



Experiments with exotic nuclei II

MICHIGAN STATE
UNIVERSITY

Advancing Knowledge.
Transforming Lives.

Monday

~~Tuesday~~ *Monday*

Excited states

Experimental considerations: Reactions

Collectivity

Single-particle degrees of freedom

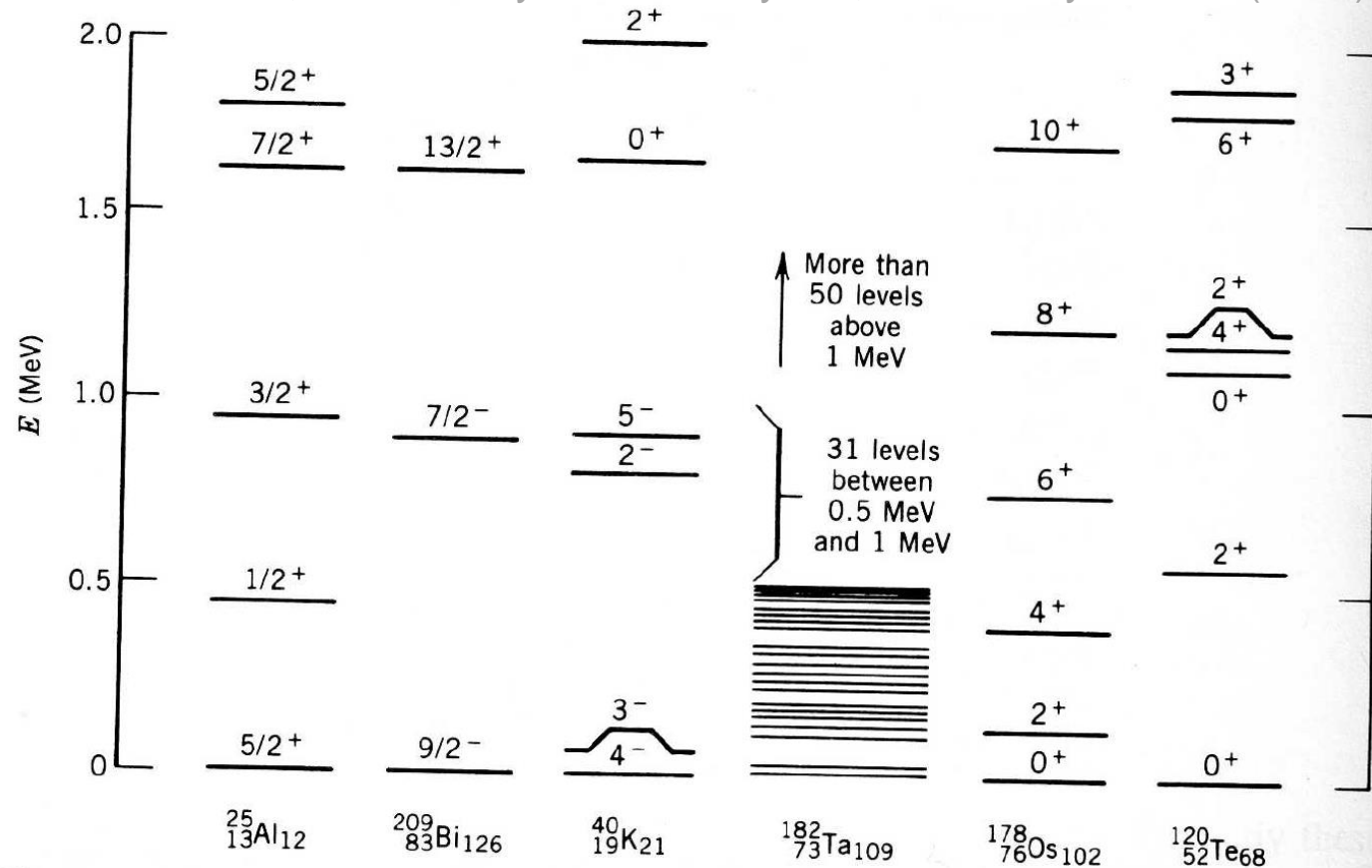
Transfer and knockout (only brief: See A. Wuosmaa lectures)

Excited-state lifetimes

K. S. Krane, Introductory Nuclear Physics, John Wiley & Sons (1988)

Collective excitation:
all nucleons outside a closed shell contribute coherently to the excitation (vibration, rotation)

Single-particle excitation: Excited states are formed by rearranging one or a few nucleons in their orbits

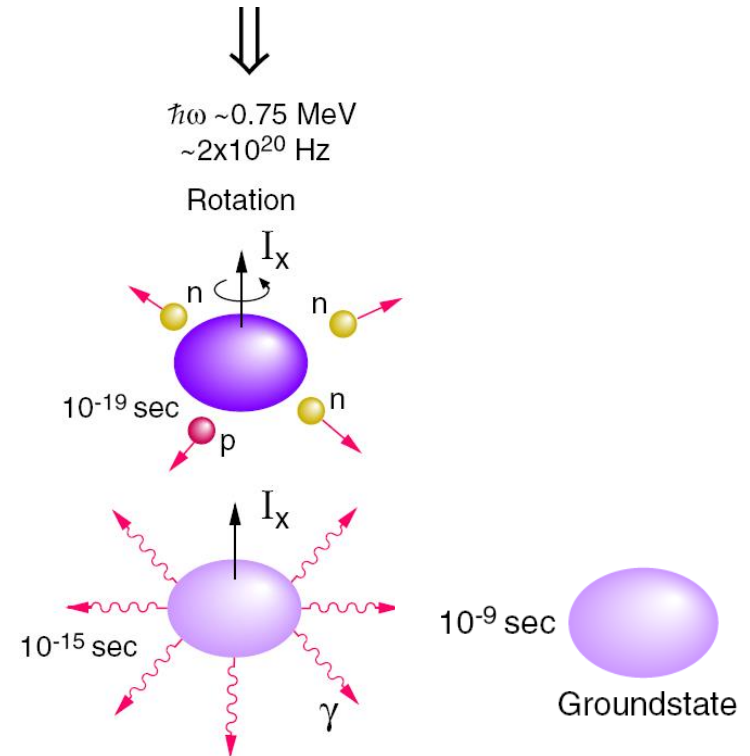
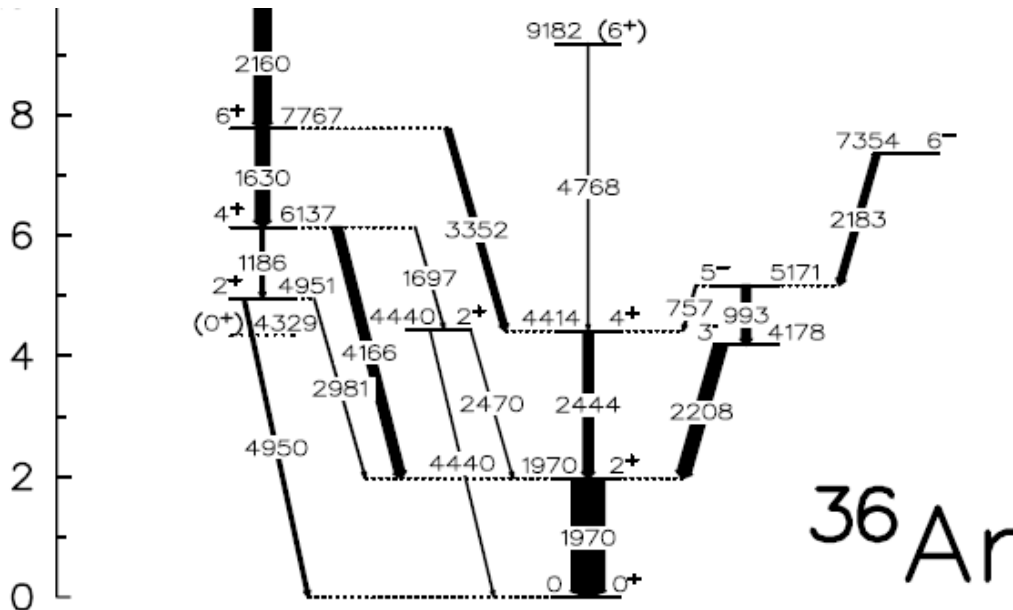
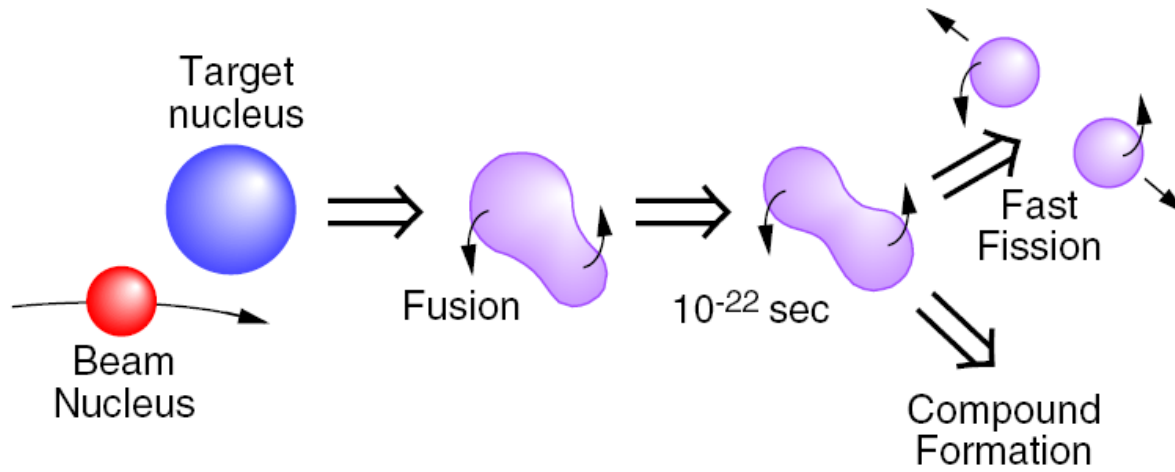


• In nuclei, the energy scales are close:

$$E_{\text{rot}} \sim E_{\text{vib}} \sim E_{\text{sp}} \text{ (MeV)}$$

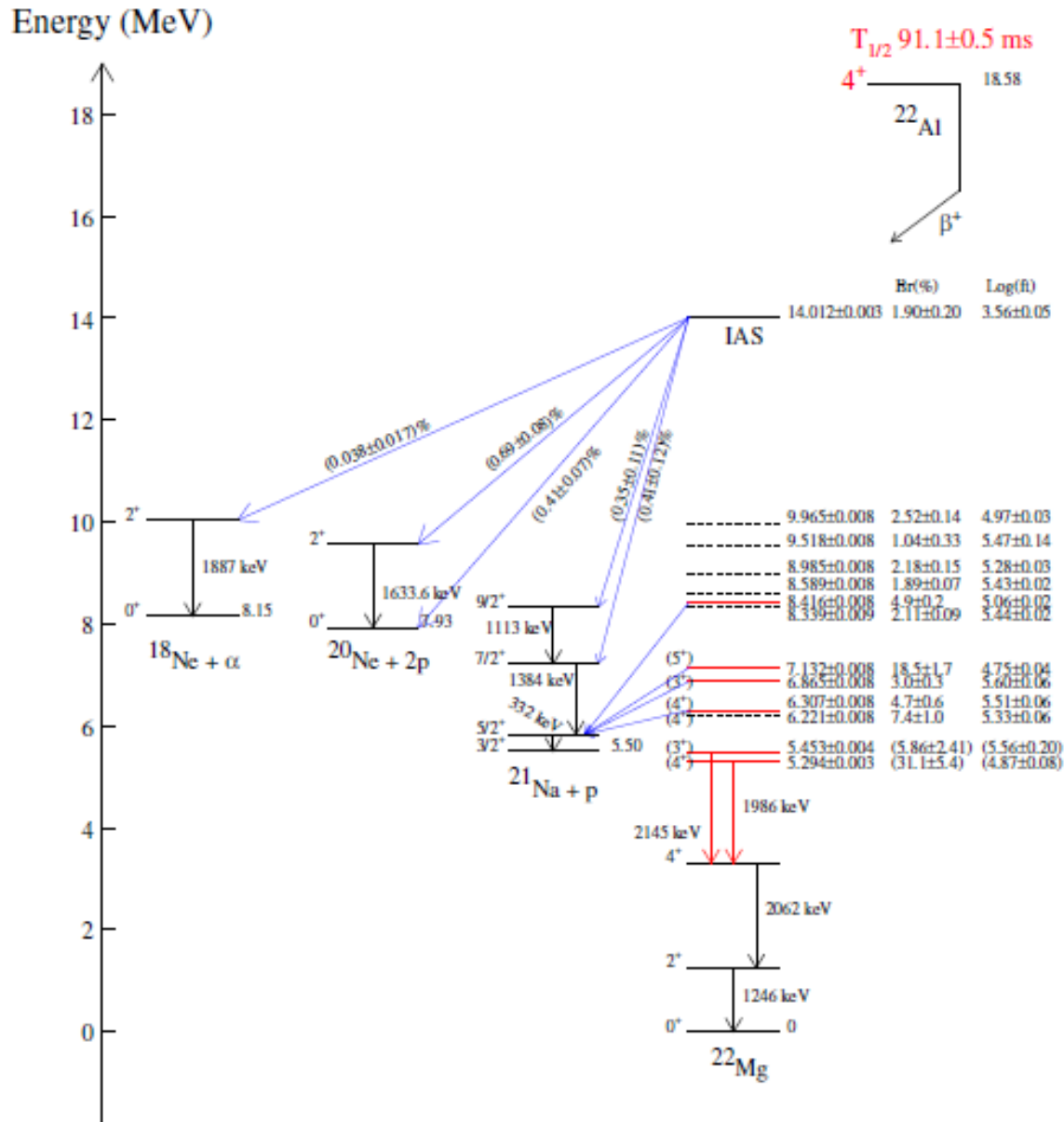
In your hands-on measurement, you will be able to study ^{24}Mg , a well-deformed rotor

