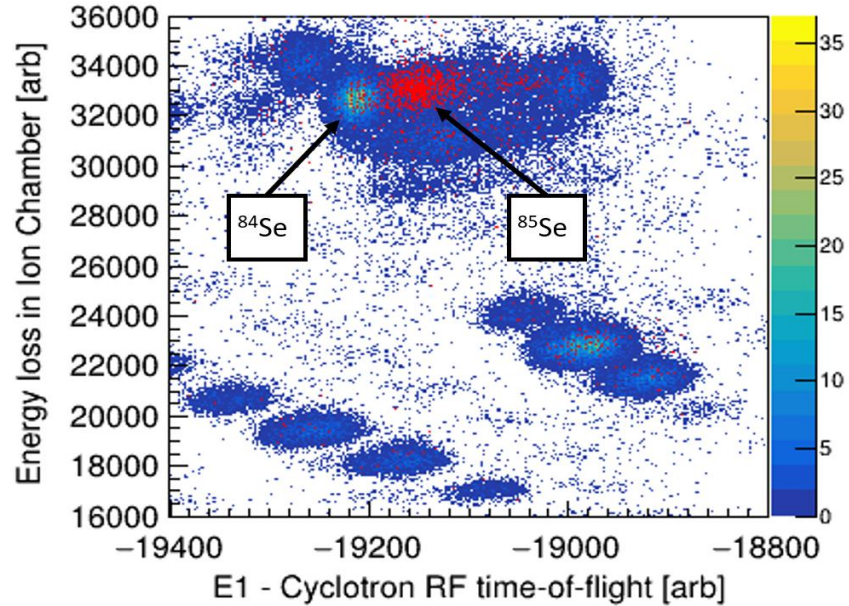
Focal plane position

Three responses in the FP

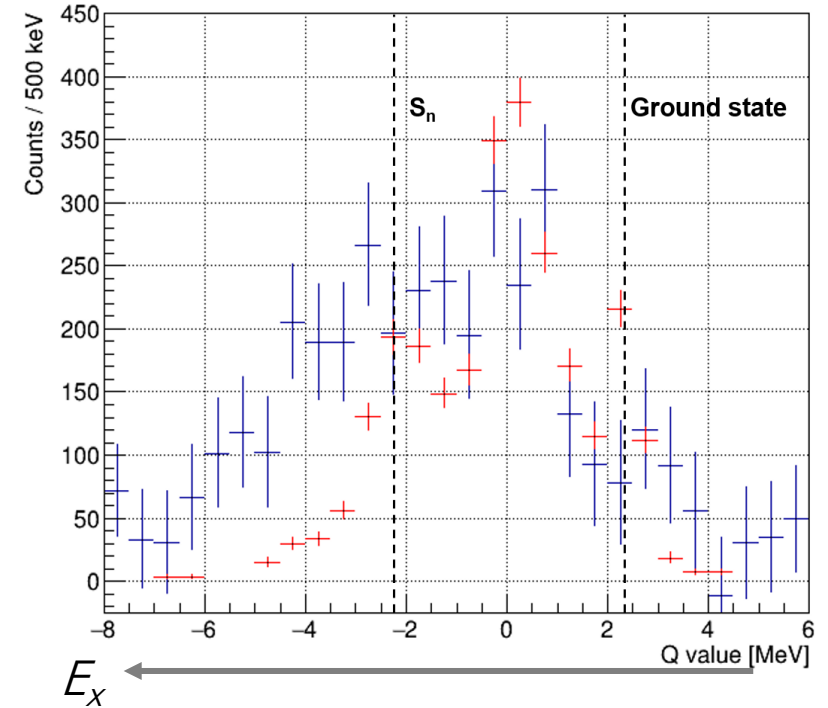
1. ^{84}Se unreacted beam
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An alternative with RIBs...



H. Sims,
J.A. Cizewski,
S.D.Pain,
A. Ratkiewicz,
et al.

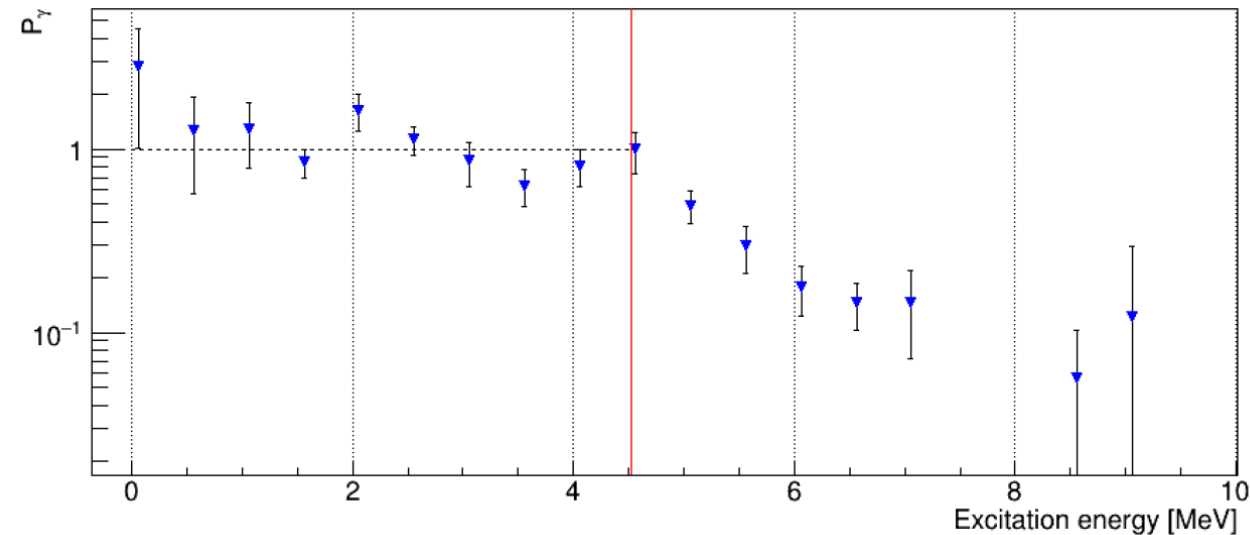


Advantages

- concentrates all statistics in a single observable
- high (25-50%), simple and experimentally-determinable detection efficiency (cf γ cascades)
- Enables measurements on (almost) any nucleus on same footing

Challenges

- need careful characterization of BG reactions on C in target



Work ongoing with Jutta to extract (n,γ) cross section

Unique opportunity at FRIB

Combination

- FRIB n-rich beams
- S800
- GODDESS [ORRUBA+GRET(IN)A]

Two approved experiments

- ^{80}Ge (Sims, Grinder, Cizewski, Pain, et al)
– *weak r process*
- ^{75}Ga (Pain, Balakrishnan, et al)
– *i-process*

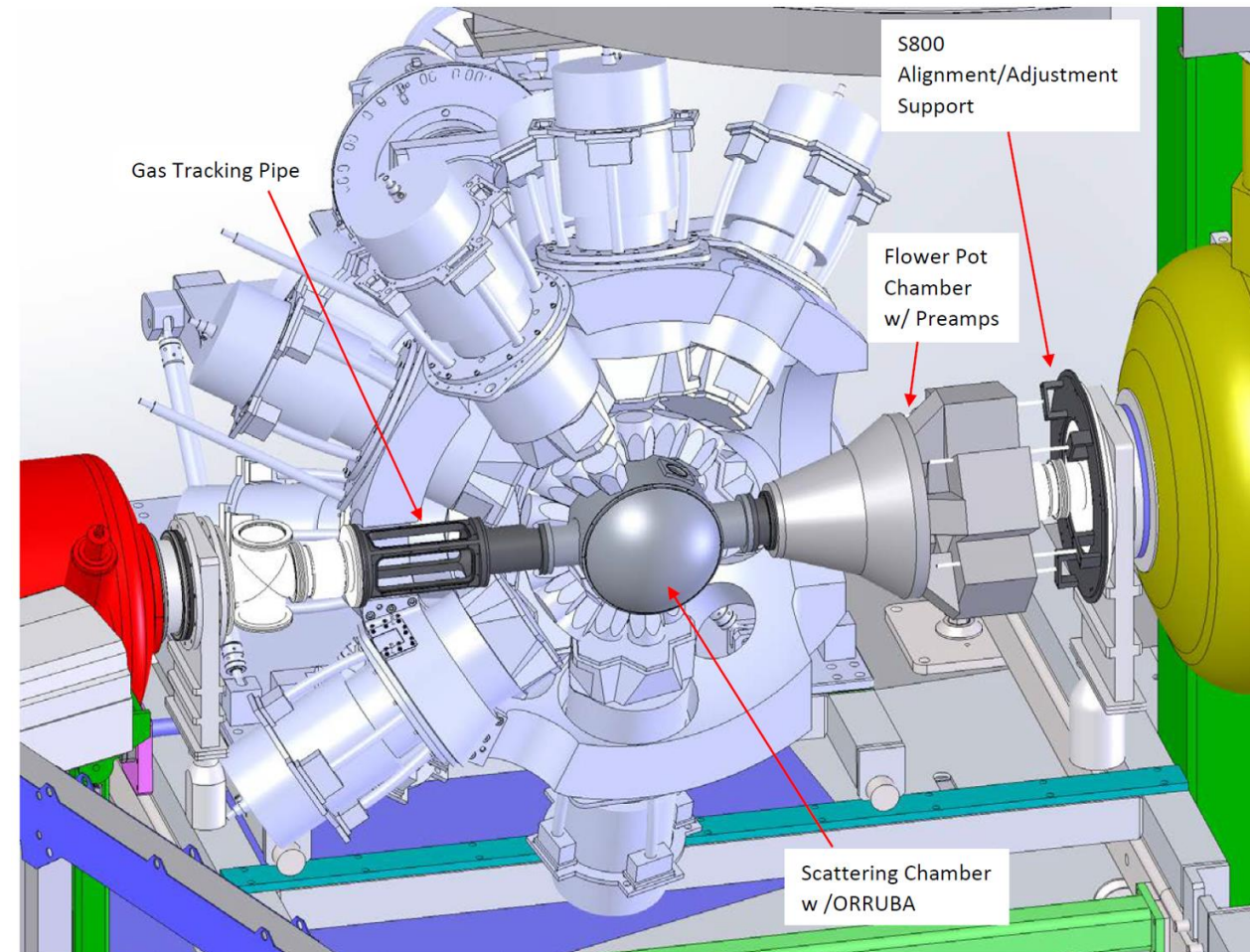
Cannot measure all; target specific interesting cases

Ideally like to have (empirical) predictive model of (n,γ) cross sections

- Model constrained by experiment in sensitive cases?

Detect protons, gammas and recoils

- Discrete particle- γ spectroscopy
- SRM with recoils
- SRM with γ



Transfer on sd nuclei

- Testing ground of LBSM calculations

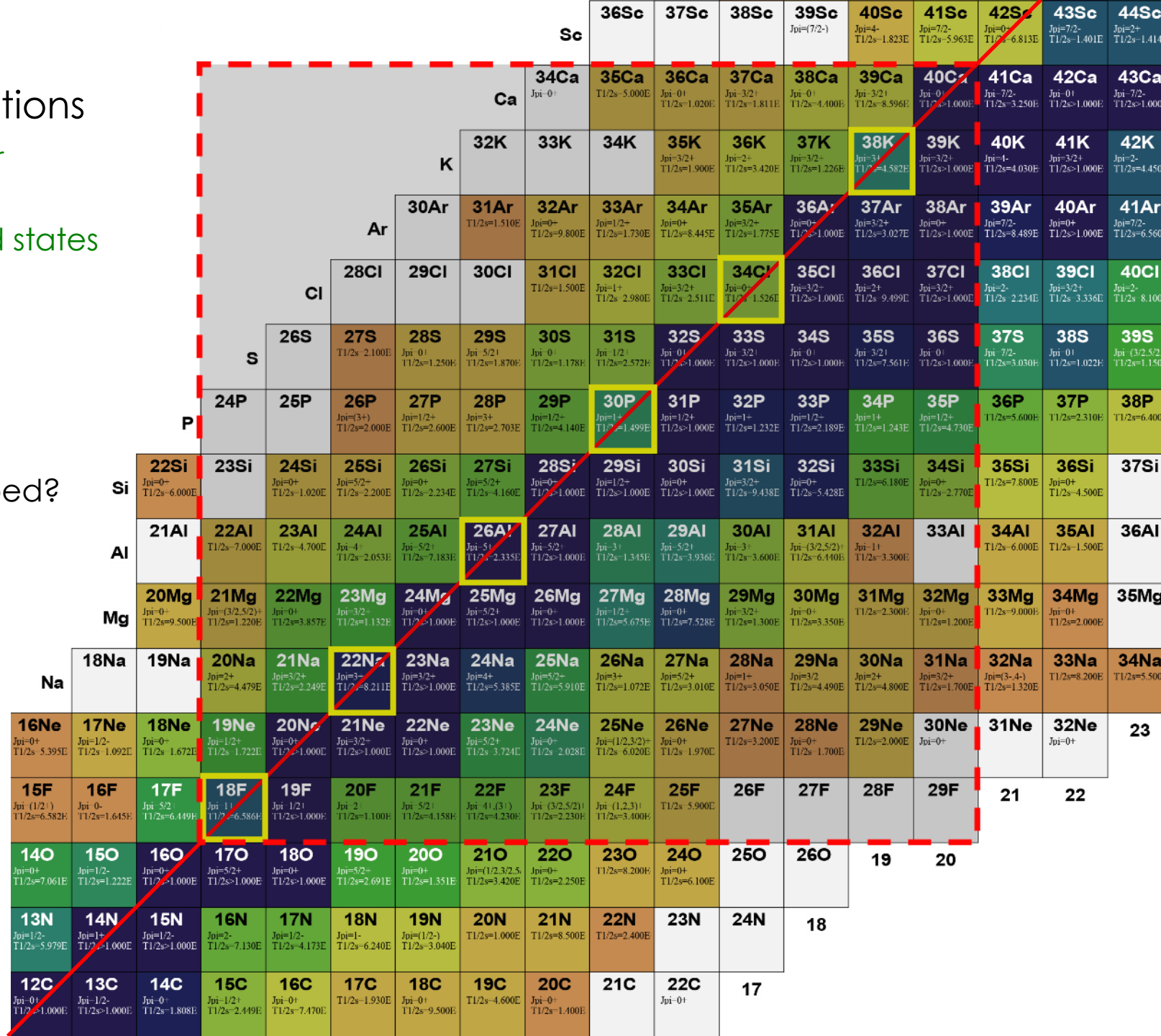
- Wealth of experimental data (near stability)
- Well-constrained interactions for sd states (eg USDb)
- Mid shell
 - highly mixed states
 - non-zero J^π ground states
 - non-spherical systems
- How well are fp excitations described?

- Reaction models

- Lower-end of well-constrained nucleon-nucleus global potentials (near stability)
- ADWA vs DWBA?
- Finite range effects?
- ...

- Beautiful experiments

- Astrophysical motivation $N = Z$



Odd-odd N=Z sd-shell nuclides

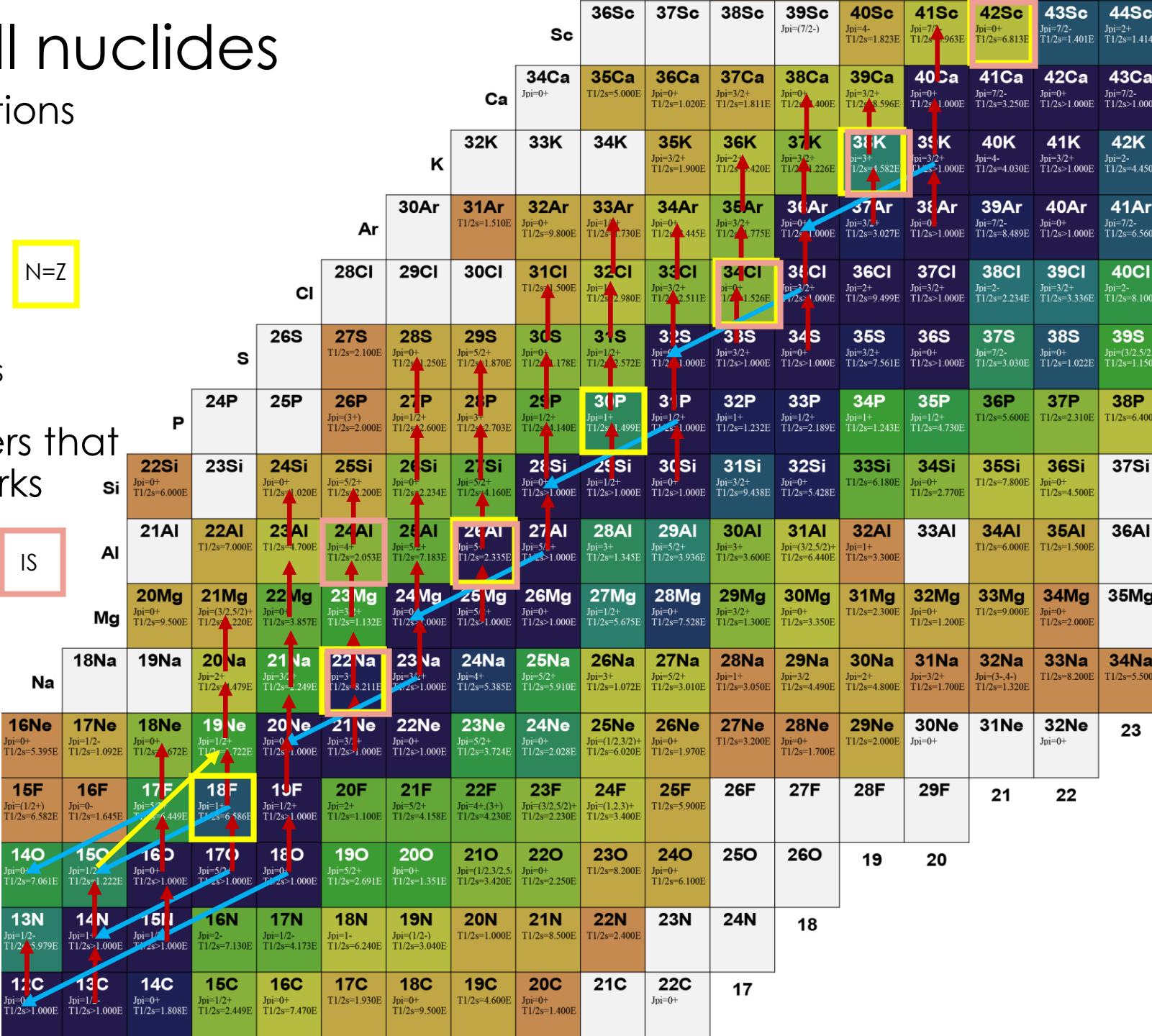
- Networks of (p, γ) and (p, α) reactions (beta decays omitted) in novae

- (p, γ) on odd-odd N=Z nuclides particularly important

- bottleneck reactions
- impact on astronomical observables

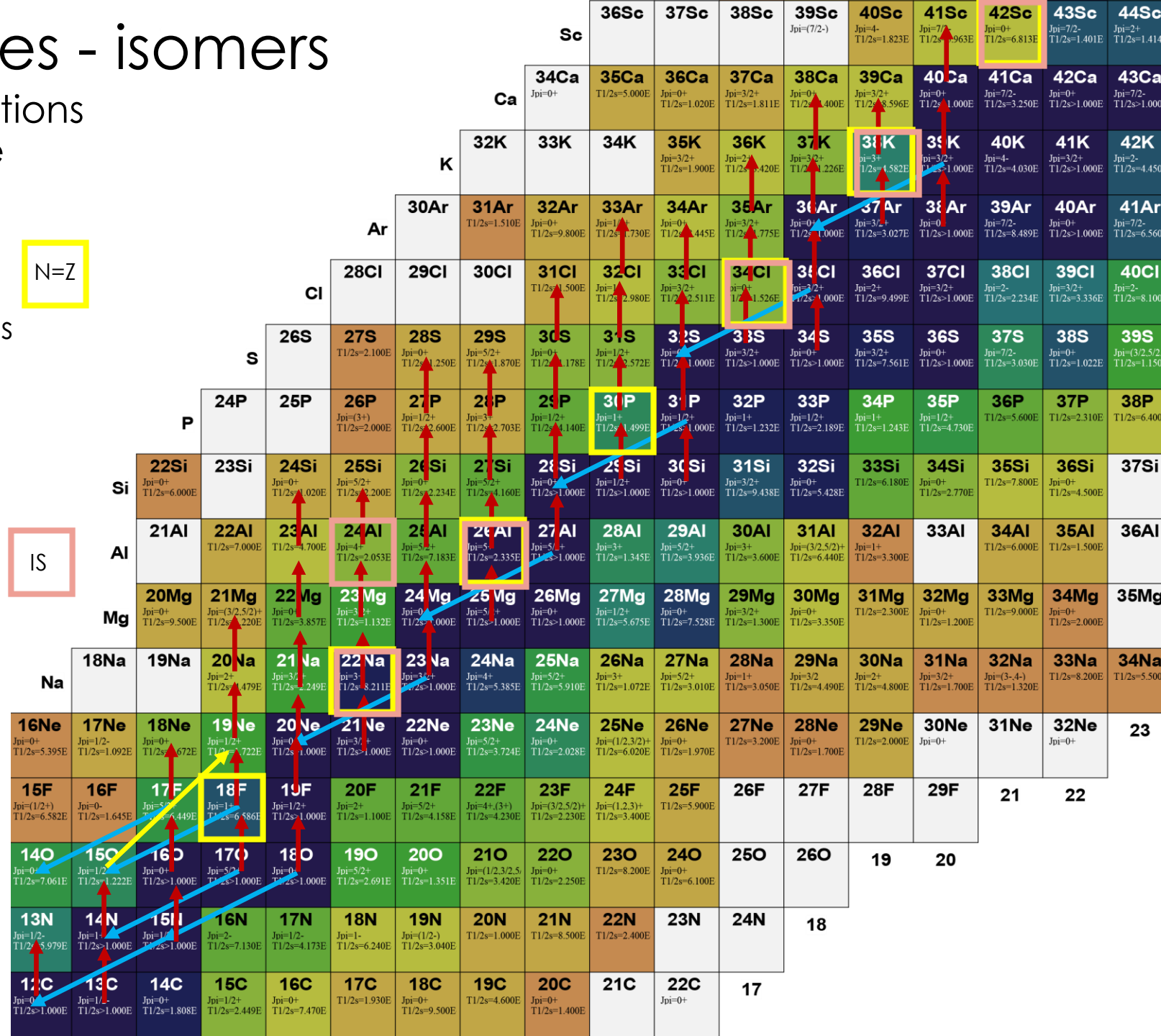
- Many have long-lived spin isomers that can play roles in reaction networks (astromers)

Species	t(Gs)	t(Is)	J π (Gs)	J π (Is)
- ²² Na	2.6 y	240 ns	3 ⁺	1 ⁺
- ²⁴ Al	2 s	130 ms	4 ⁺	1 ⁺
- ²⁶ Al	0.7 My	6.3 s	5 ⁺	0 ⁺
- ³⁰ P	2.5 m	96 fs	1 ⁺	0 ⁺
- ³⁴ Cl	1.5 s	32 m	0 ⁺	3 ⁺
- ³⁸ K	6.7 m	0.9 s	3 ⁺	0 ⁺
- ⁴² Sc	0.7 s	1 m	0 ⁺	7 ⁺