Collective and single-particle excitation can be separated but interact strongly



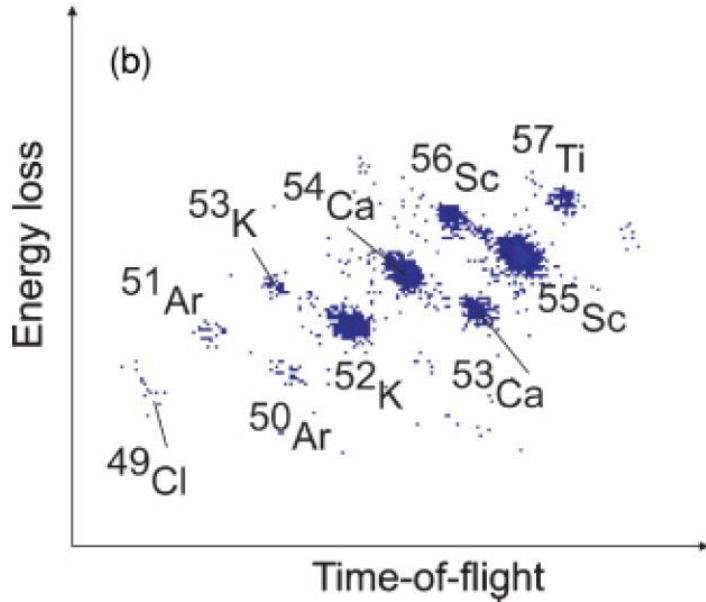


Population of excited states - Decays

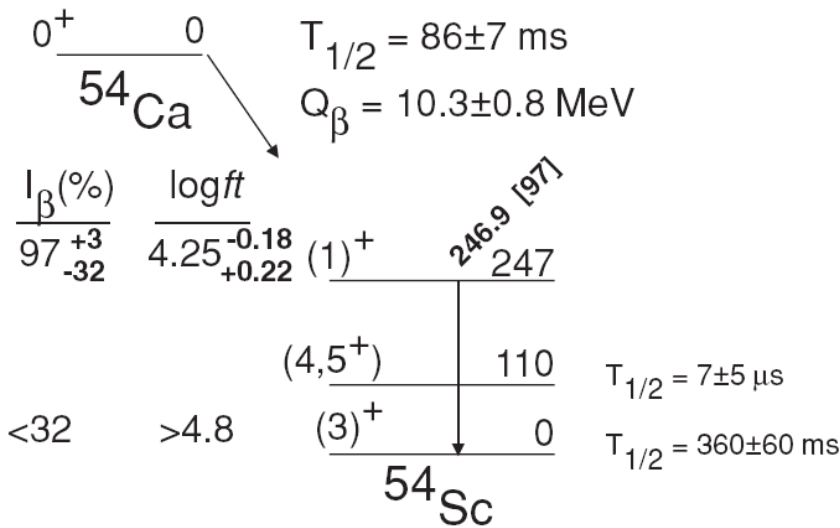
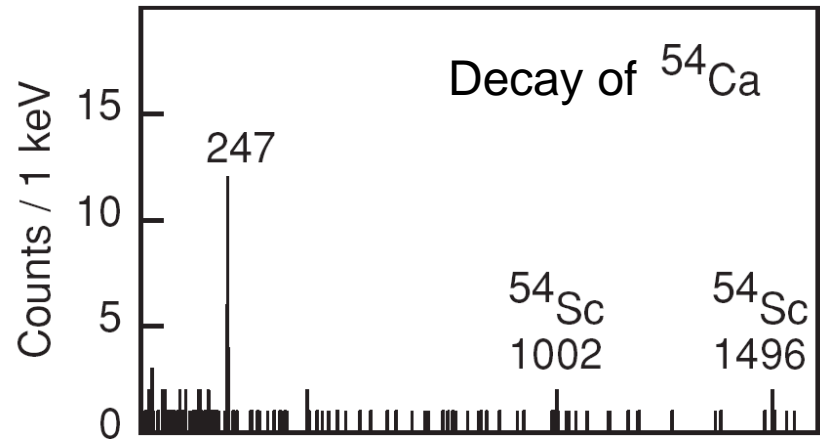


Excited states populated in β decay

Selectivity through selection rules



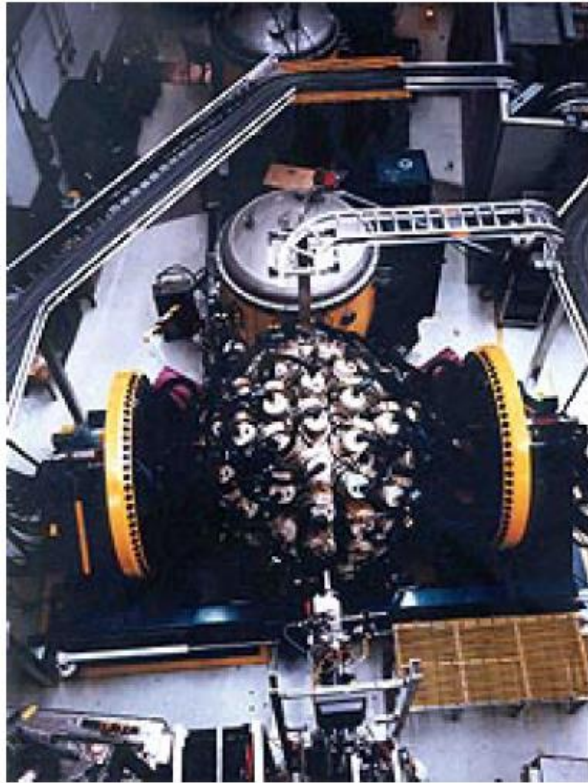
Total number of ^{54}Ca implants: 654 only



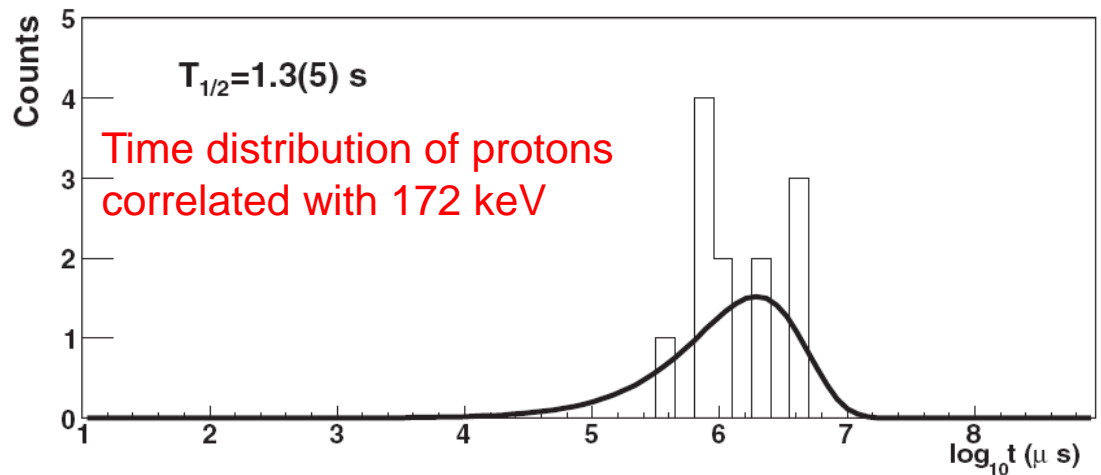
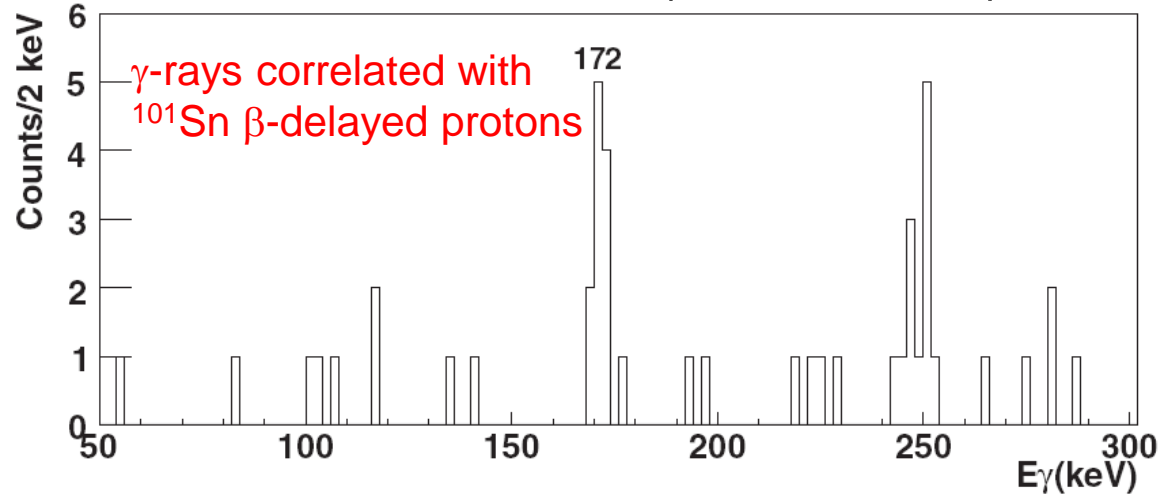
Selection rules in β decay, any textbook

Type	$\log(ft)$	L	$\Delta\pi$	ΔJ	
				$\vec{S} = \vec{0}$ Fermi	$\vec{S} = \vec{1}$ Gam-Tel
super-allowed	2.9-3.7	0	+	0	0
allowed	4.4-6.0	0	+	0	0,1
first forbidden	6-10	1	-	0,1	0,1,2
second forbidden	10-13	2	+	1,2	1,2,3
third forbidden	> 15	3	-	2,3	2,3,4