Odd-odd $N=Z$ nuclides - isomers

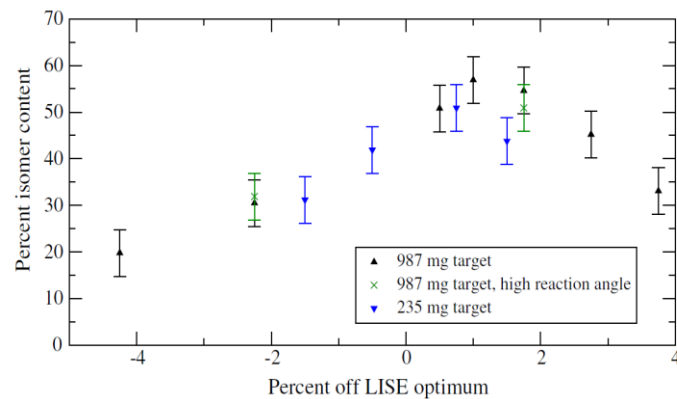
- Networks of (p,γ) and (p,α) reactions (beta decays omitted) in novae
- (p,γ) on odd-odd $N=Z$ nuclides
 - bottleneck reactions
 - impact on astronomical observables
- Reaction networks
 - independent
 - or thermal coupling at high T
- Want reaction rates on both GS and IS
 - v. different SP structure, limited expt
 - sd-pf states
- General rule
 - Insufficient beam intensities for direct (p,γ) measurements currently (some at FRIB)
 - indirect techniques within reach



Transfer reactions on isomeric beams at FRIB

- Unique design of FRIB gives opportunities for producing beams of long-lived ($>ms$) nuclear isomers at ideal beam energies/optics for transfer reactions - ReA
 - Produce GS and IS with fragmentation, reaccelerate
 - Control the ground:isomer composition via
 - selection of production yields, via fragment separator (spin, though not specifically that of final state)
 - Adjustment of hold-up times inherent to ReA (lifetimes)
- Transfer, charge-exchange, Coulex,... for structure/indirect astrophysics (ORRUBA, SOLARIS, GODDESS, GRETA, LENDA, SeGA, Clarion2, ...)
 - Direct measurements of astrophysical reactions [eg (p,g) with SECAR, or (α,p) (α,n) with JENSA, MUSIC, HabaNERO, ...]

Selection on production



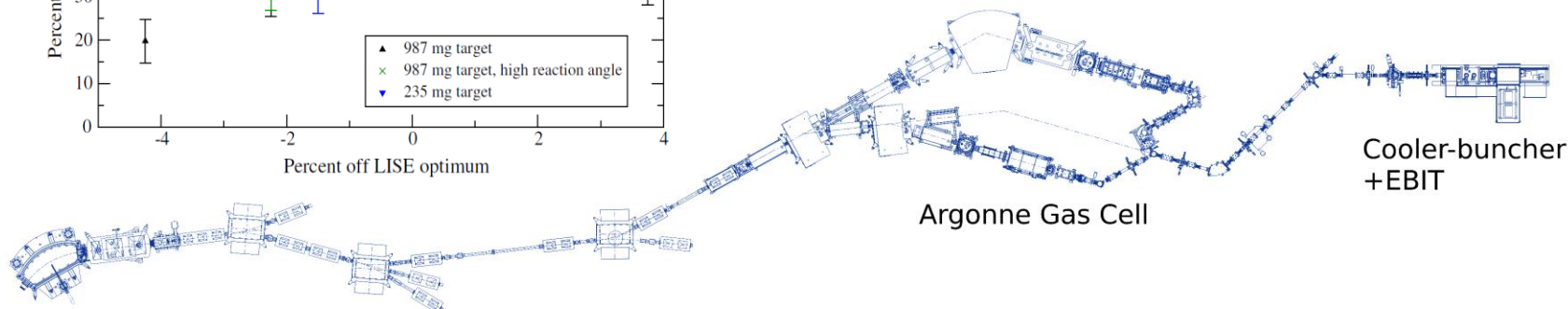
^{38}K

GS 3^+

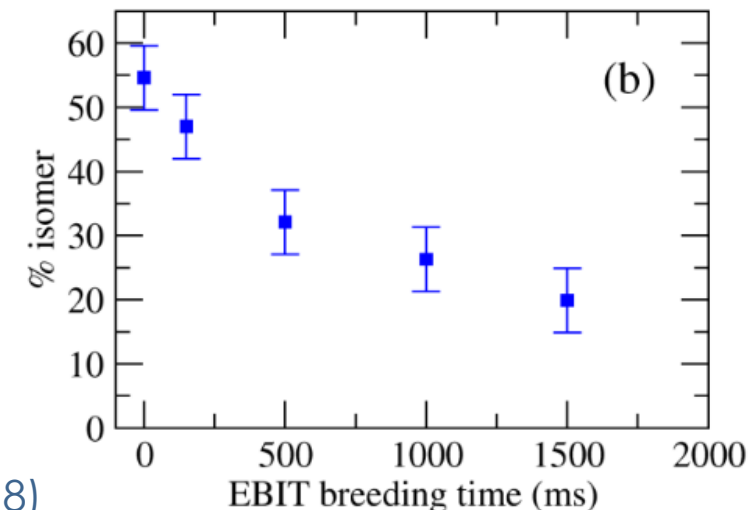
Isomer 0^+ (130 keV)

$t_{1/2} \sim 7.6$ min

$t_{1/2} \sim 1$ sec



Selection by charge-breeding

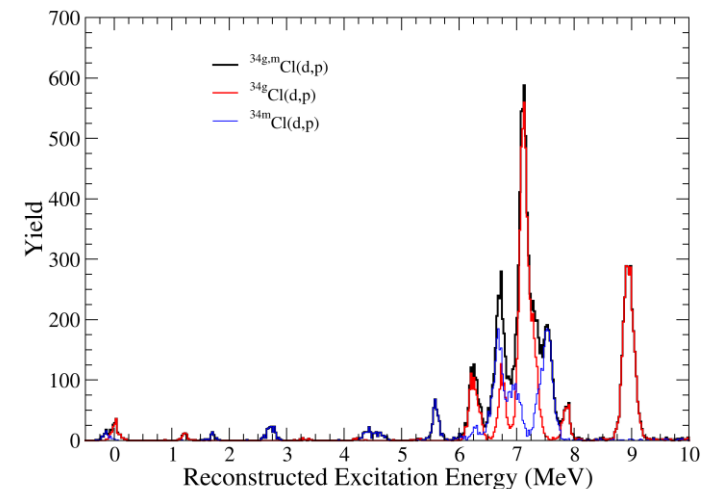
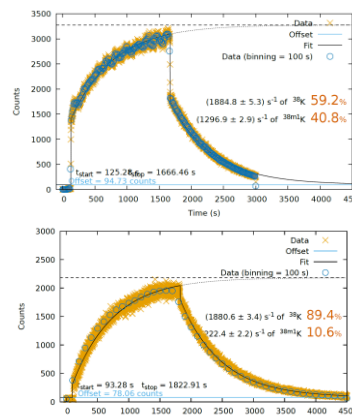
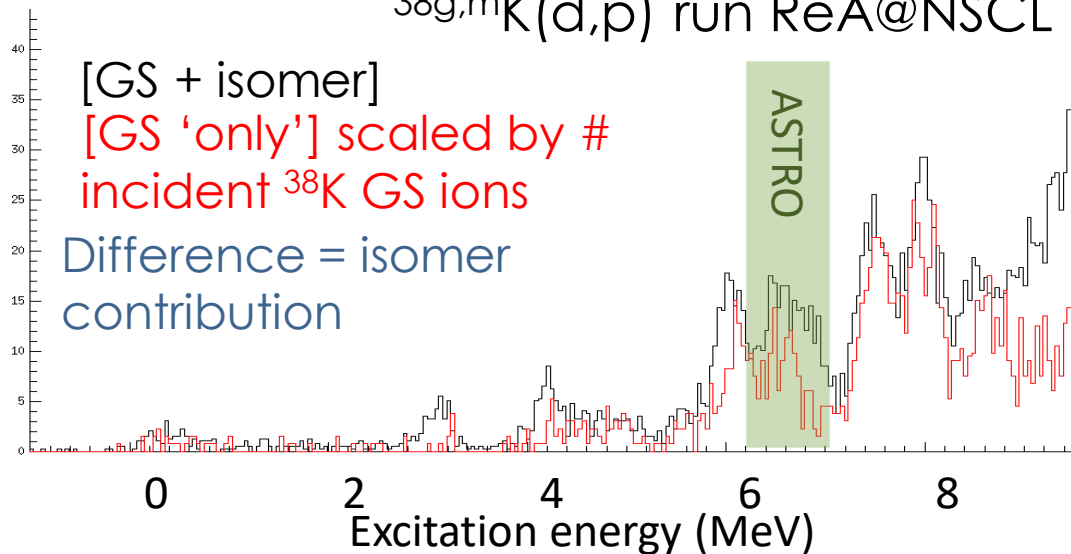


Previous and upcoming isomer expts

Nova nucleosynthesis

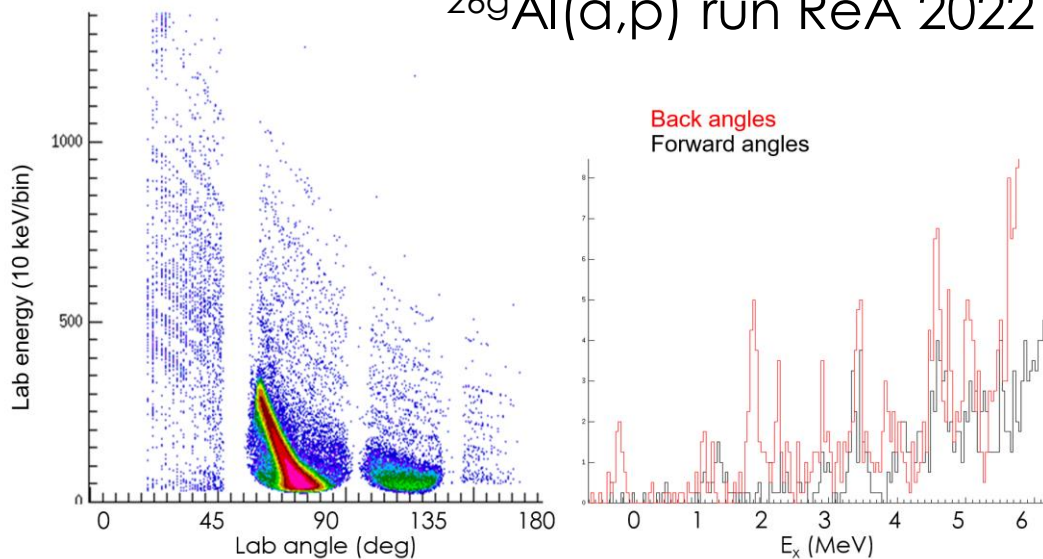
$^{34g,m}\text{Cl}(d,p)$ FRIB PAC1 approved

$^{38g,m}\text{K}(d,p)$ run ReA@NSCL 2020

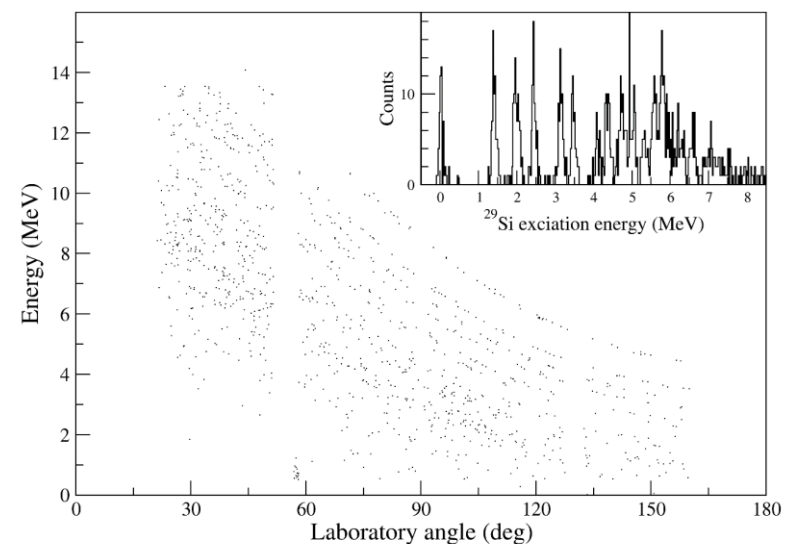


$^{26m}\text{Al}(a,p)$ FRIB PAC2 approved

$^{26g}\text{Al}(a,p)$ run ReA 2022



*Direct
measurements
for XRB and SN
nucleosynthesis*



Indirect constraints on (p,γ) reactions

- Dominated by isolated resonances (some too low for direct measurements)
- Locate states E_r
- To constrain **resonance strength**, determine:
 - Spins
 - l_p (constrains barrier, Γ_{sp})
 - Determine reduced width (10^2) $\Gamma_p = C^2 S \cdot \Gamma_{sp}$ ←

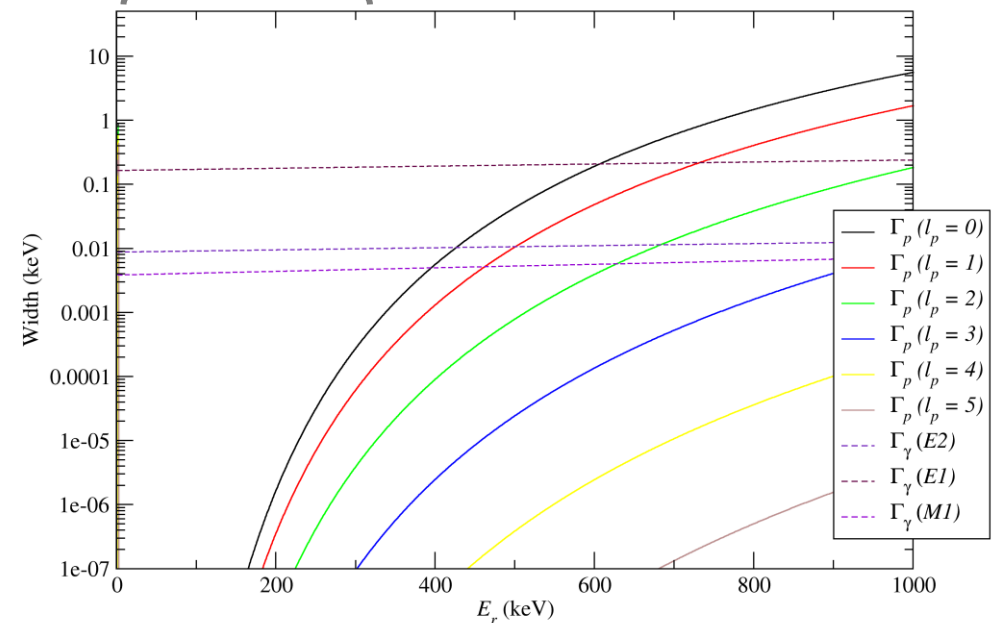
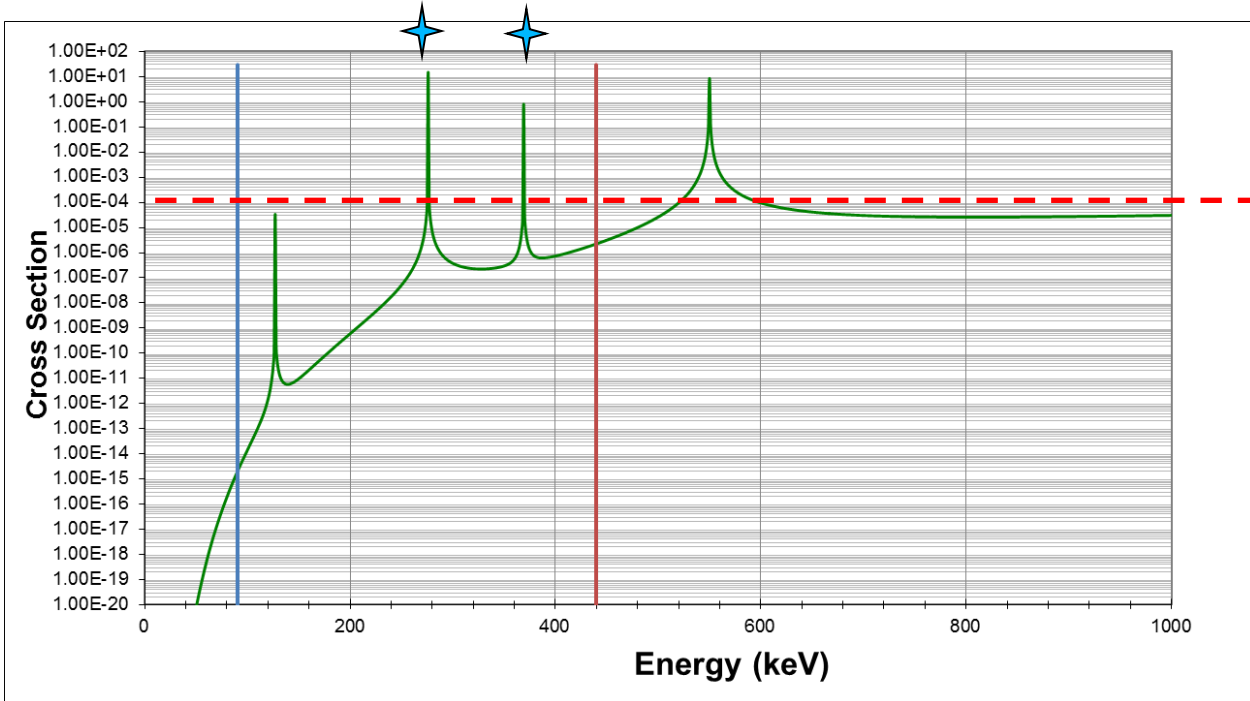
$$\langle \sigma v \rangle = \left(\frac{2\pi}{\mu kT} \right)^{3/2} \eta^2 \omega \gamma \exp\left(-\frac{E}{kT}\right)$$

$$\omega = \frac{2J+1}{(2J_1+1)(2J_2+1)} (1 + \delta_{l_2}) \quad \gamma = \frac{\Gamma_p \Gamma_\gamma}{\Gamma}$$

low-energy limit

$$\Gamma_p \ll \Gamma_\gamma$$

$$\omega \gamma \approx \omega \Gamma_p$$



What can we learn from transfer?

- Proton transfer ideal (d,n) or ($^3\text{He},d$)
 - Selectivity*
 - Energies 10s of keV*
 - l_p
 - C^2S

Experimental challenges

- Neutron detection
- Inclusive measurements
 - Gamma tagging
 - Non-spin-zero ground/isomeric states
- ^3He targets

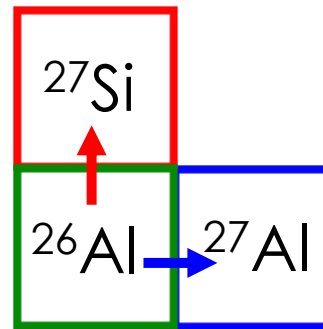
- Infer C^2S for *single-proton states* via *mirror symmetry*

- Guide by SMEC
- 10-20% effect

$$C^2S_p \approx C^2S_n$$

$$\Gamma_p = C^2S \cdot \Gamma_{sp}$$

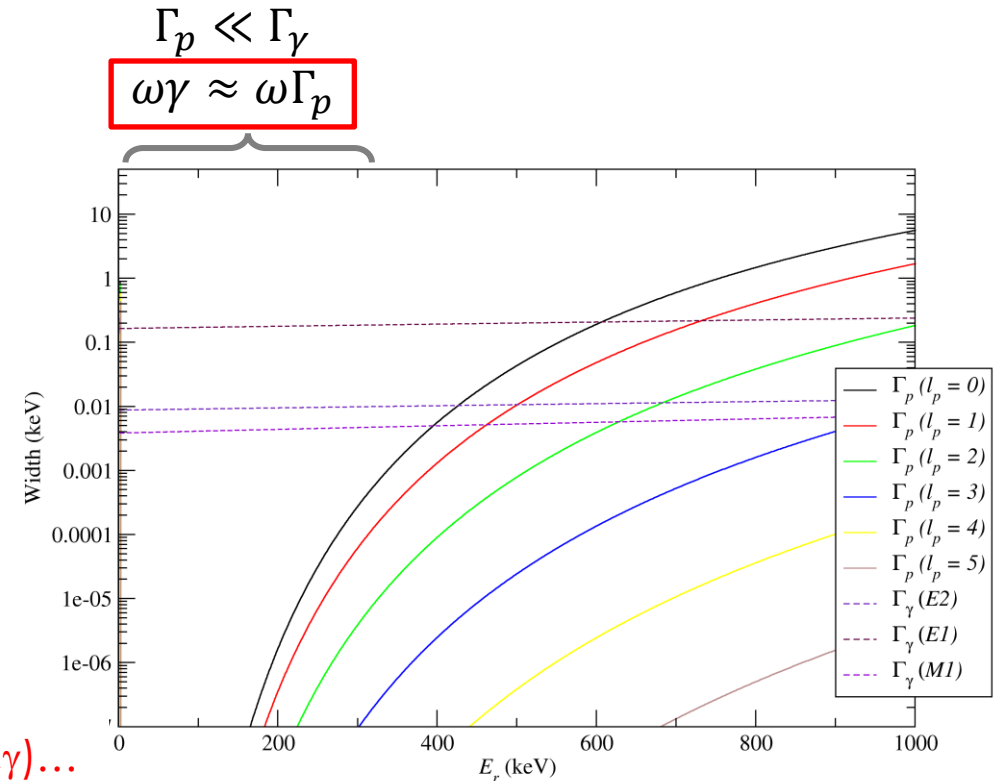
$$\omega\gamma \approx \omega\Gamma_p$$



Benchmark against $^{26}\text{Al}(p,\gamma)\dots$

$$\langle \sigma v \rangle = \left(\frac{2\pi}{\mu kT} \right)^{3/2} \eta^2 \omega \gamma \exp\left(-\frac{E}{kT}\right)$$

$$\omega = \frac{2J+1}{(2J_1+1)(2J_2+1)} (1 + \delta_{l_2}) \quad \gamma = \frac{\Gamma_p \Gamma_\gamma}{\Gamma}$$