γ -ray spectroscopy tagged with β -delayed protons



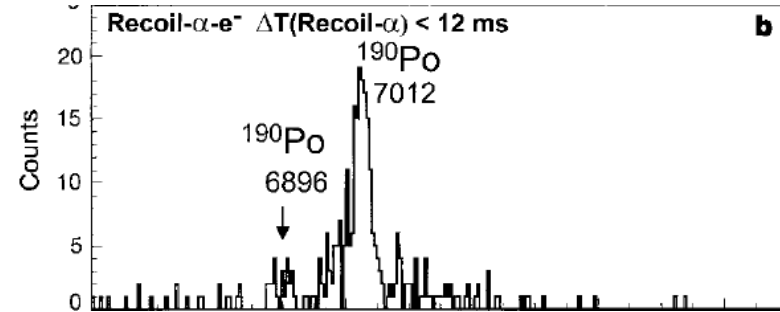
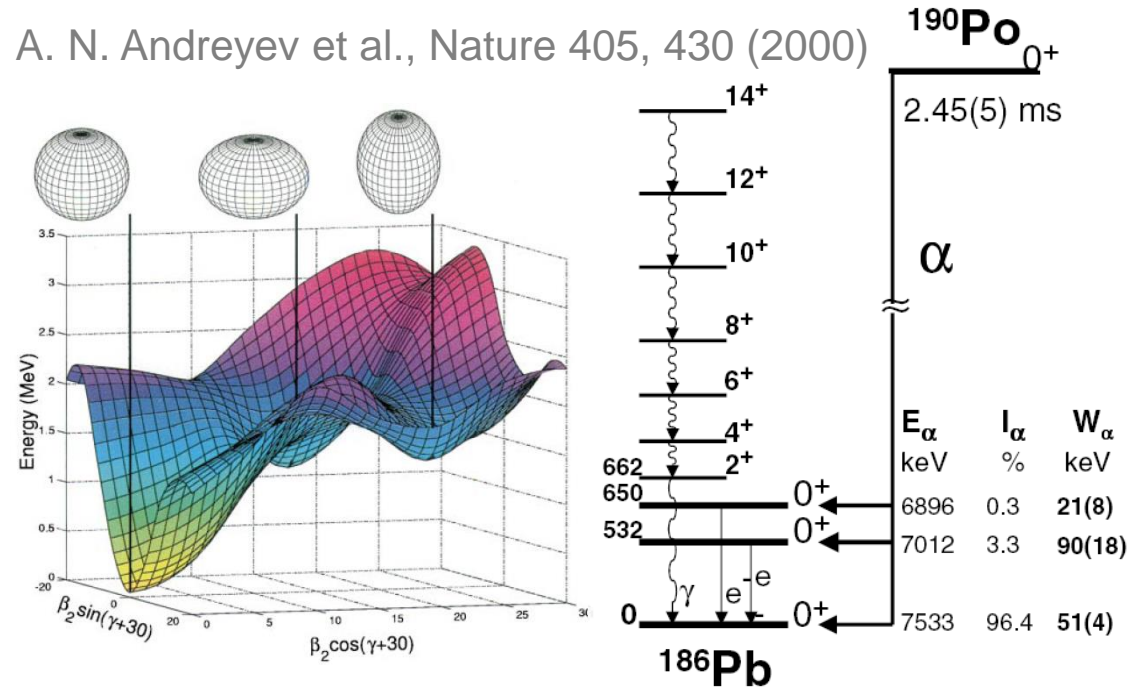
$^{58}\text{Ni}+^{46}\text{Ti}$ at 192 MeV (ATLAS/ANL)



Single-neutron states
above doubly magic
 ^{100}Sn :
 $d_{5/2} - g_{7/2} \sim 172 \text{ keV}$

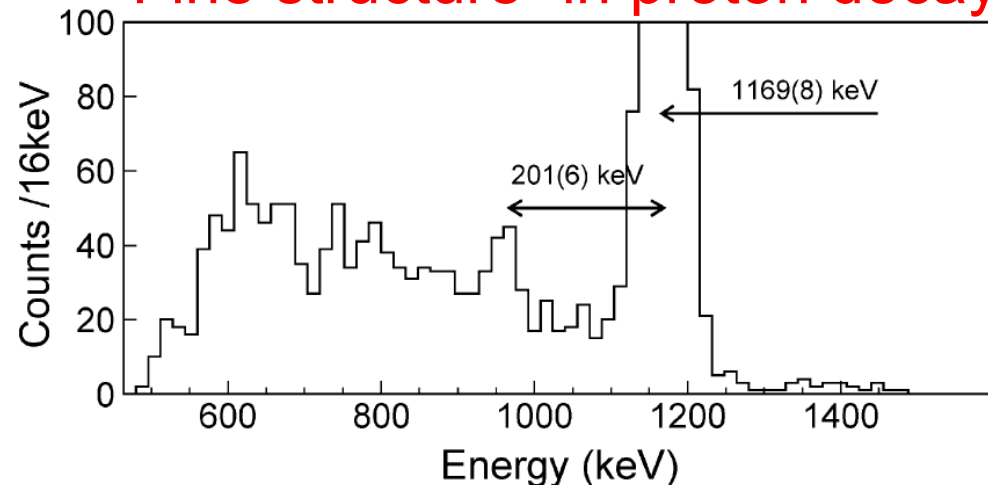
Excited states populated following α and proton emission

A. N. Andreyev et al., Nature 405, 430 (2000)



Ground state and first excited state (201 keV) of ^{140}Dy populated in proton decay of ^{141}Ho

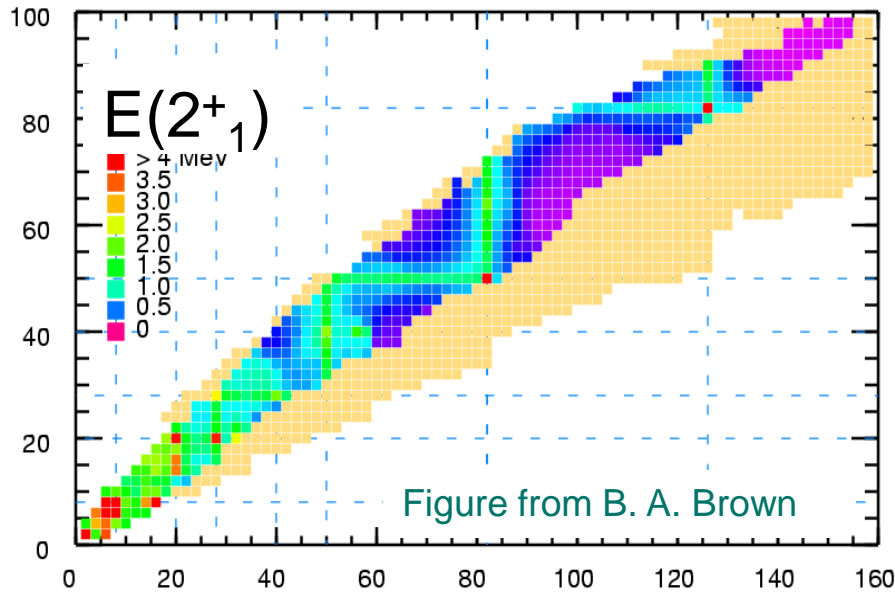
“Fine structure” in proton decay



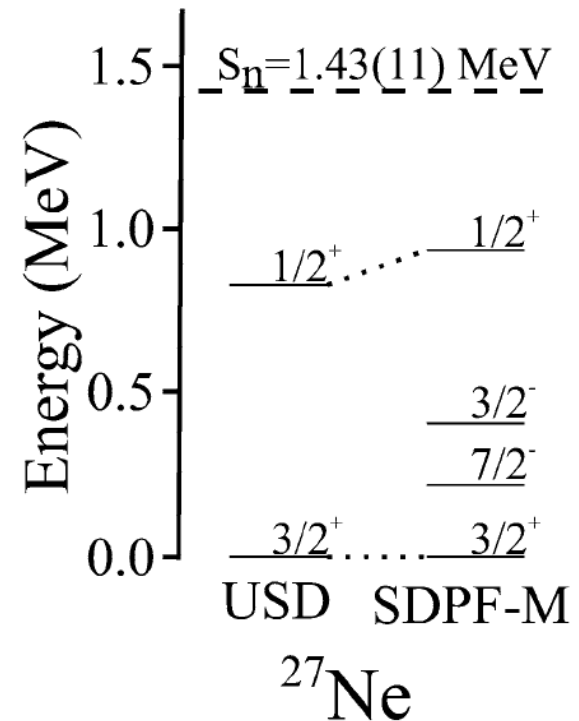
M. Karny et al., PLB 664, 52 (2008)

Structure information from excited states

As one indicator of shell closures

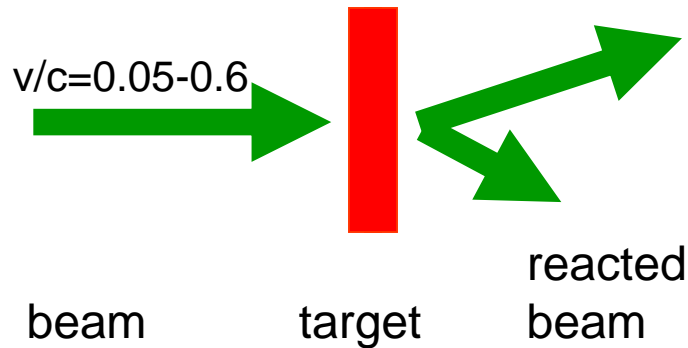


Guide model calculations





Experimental considerations: *Reactions*



- The choice of the target depends on the reaction that is desired

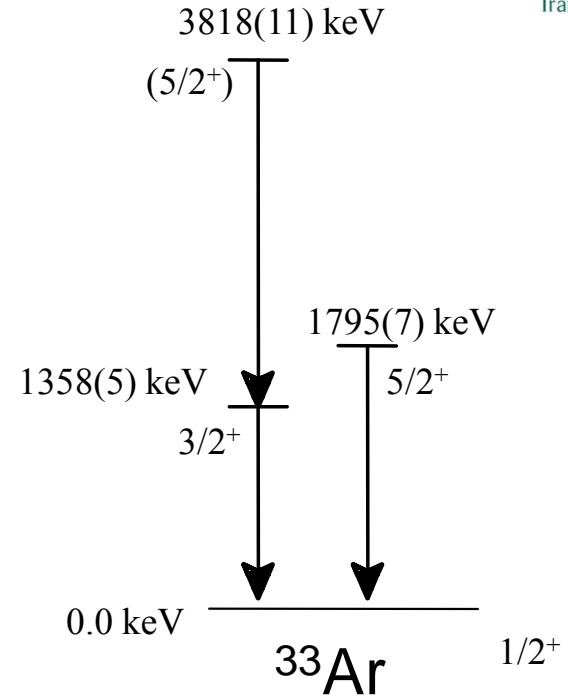
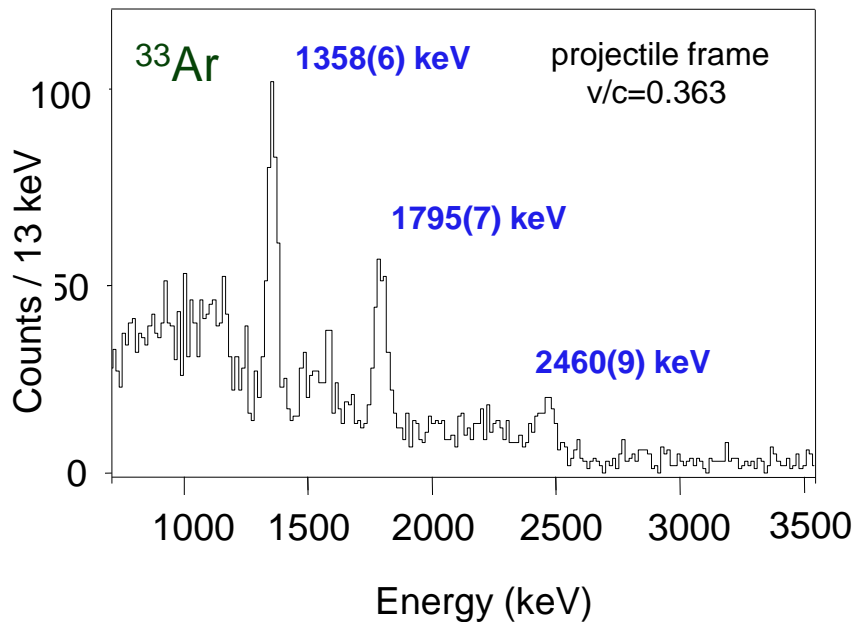
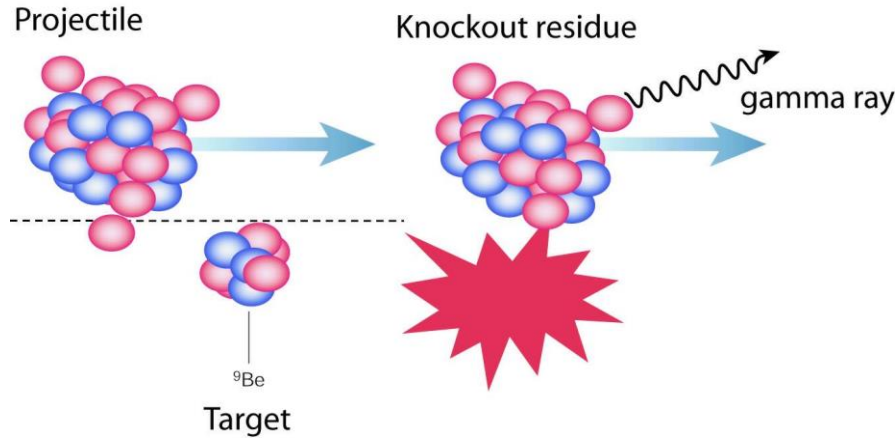
- $N_R = \sigma \times N_T \times N_B$
 - σ Cross section
 - N_T Atoms in target
 - N_B Beam rate
 - N_R Reaction rate