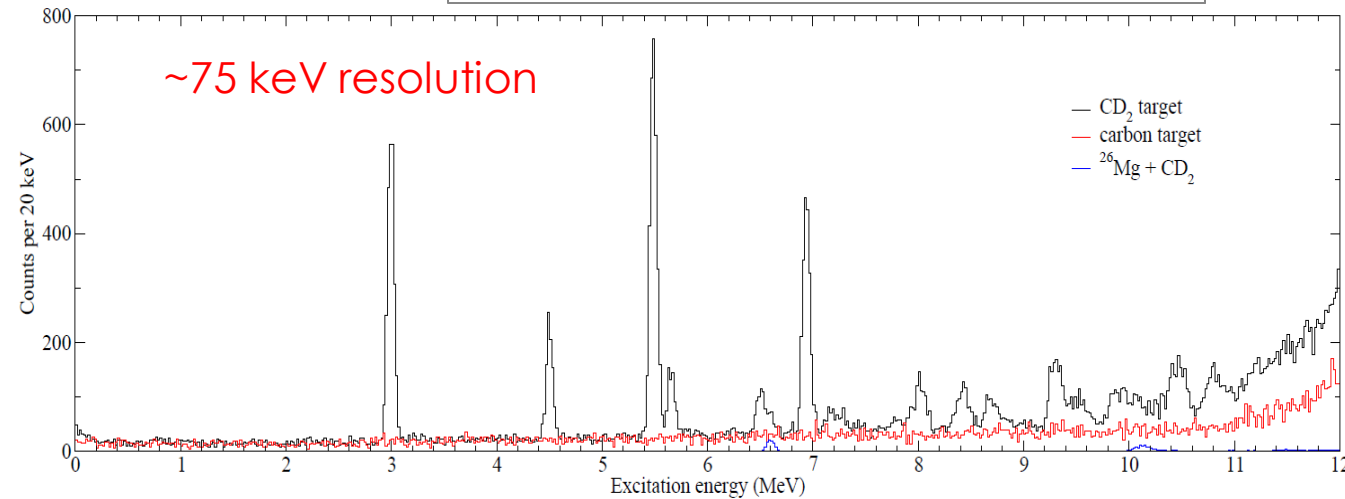
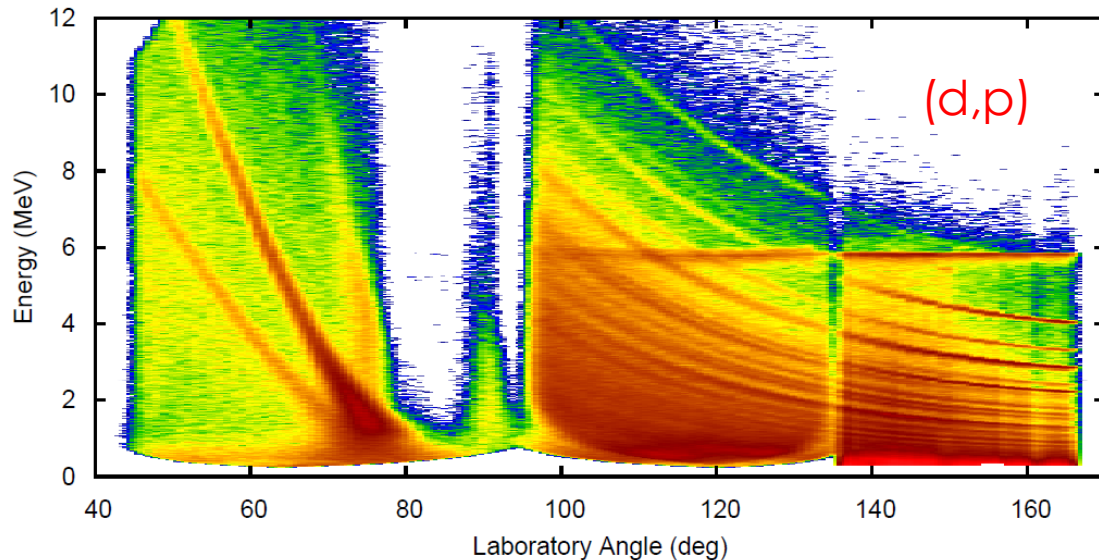
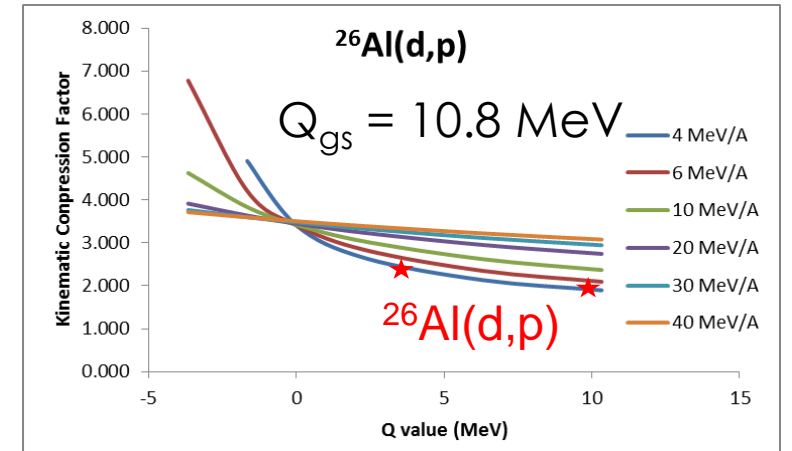
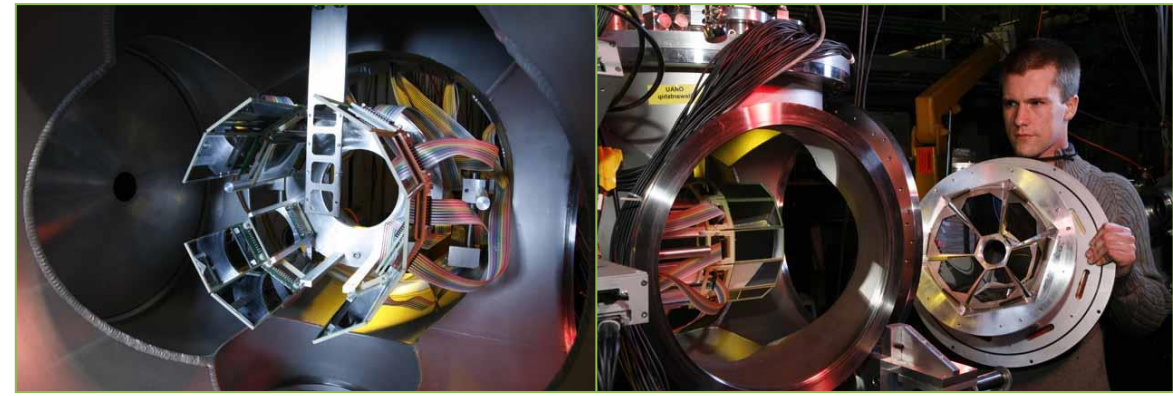


$^{26}\text{Al}(d,p)^{27}\text{Al}$ experiment

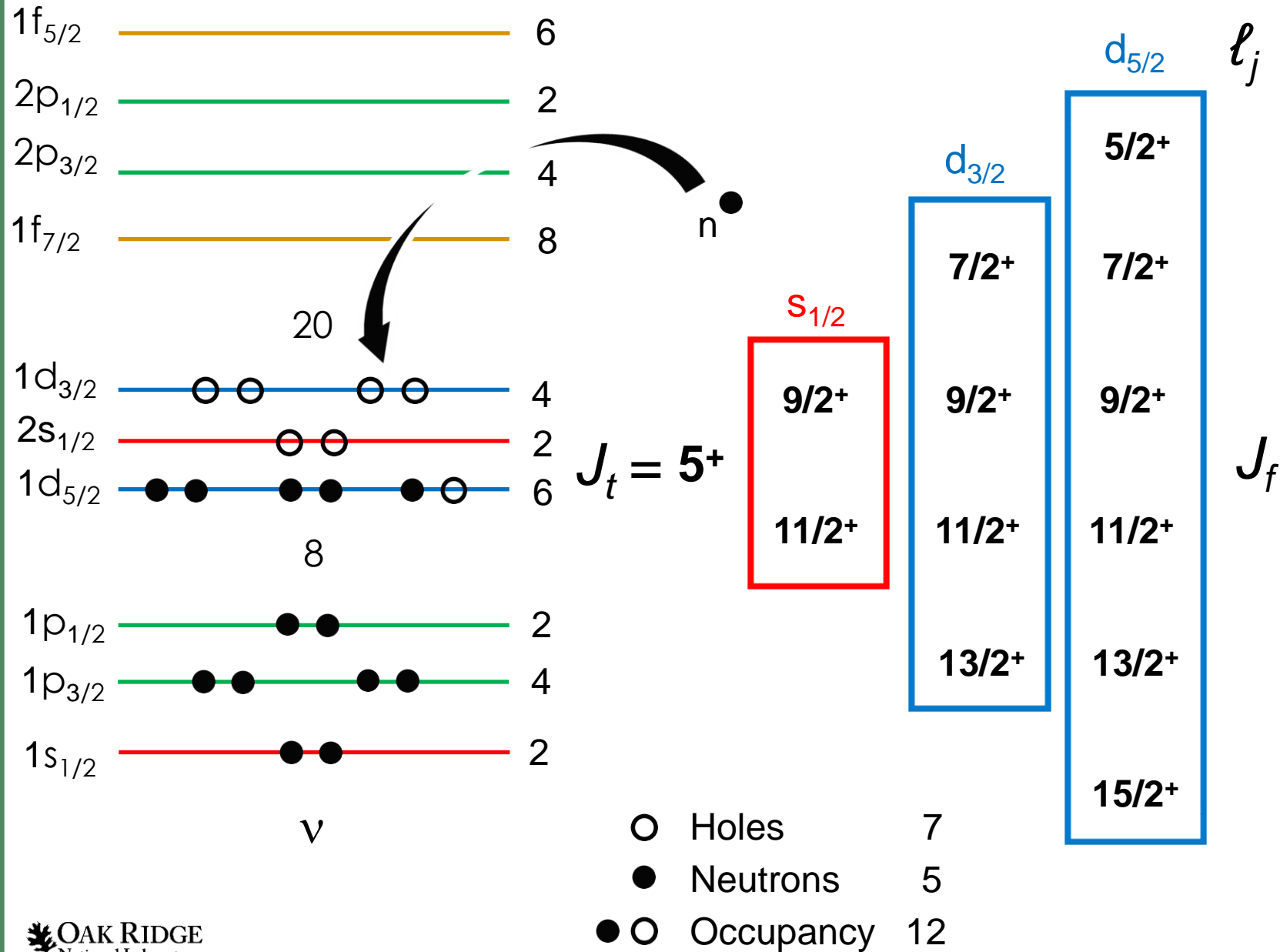


RRUBA

- 4.5 MeV/u ^{26}Al (Oak Ridge Tandem)
- 5×10^6 pps
- $150 \mu\text{g}/\text{cm}^2$ CD_2
- MCP normalization (200 kHz)
- Large Q value = low kinematic compression



^{26}Al sd -shell states

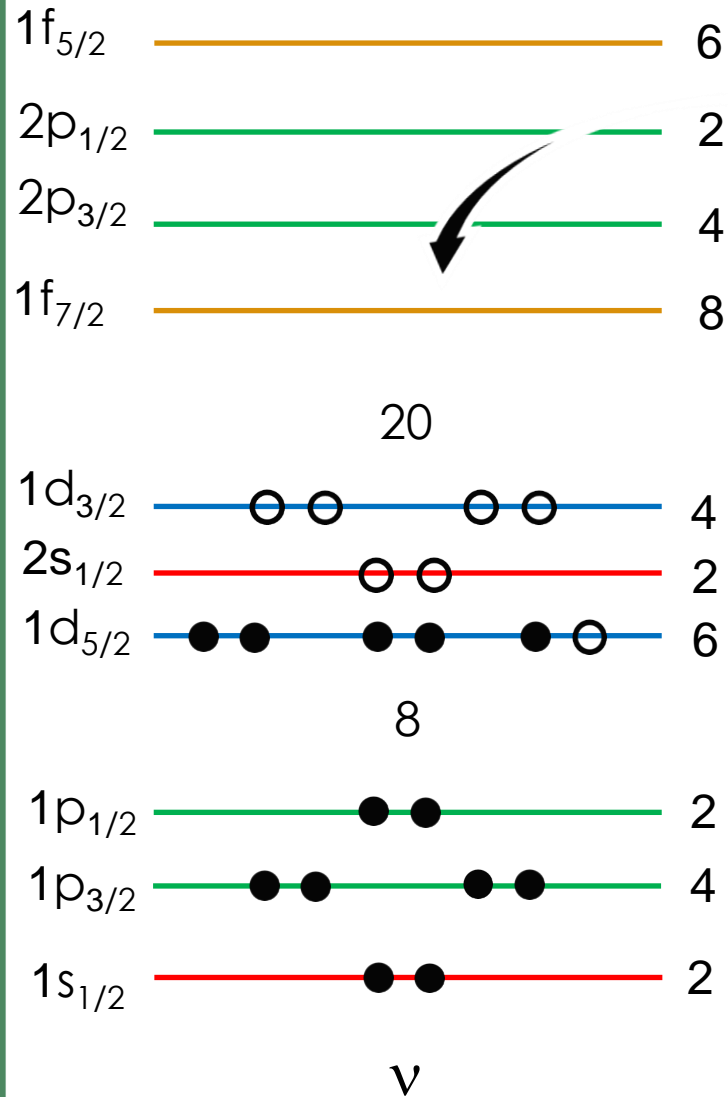


What to expect?

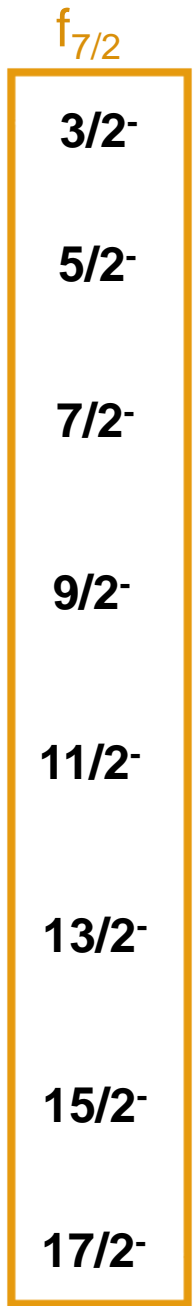
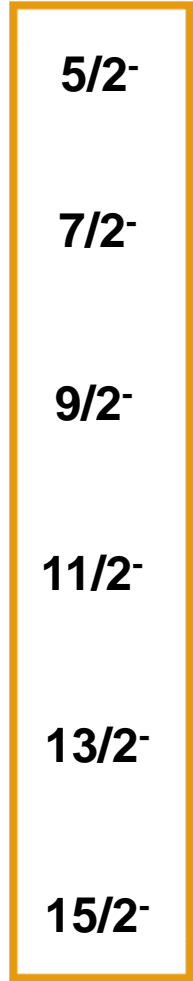
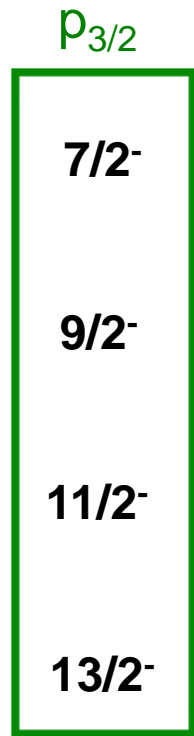
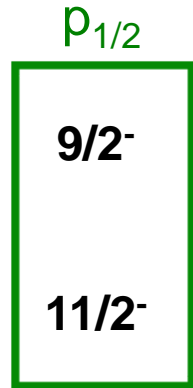
- sd -shell excitations
- fp -shell excitations at higher E_x

$$J_t - j \leq J_f \leq J_t + j$$

^{26}Al fp -shell states



$J_t = 5^+$



ℓ_j

J_f

What to expect?

- sd -shell excitations
- fp -shell excitations at higher E_x

$$J_t - j \leq J_f \leq J_t + j$$

$^{26}\text{Al}(d,p)^{27}\text{Al}$ angular distributions

total

s wave

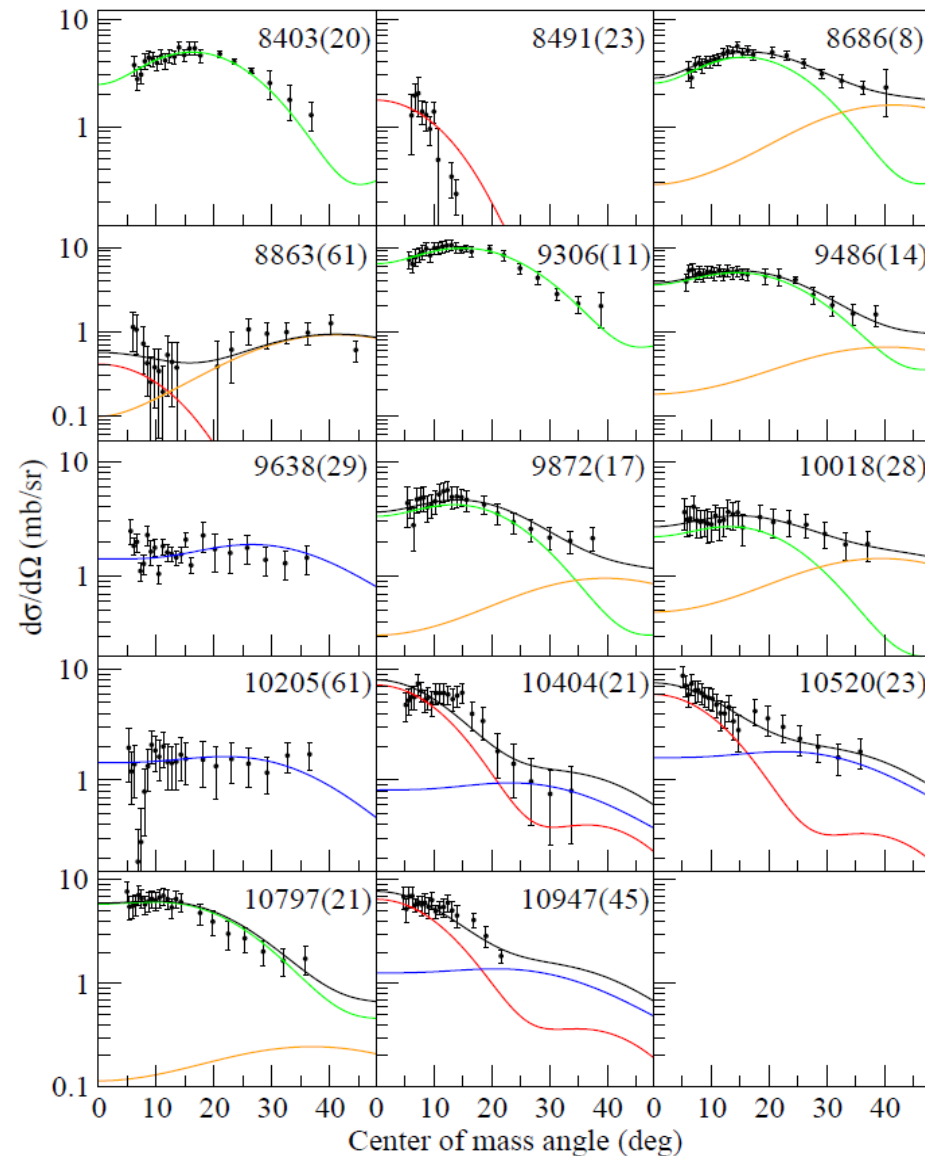
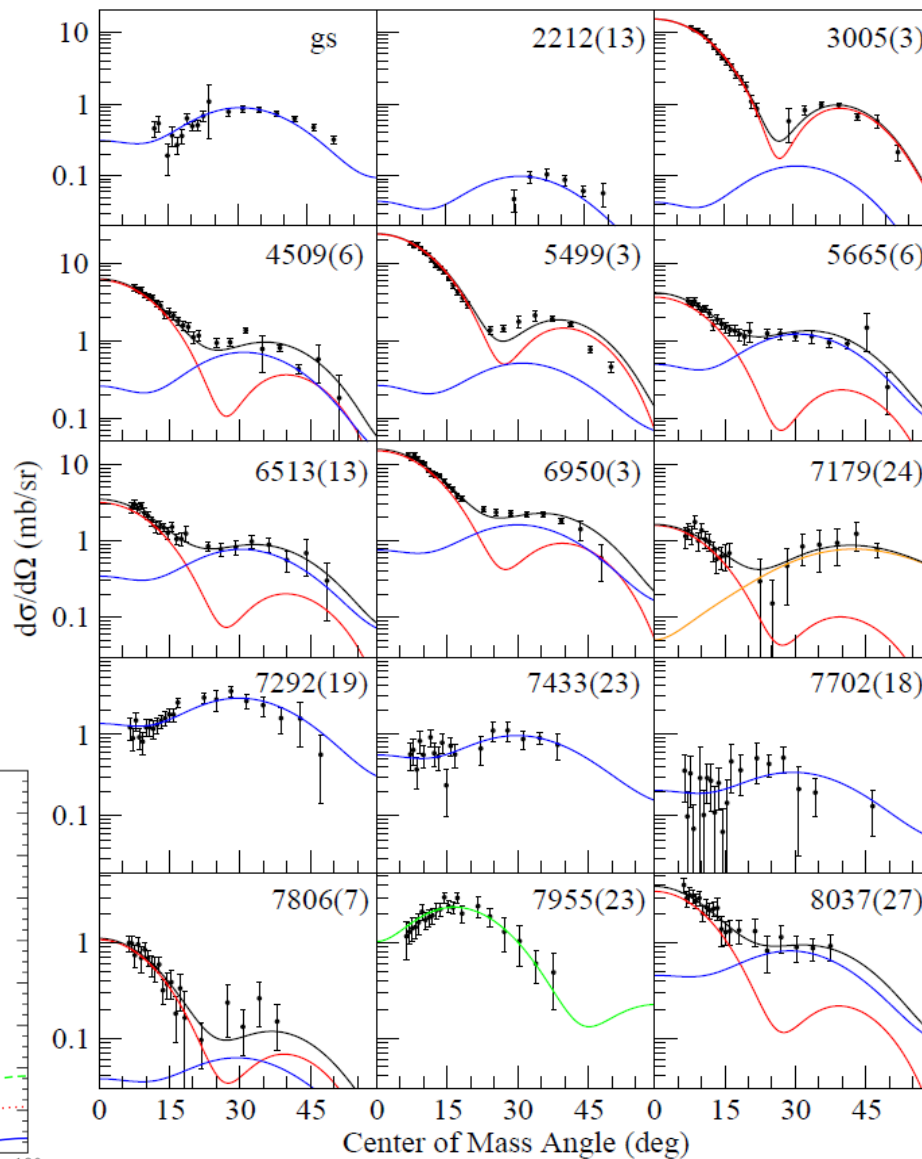
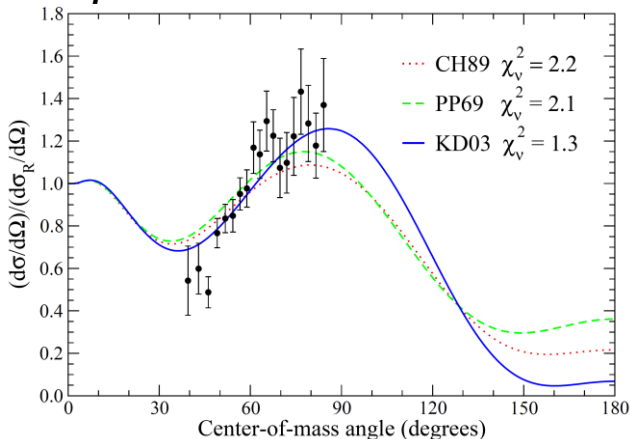
p wave

d wave

f wave

Important for quality analysis of transfer data

- Good coverage of first stripping peak
- ADWA
- Finite Range (d and T)
- KD nucleon-nucleus OMPs
- Standard geometry parameters