- Reactions

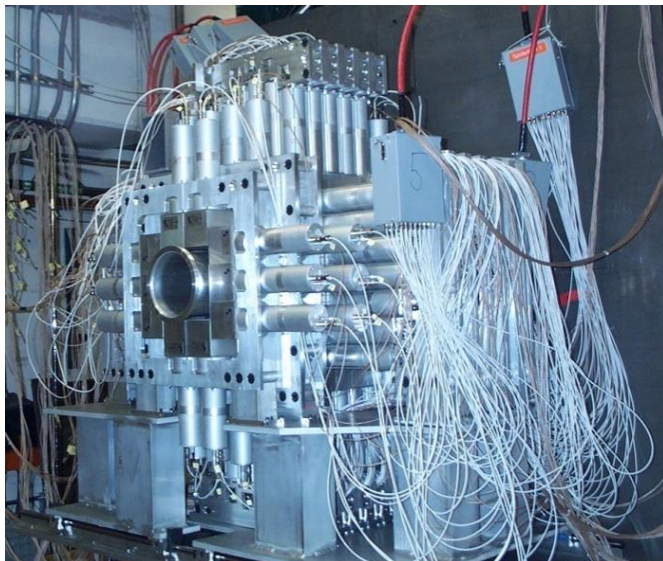
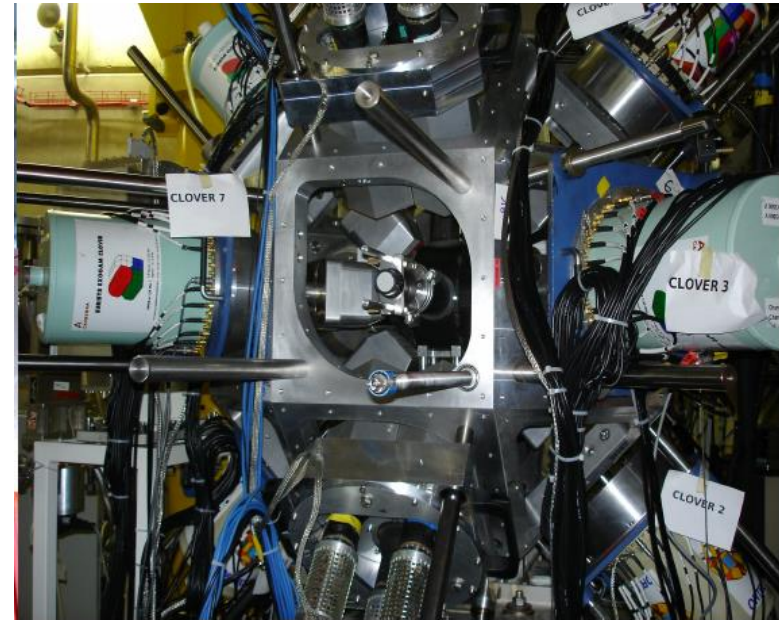
- Inelastic scattering
- Nucleon transfer
- Fusion, fusion-evaporation
- Breakup/fragmentation

- Experimental task

- Identify and count incoming beam
- Identify and count reacted beam
- Tag the final state of the reaction residue
- Measure scattering angles and momentum distributions

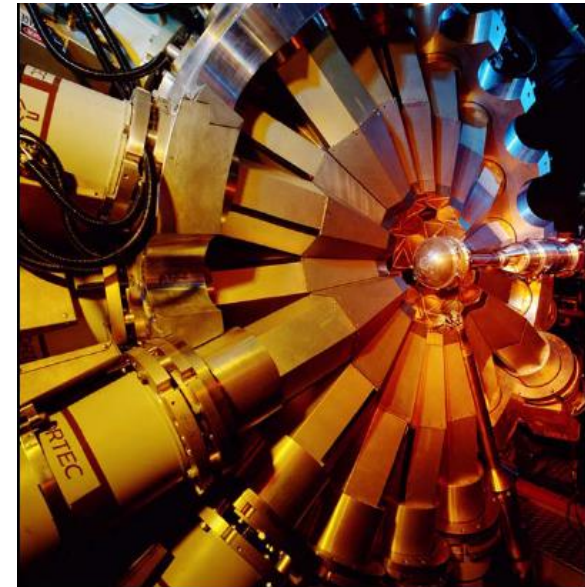


- Tag the population of excited states by measuring the decay γ rays. The γ -ray energy gives the energy difference between two states.



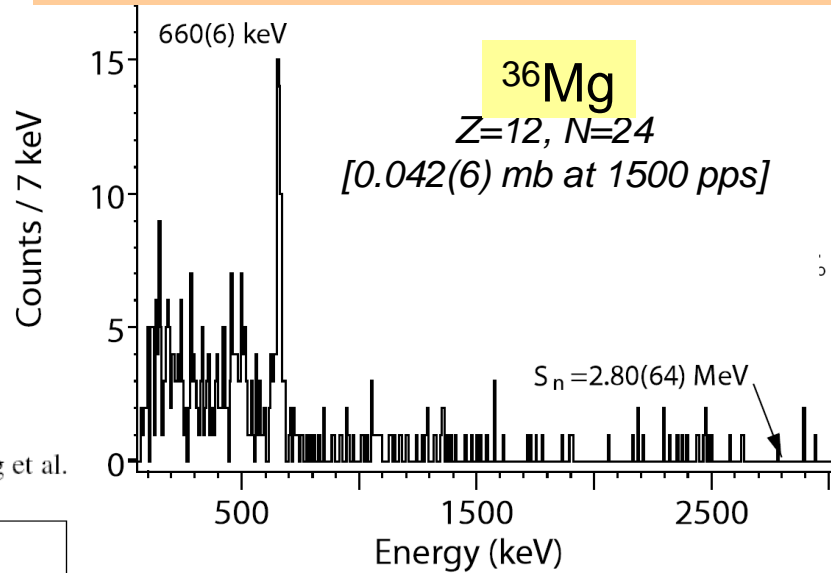
Germanium detectors:
Superior energy resolution, but modest efficiency

Scintillator-based:
High-efficiency, moderate resolution



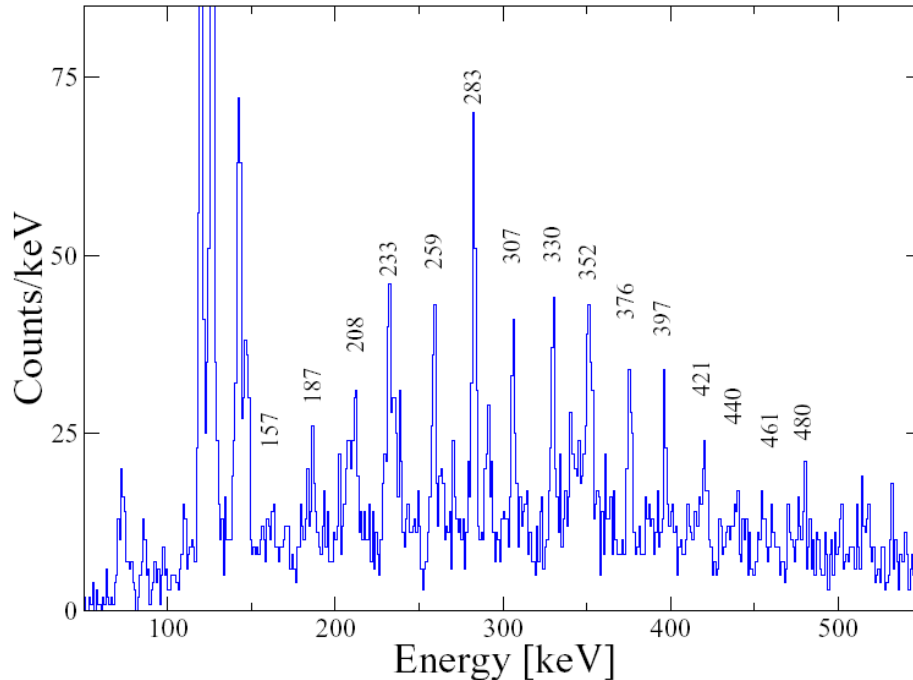
Two-proton knockout to ^{36}Mg .
Only the first excited state
was observed.

^{38}Si -2p at 83 MeV/u, SeGA @ NSCL



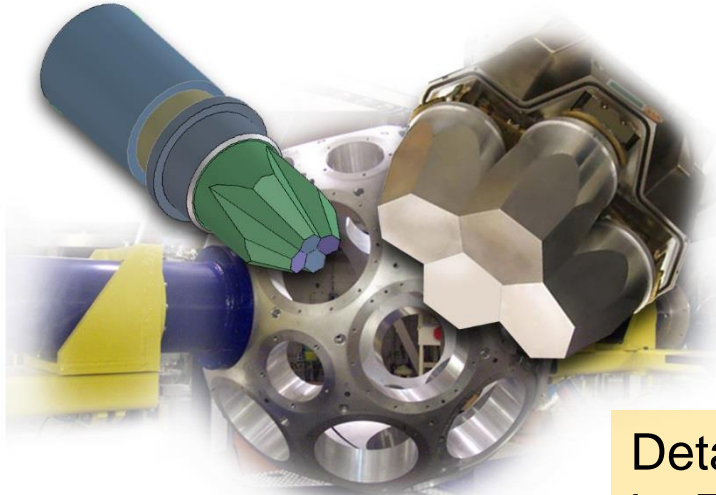
A. Gade et al., PRL 99, 072502 (2007)

$^{48}\text{Ca} + ^{207}\text{Pb} \Rightarrow ^{253}\text{No} + 2n$, JUROGAM+RITU+GREAT, R.-D. Herzberg et al.



Low-energy fusion-
evaporation reaction to
produce ^{253}No . Many excited
states are populated.

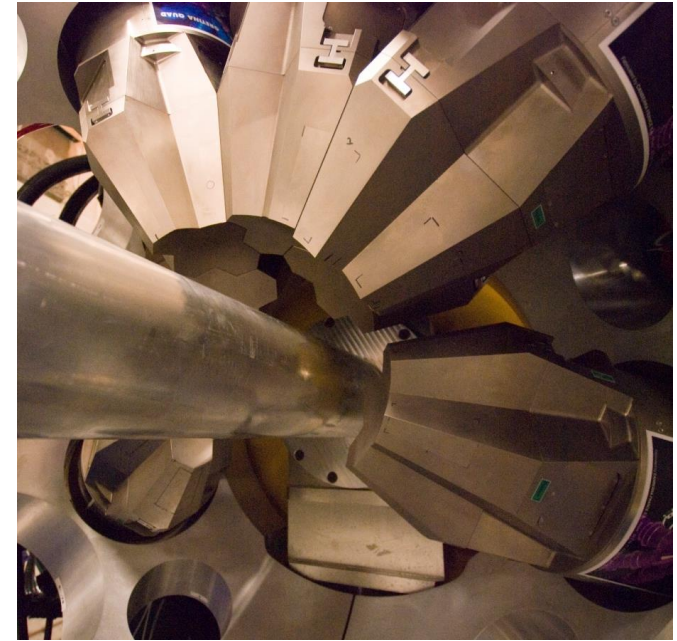
You will be doing an experiment with **GRETINA**



Lead institution: Lawrence Berkeley National Lab

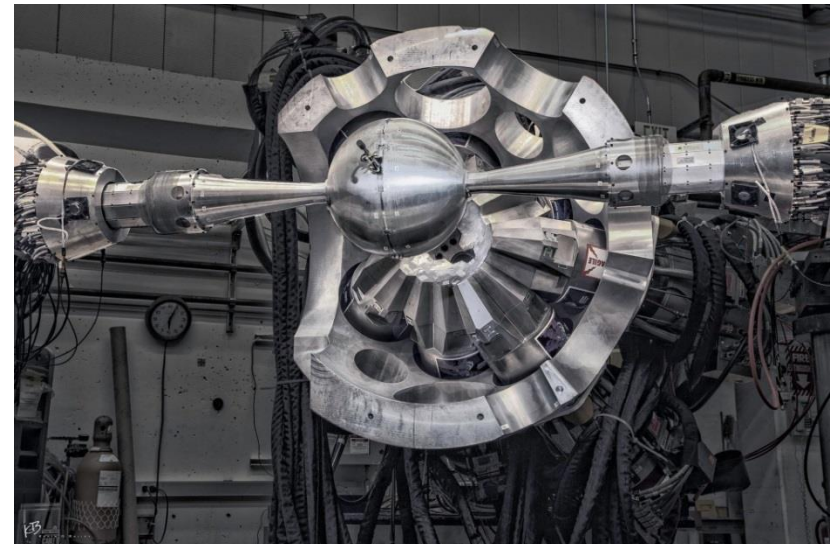
Array hosted by ANL and NSCL for experimental campaigns