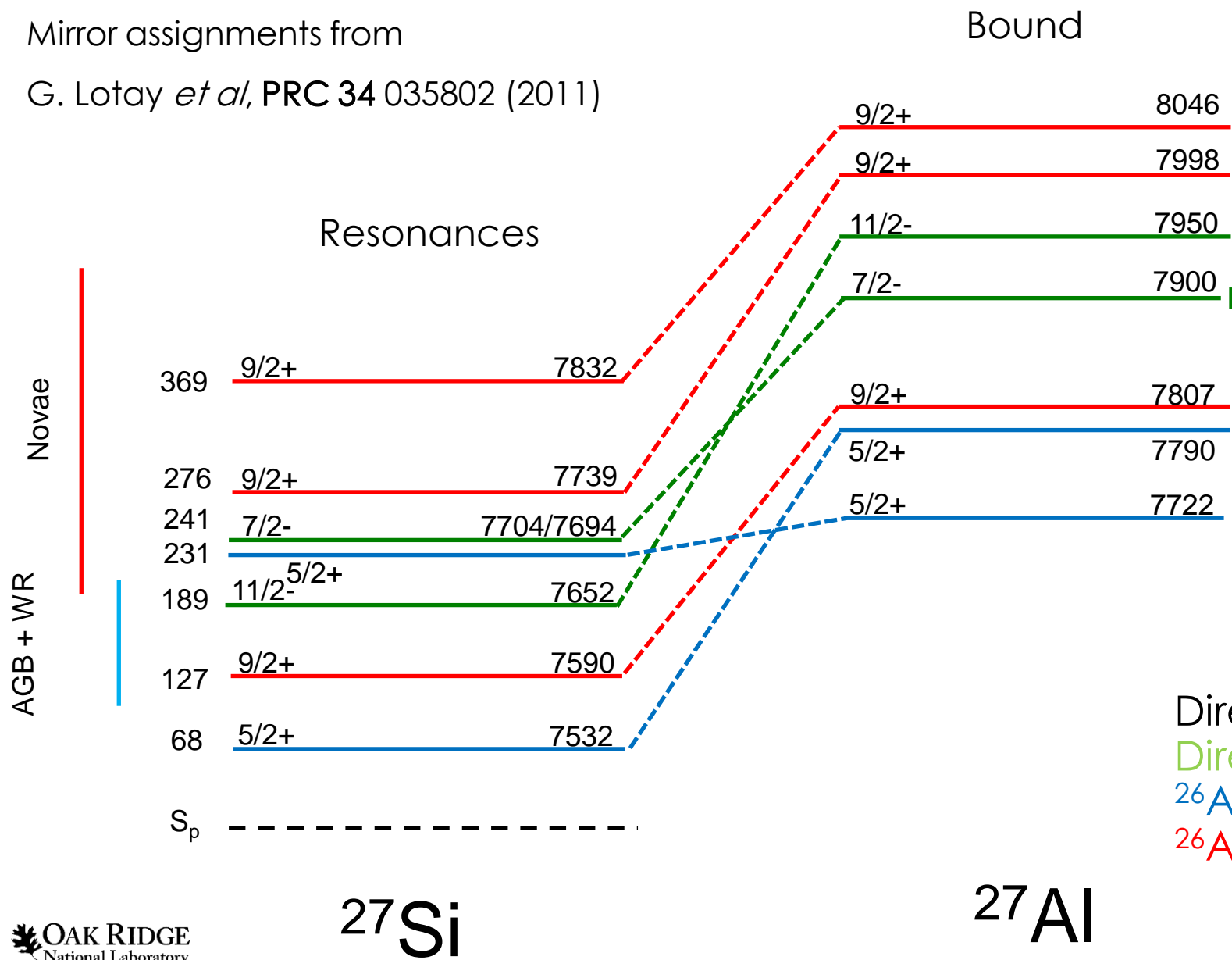


Resonance strengths from (d,p)

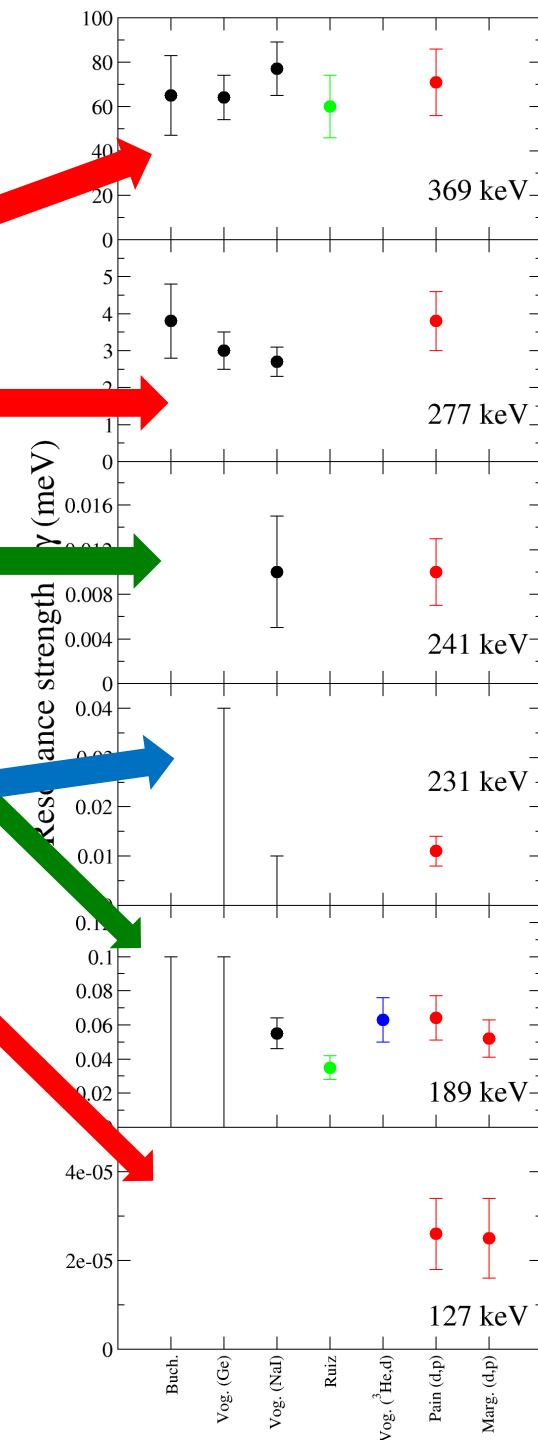
SMEC gives ~10-20% reduction in C^2S for ^{27}Si unbound states

Mirror assignments from

G. Lotay *et al*, PRC 34 035802 (2011)

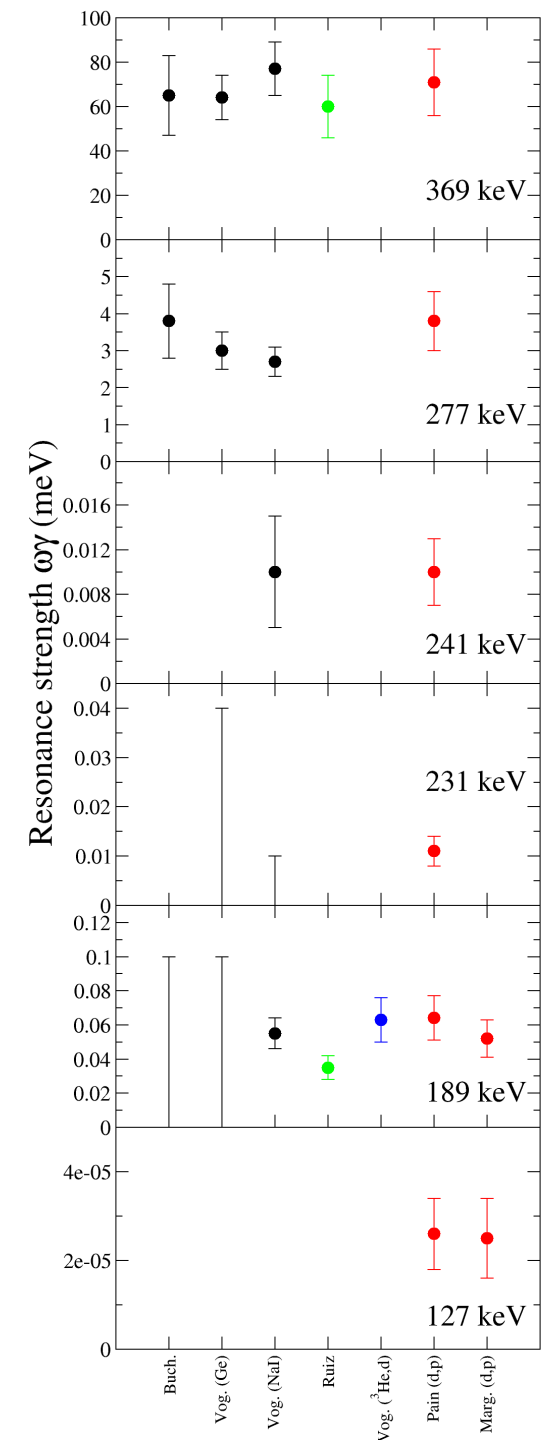
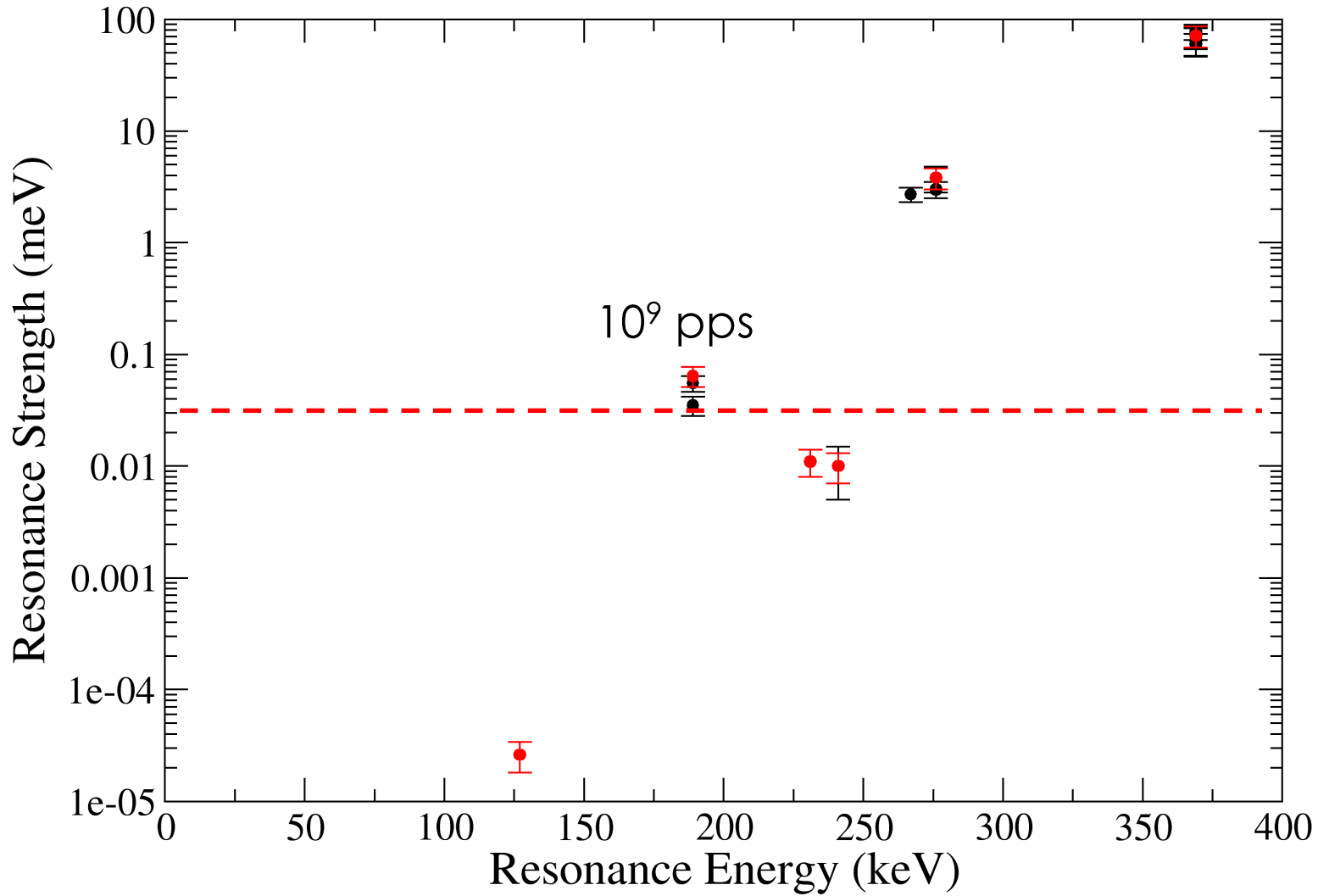


Direct (p, γ) NK
 Direct (p, γ) IVK
 $^{26}\text{Al}(^3\text{He},d)^{27}\text{Si}$
 $^{26}\text{Al}(d,p)^{27}\text{Al}$



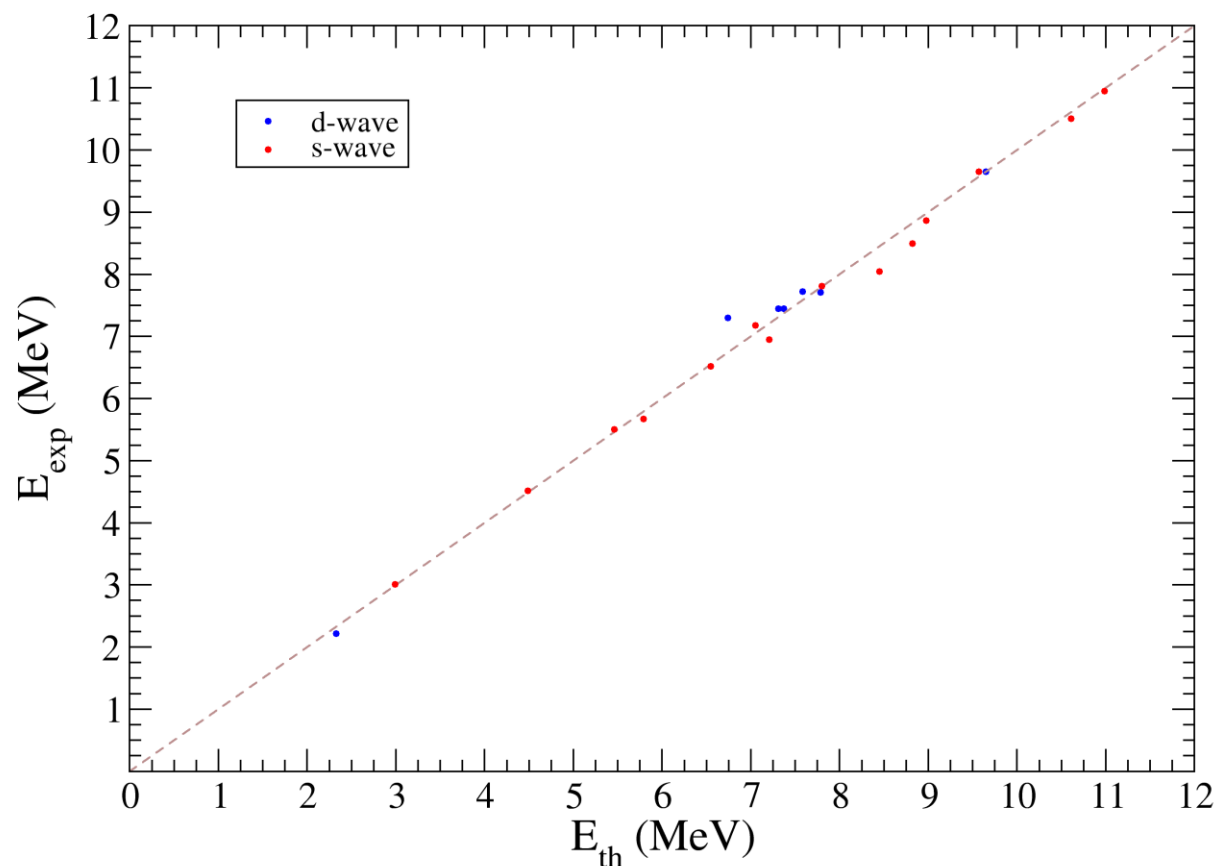
Resonance strengths

$^{26}\text{Al}(p,\gamma)^{27}\text{Si}$ Resonances



Comparison with USDB - energies

- Using NuShellX@MSU
- Calculated the first 40 states of each positive parity ($5/2+$ - $17/2+$) in ^{27}Al (dim 80,000) and calculate overlaps with ^{26}Al 5+ ground state (dim 70,000) (few minutes with 6-core/12-threads (280 states total))
- Match by comparing C^2S and energy



Excellent agreement in energies

- Perhaps unsurprising, as USDB fitted to energy levels in the SD shell (608 states, 77 nuclei, incl $^{26,27}\text{Al}$)
 - Only fitted up until J^π becomes ambiguous - typically around 6-7 MeV
 - Agreement up to 11 MeV in expt

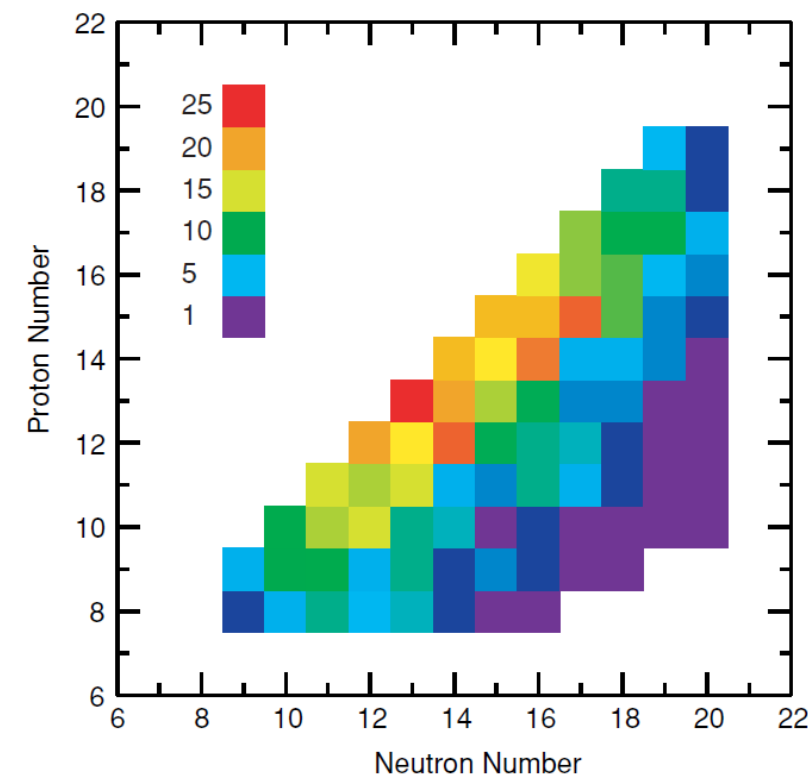
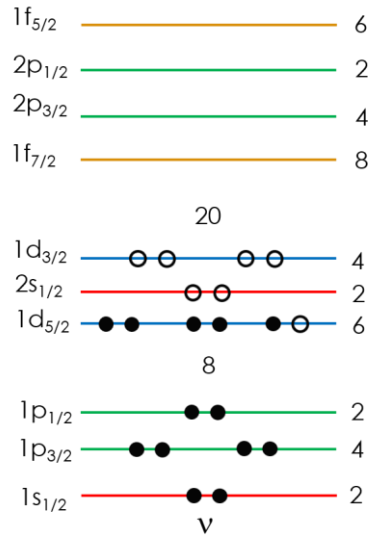


FIG. 2. (Color) Number of states used for the USDA and USDB Hamiltonians for each nucleus.

Comparison with USDb

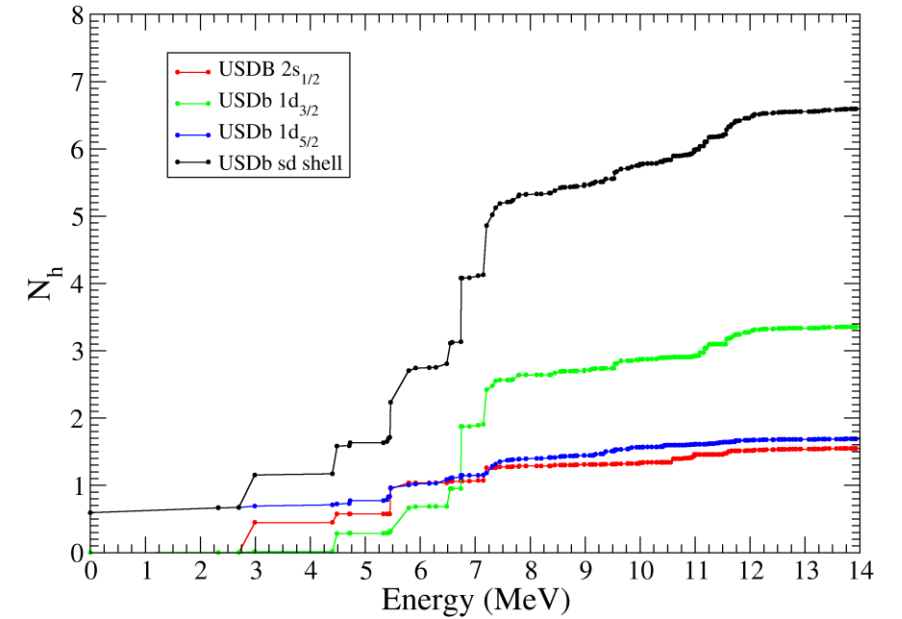


Macfarlane & French sum rules

$$N_h = \sum_E \frac{2J_f + 1}{2J_t + 1} C^2 S_{(d,p)}$$

$$N_n + N_h = 12 \text{ (for sd shell)}$$

- Vacancies 7
- Occupancies 5
- ○ sd-shell space 12



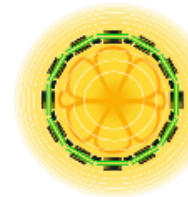
Summary

- Impossibly broad scope of FRIB transfer reaction program - focus on a couple of unique opportunities
- Developments in SRM: (d,p) for (n, γ)
- Opportunities for (d,p) measurements at the S800
 - strong beams in the mass ~ 80 region
 - discrete particle and particle- γ spectroscopy
 - New technique: SRM for CN neutron transfer using recoils, and γ s
 - Two approved experiments GODDESS+S800 upcoming
- Ability to produce high-quality Reacc. beams with controllable isomer content
 - Mirror studies for (p, γ) reactions on isomers, ultimately (p, γ) SECAR
 - Direct (α ,p) measurements (JENSA) on isomers, ultimately SECAR
 - Two approved ReA experiments – $^{34}\text{Cl}(d,p)$ and $^{26}\text{Al}/^{26}\text{Si}(\alpha,p)$
 - expt/SM across the sd N=Z (^{22}Na , ^{30}P , $^{34g,m}\text{Cl}$, $^{26g,m}\text{Al}$, $^{38g,m}\text{K}$)

Thanks

ORRUBA, GODDESS, JENSA and SECAR Collaborations
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ReA: A. Henriques, A. Lapierre, K. Lund, Y. Liu, S. Nash, C. Sumithrarachchi, A. Villari



ORRUBA
Si detector array

JENSA **SECAR**