Details in the lecture by T. Lauritsen



GRETINA is the next-generation Germanium-based gamma-ray tracking array:

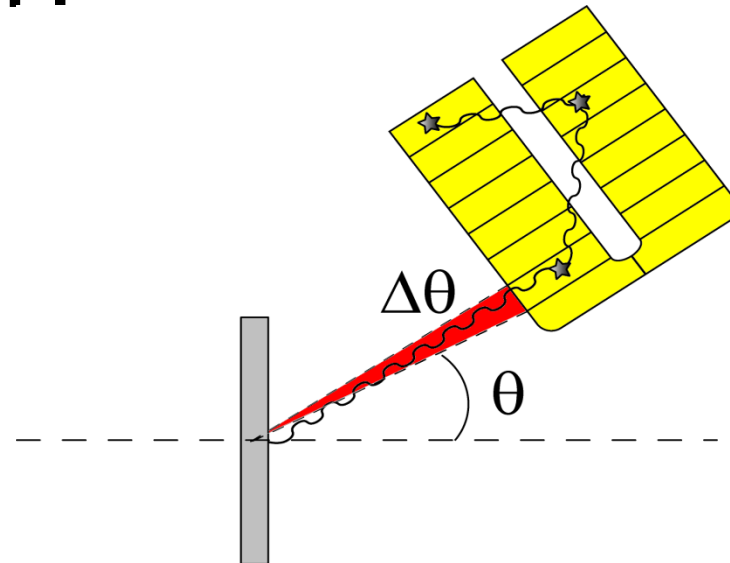
- By now: 9 modules with 4 crystals that are 36-fold segmented each (>1300 electronics channels)
- High segmentation and sub-segment position resolution through tracking of gamma-ray interactions inside the crystal



Why segmentation: Emission in flight \rightarrow Doppler shift!

$$E = E_0 \frac{\sqrt{1 - \beta_0^2}}{1 - \beta_0 \cdot \mathbf{e}}$$

$$\beta_0 \cdot \mathbf{e} = |\beta_0| \cos \theta_0$$



Example: SeGA geometry (NSCL)



E_0 γ -ray energy in the source frame

E γ -ray energy in the lab frame

β_0 velocity of the source

θ_0 γ -ray angle of emission

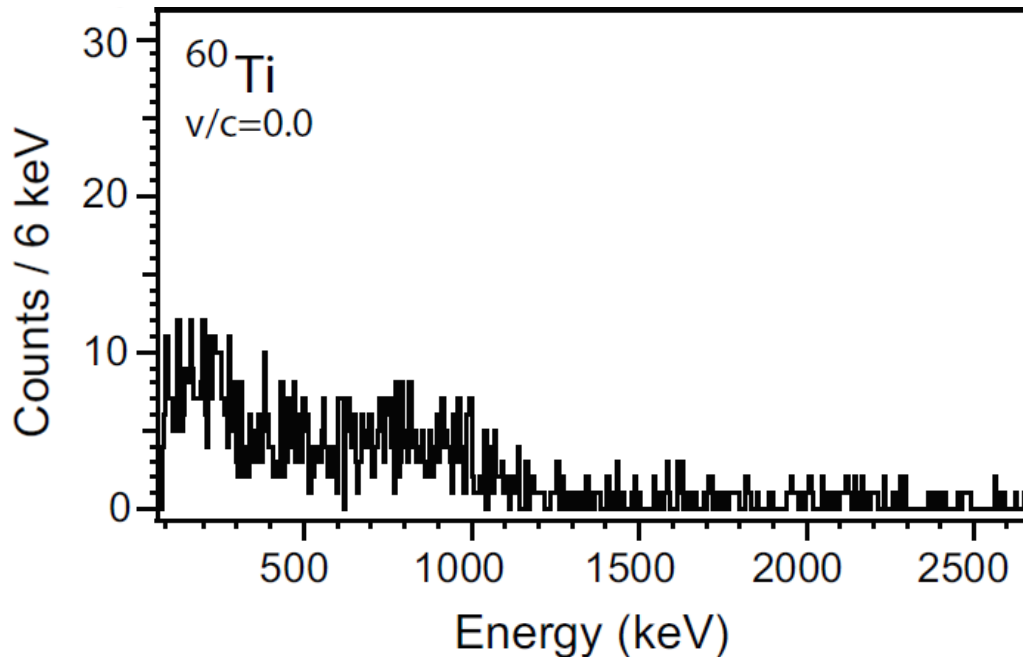
Details in the lecture by T. Lauritsen



Gamma-rays to tag the final state

A. Gade, Eur. Phys. J. A 51, 118 (2015) - review

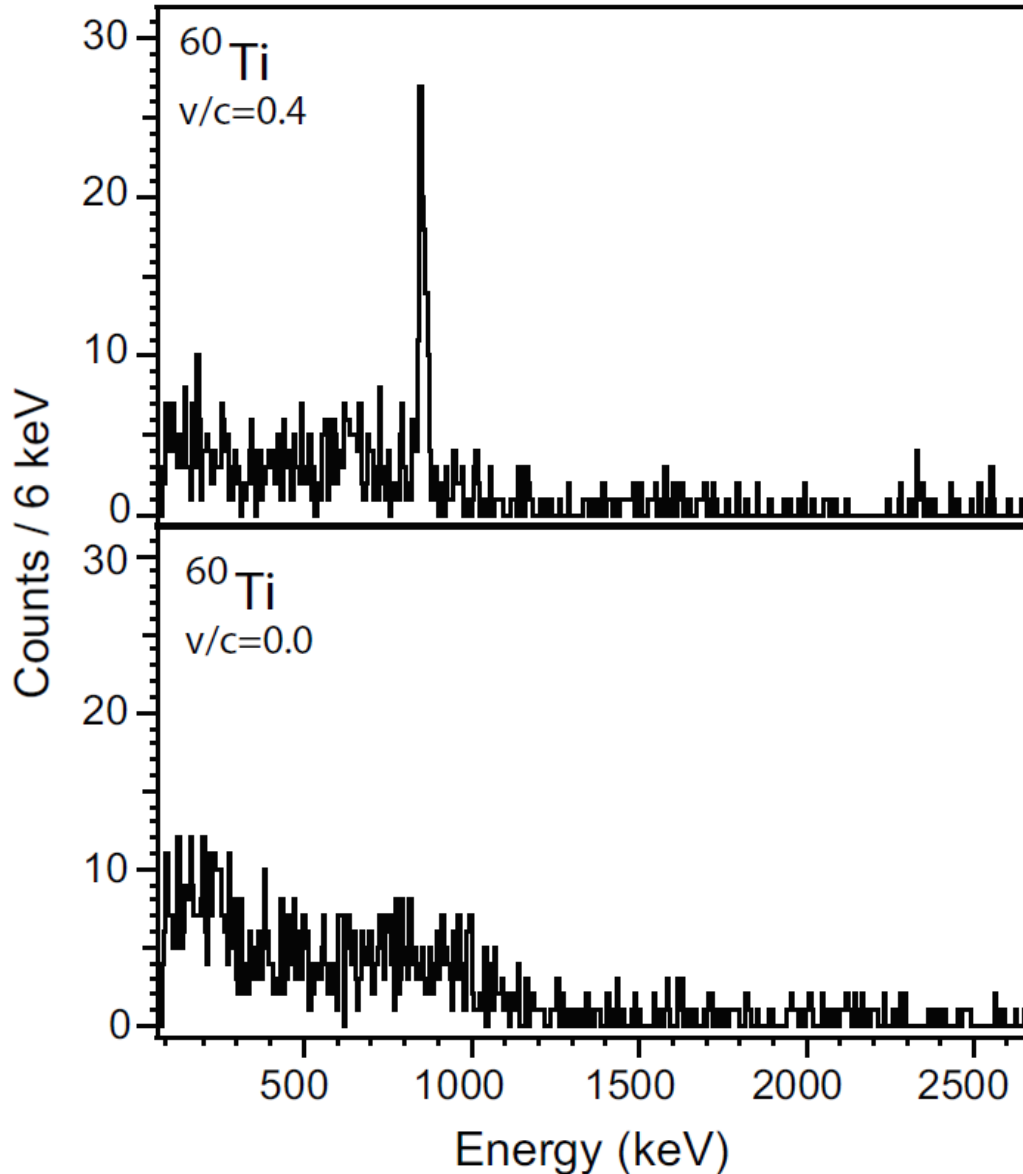
Making a histogram of
energies as measured in the
laboratory reference frame





Gamma-rays to tag the final state

A. Gade, Eur. Phys. J. A 51, 118 (2015) - review



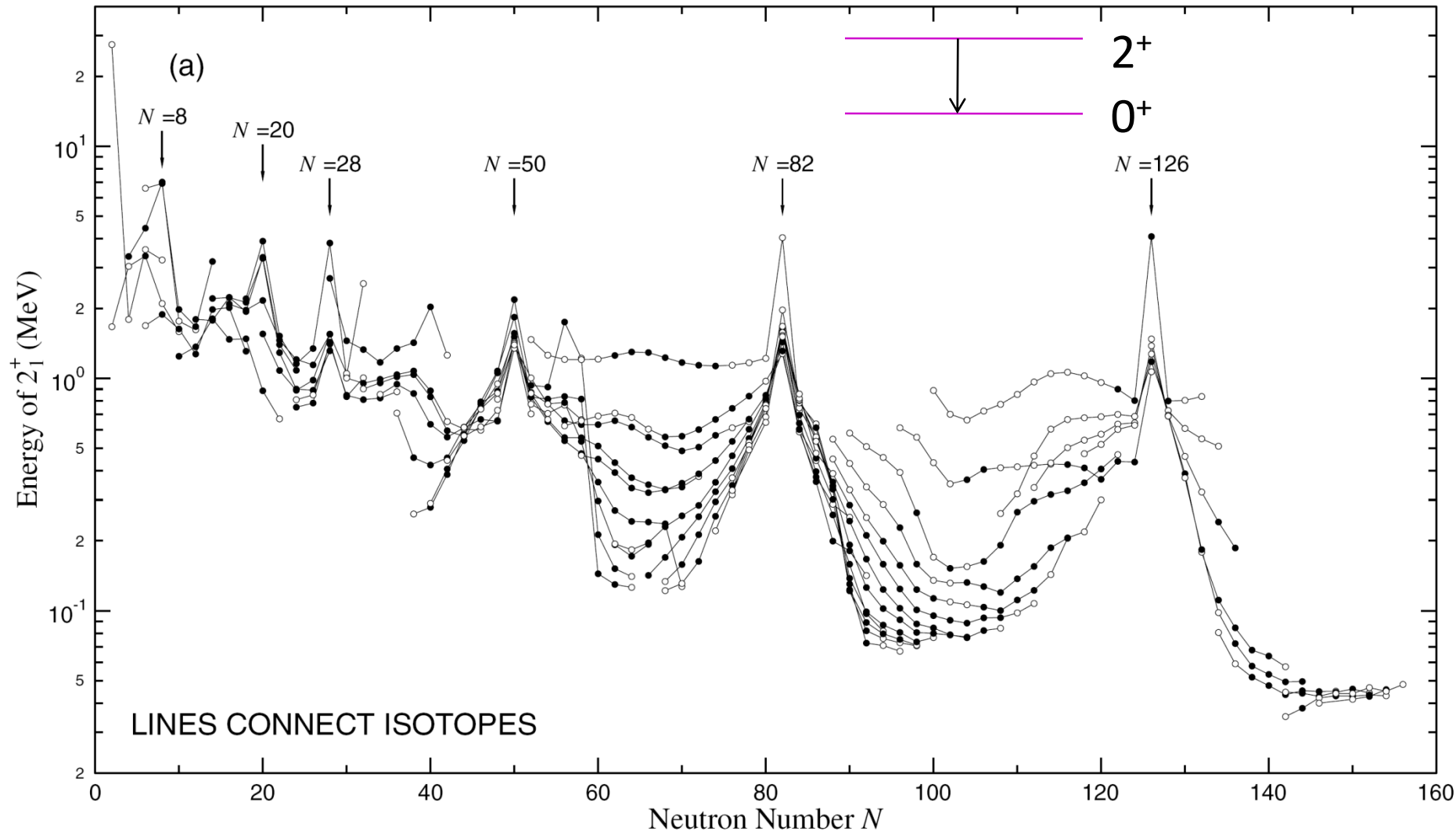
Event-by-event Doppler reconstructed using the rare isotope's velocity and the emission angle of the γ -ray



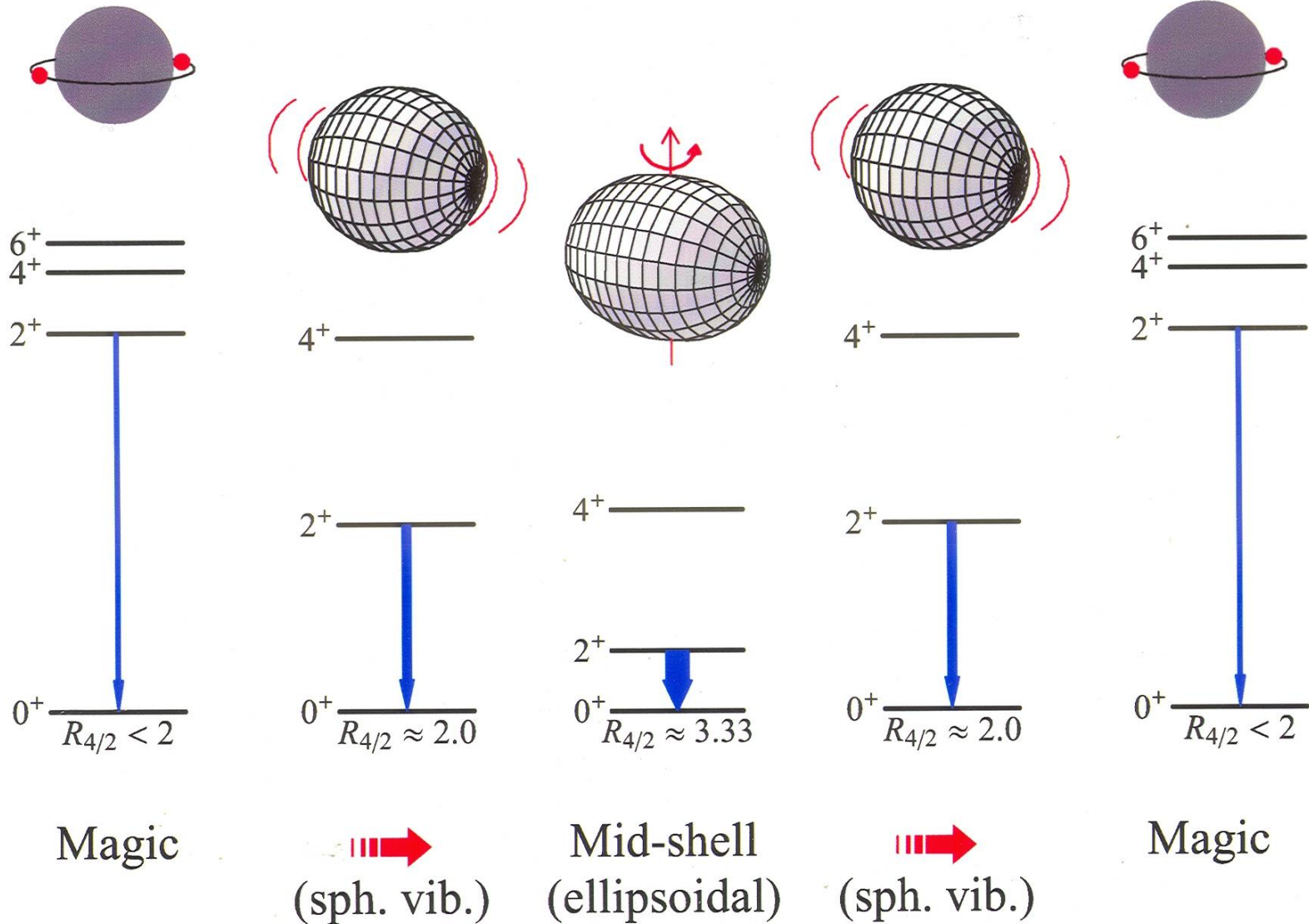
Collective excitations

Even-even nuclei: 2^+_1 state energy as an indicator of shell structure

S. Raman et al., Atomic Data & Nuclear Data Tables 78, 1

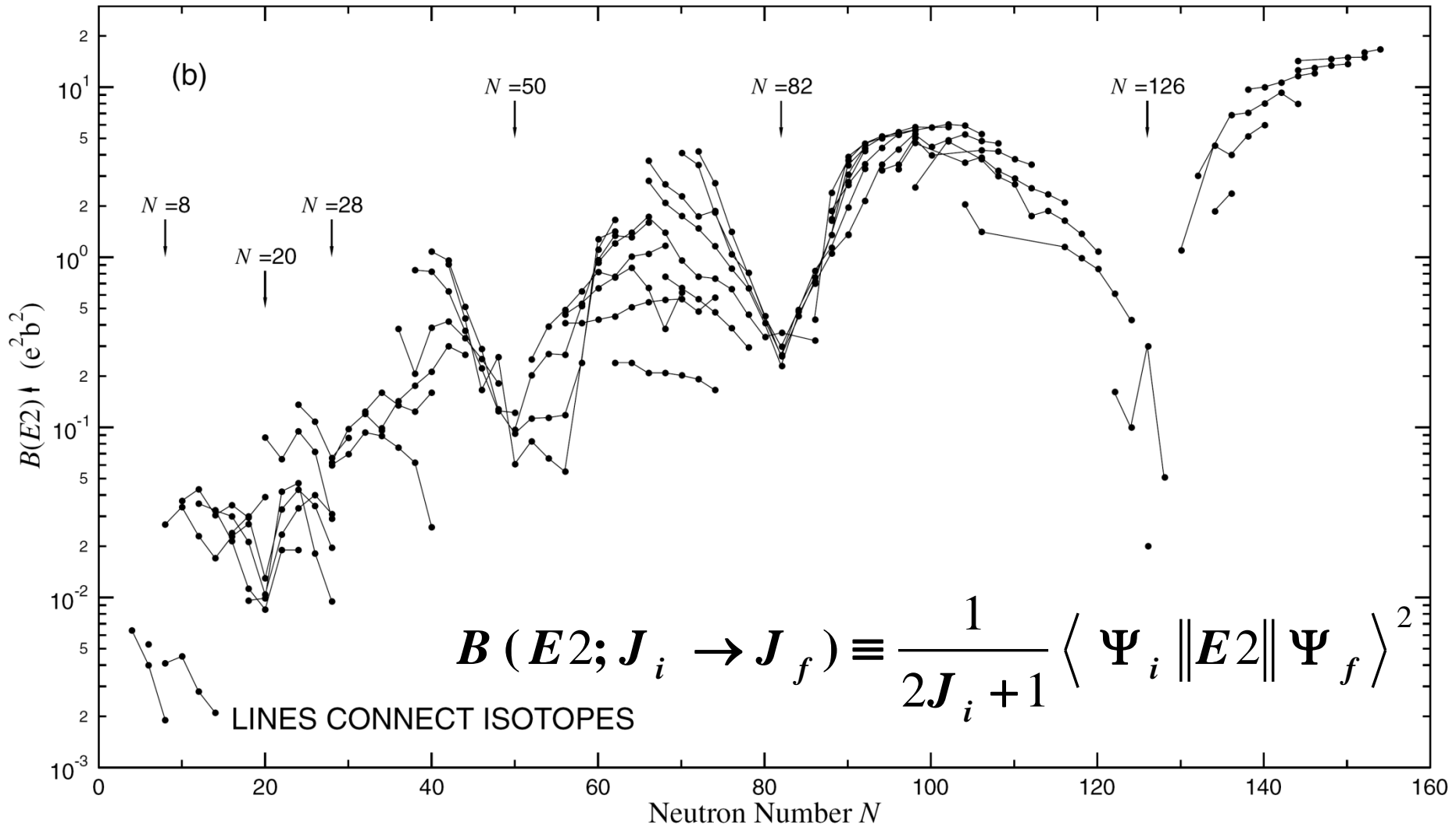


Even-even nuclei: 2^+ states are typically the first excited state on top of 0^+ ground states



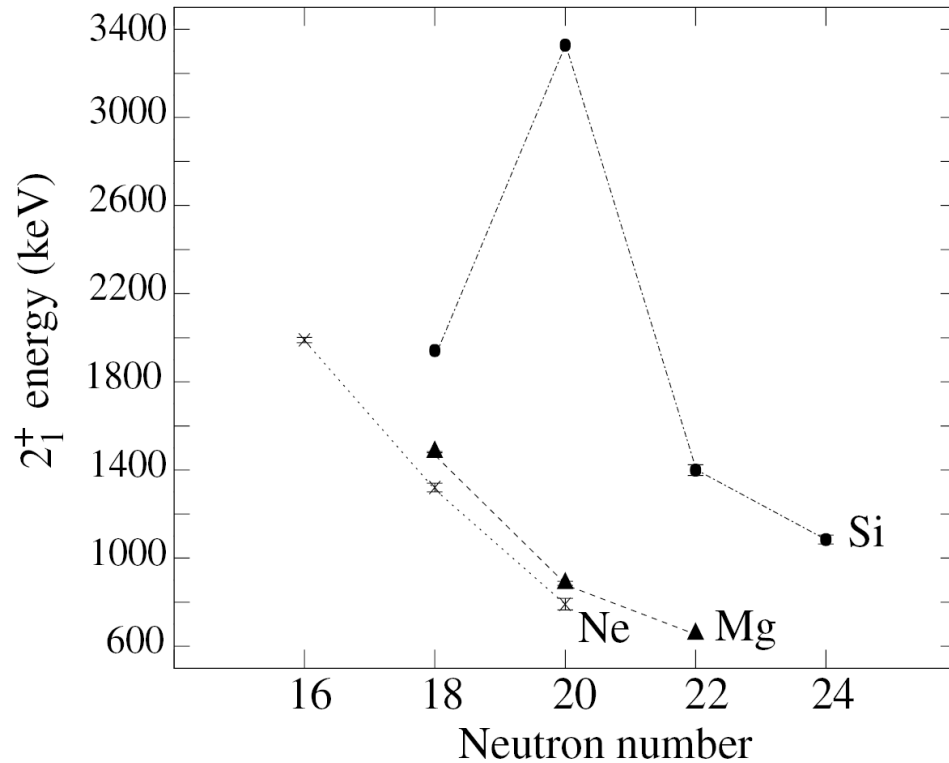
Even-even nuclei: 2^+_1 excitation strength as an indicator of shell structure

S. Raman et al., Atomic Data & Nuclear Data Tables 78, 1



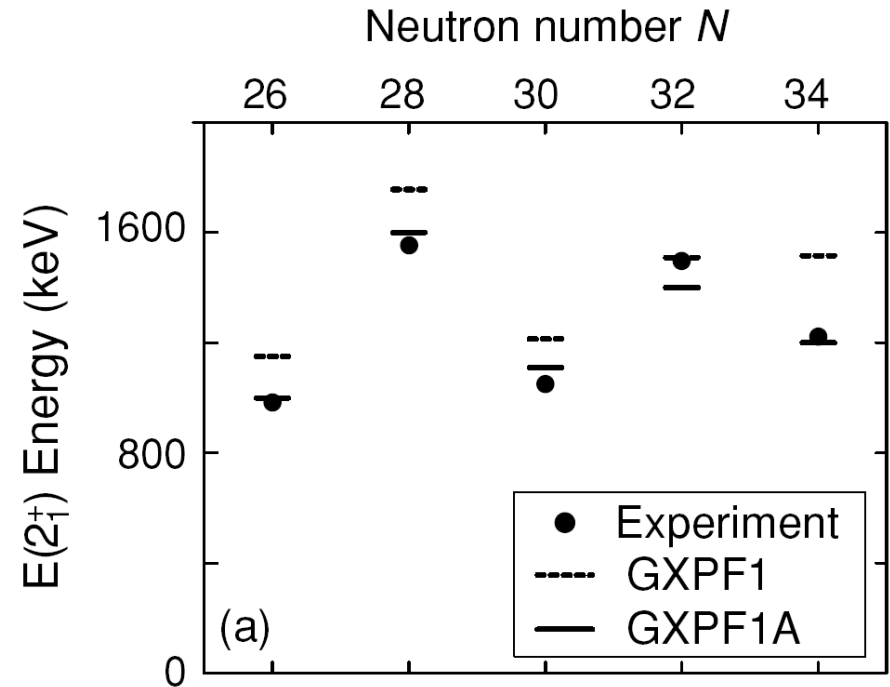
Examples of changes in shell structure

A. Gade and T. Glasmacher, Prog. In Part. and Nucl. Phys. 60, 161 (2008)

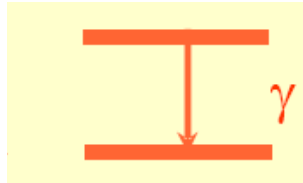
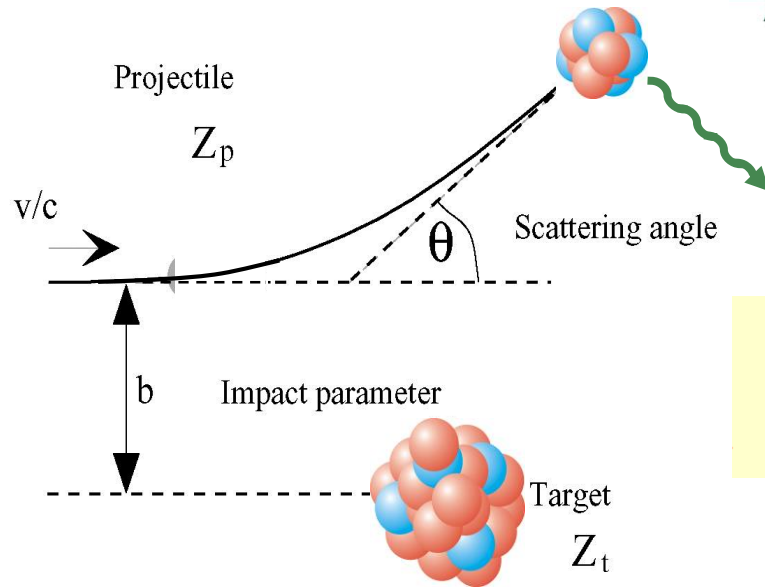
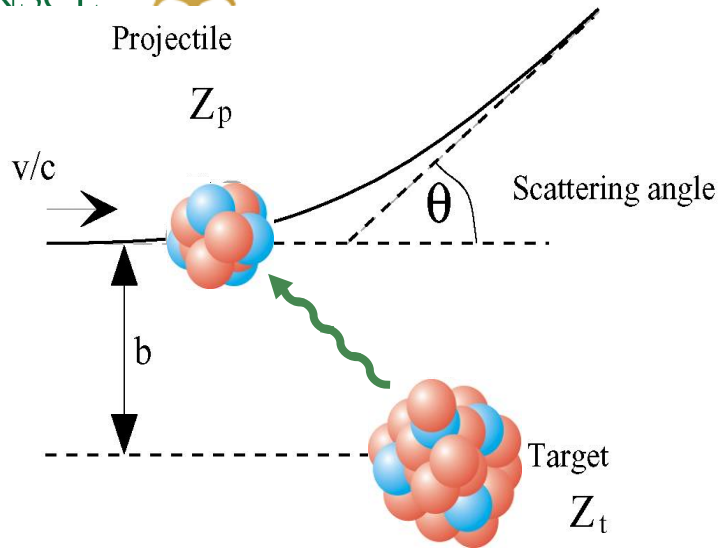


N=20 is not a good shell closure anymore in Mg and Ne isotopes

N=32 is a new magic number in the Ti isotopes



D.-C. Dinca et al., PRC 71, 041302 (2005)



Exchange of virtual photons mediates excitation

Measure de-excitation γ -rays

Beam energies at the Coulomb barrier
(SPIRAL):

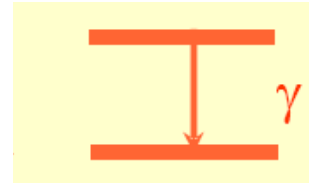
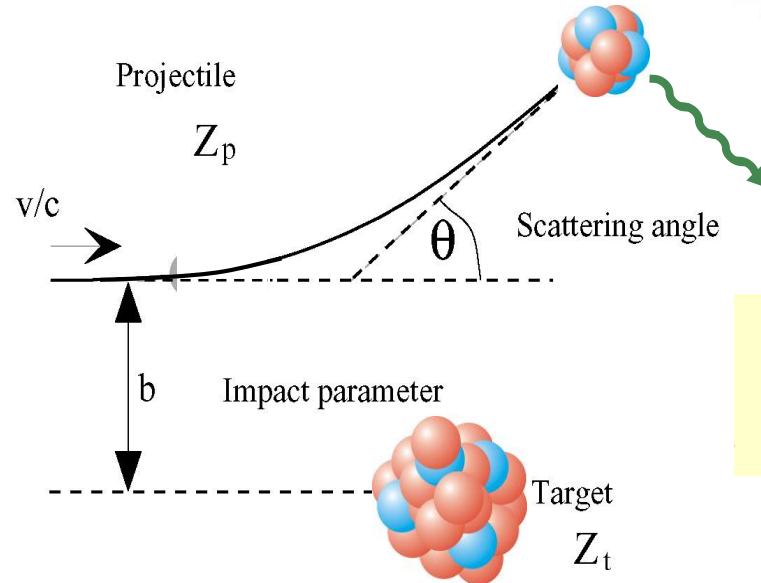
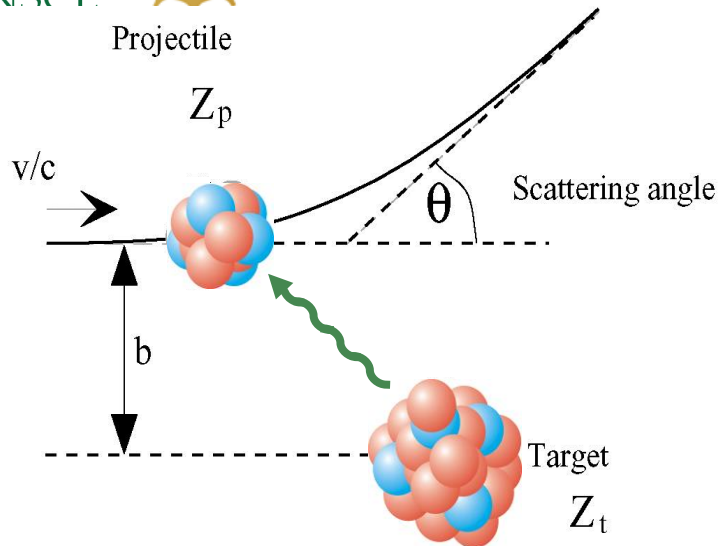
E_x , $B(\sigma\lambda)$ excitation strength, band structures
($0^+ \rightarrow 2^+ \rightarrow 4^+ \rightarrow 6^+$)

Beam energies well below the Coulomb barrier
(ISOLDE, HRIBF):

Usually only the first 2^+ state accessible

$$V_c(\text{MeV}) = \frac{1.44 \times Z_1 \times Z_2}{r(\text{fm})}$$

$$r(\text{fm}) \sim 1.2(A_1^{1/3} + A_2^{1/3})$$



Exchange of virtual photons mediates excitation

Measure de-excitation γ -rays

Intermediate and relativistic energies (NSCL, RIKEN, GANIL, GSI): $E(2^+_{11})$, $B(E2, 0^+ \rightarrow 2^+_{11})$ excitation strength, two-step to 4^+ heavily suppressed (short interaction time at high beam energies)

BUT: the collision between target and projectile happens above the Coulomb barrier for every target-projectile combination

How can this still be Coulomb excitation?

How can it be Coulomb excitation at energies above the Coulomb barrier ?!

At NSCL, RIKEN, GSI ... the collision between target and projectile happens above the Coulomb barrier for every target-projectile combination

But: electromagnetic interaction dominates for $b > R_{\text{int}}$

For given v/c :

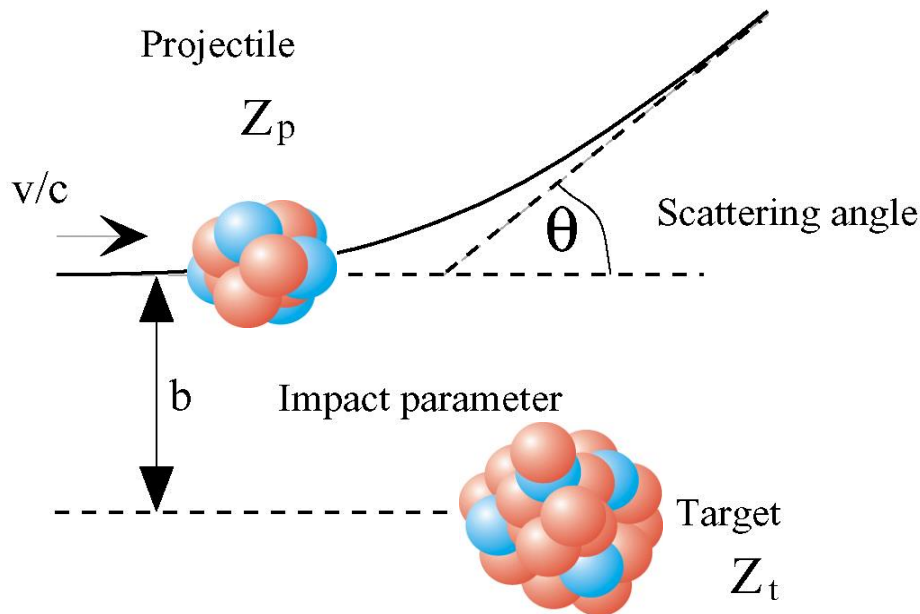
impact parameter $b = b(\theta)$

$$b_{\text{min}} = \frac{a}{\gamma} \cot(\theta_{\text{max}}^{\text{cm}}/2)$$

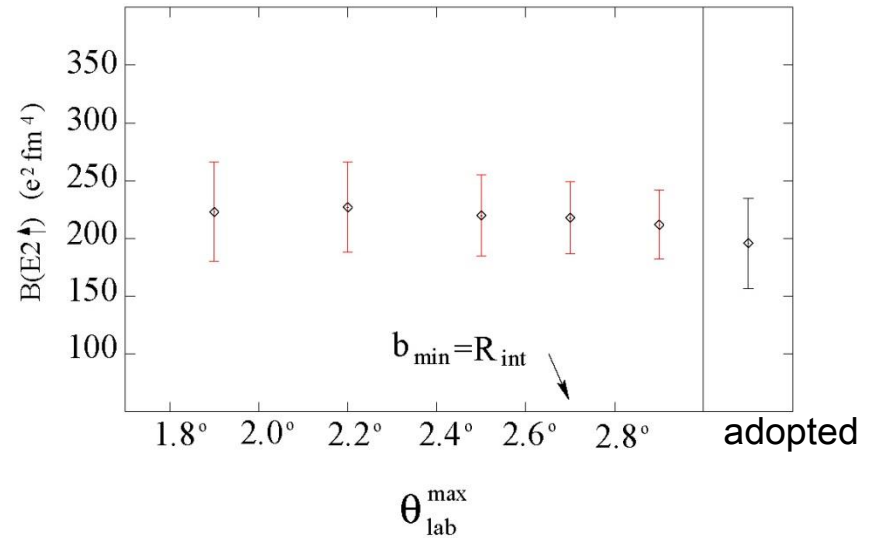
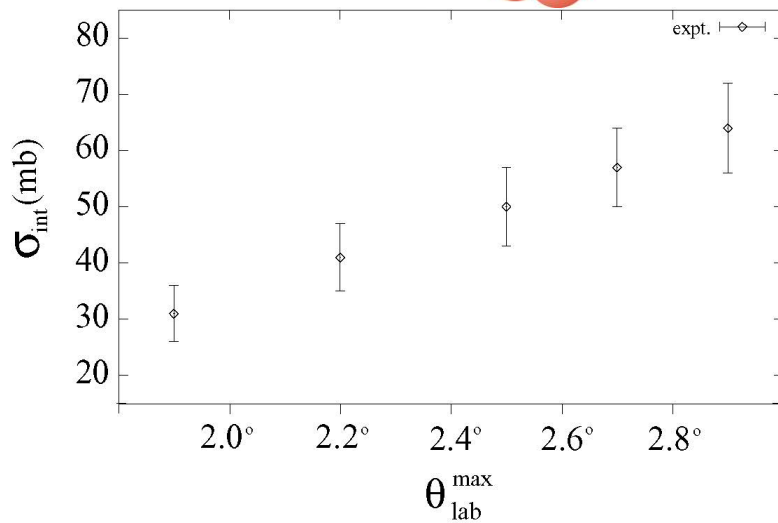
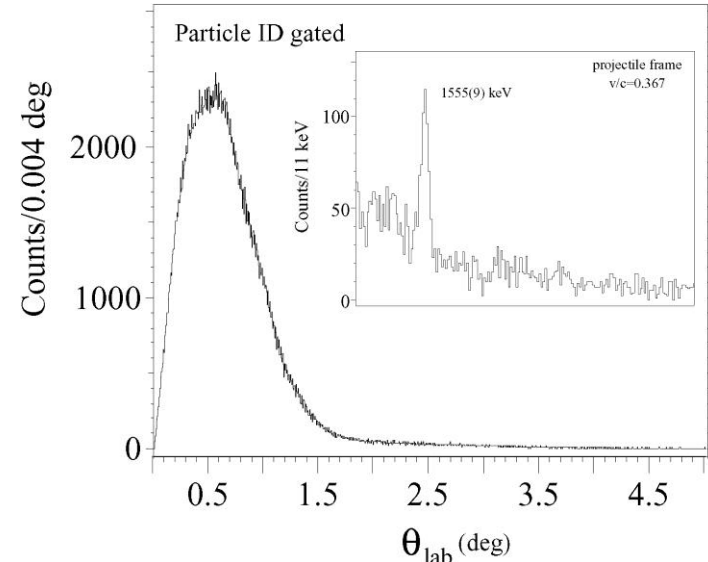
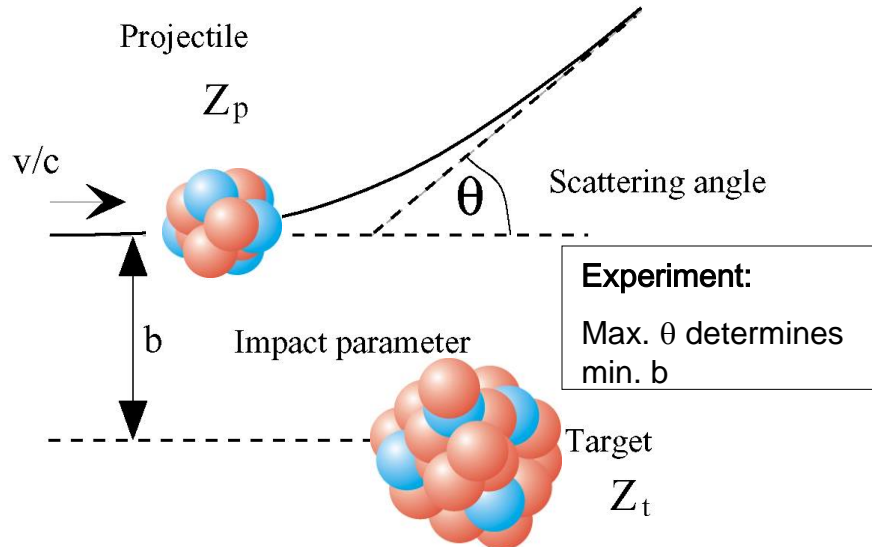
$$a = \frac{Z_p Z_t e^2}{\mu v^2}$$

Experiment:

Maximum scattering angle determines minimum b .
Restrict analysis to events at the most forward scattering angles so that $b(\theta) > R_{\text{int}}$



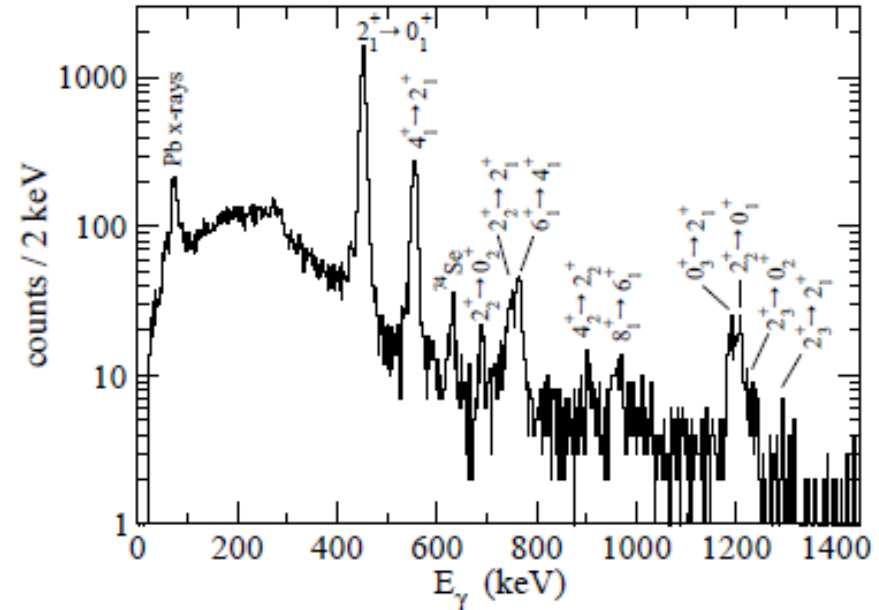
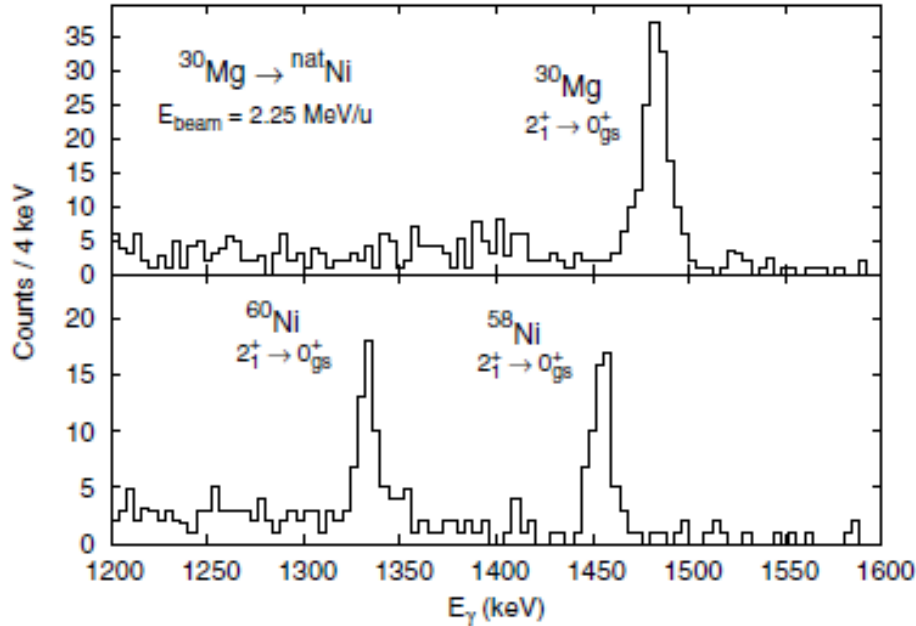
A. Gade *et al.*, PRC 68, 014302 (2003)



Low-energy Coulomb excitation

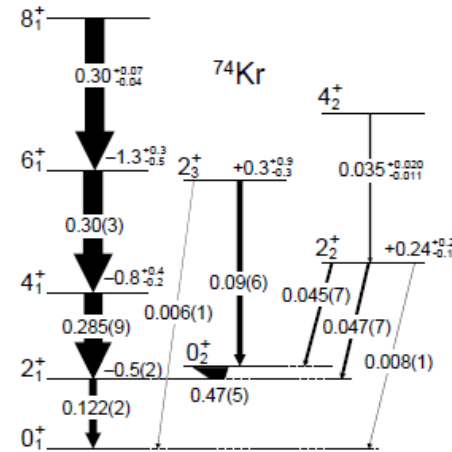
Example: $^{30}\text{Mg} + ^{58,60}\text{Ni}$ and $^{78}\text{Kr} + ^{208}\text{Pb}$

O. Niedermaier *et al.*, PRL 94, 172501 (2005)



^{30}Mg at **2.25 MeV/nucleon** on natural Ni target
(1.0 mg/cm²)
From REX-ISOLDE at CERN
 γ -ray detection with MINIBALL.
Particle detection with CD-shaped double-sided Si strip detector

$$\frac{\sigma_{\text{CE}}(^{30}\text{Mg})}{\sigma_{\text{CE}}(^{58,60}\text{Ni})} = \frac{\epsilon_{\gamma}(^{58,60}\text{Ni})}{\epsilon_{\gamma}(^{30}\text{Mg})} \frac{W_{\gamma}(^{58,60}\text{Ni})}{W_{\gamma}(^{30}\text{Mg})} \frac{N_{\gamma}(^{30}\text{Mg})}{N_{\gamma}(^{58,60}\text{Ni})}$$

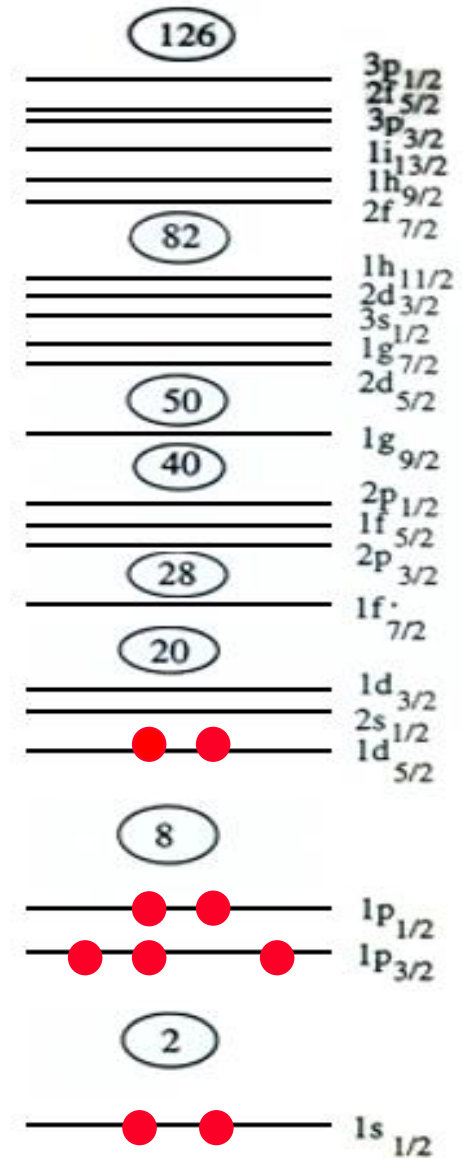
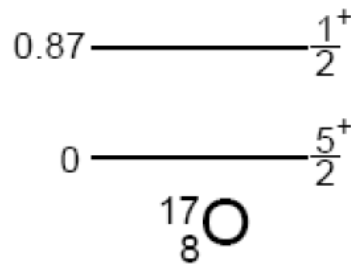
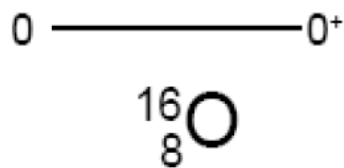
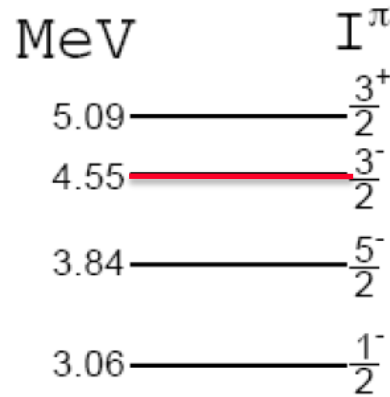
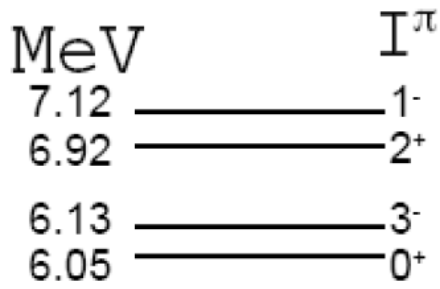


^{74}Kr multistep
Coulomb excitation at **4.7 MeV/u**
on 1 mg/cm² ^{208}Pb target at
GANIL.
Data analysis done in a χ^2 minimization
with a coupled channels code
(GOSIA)



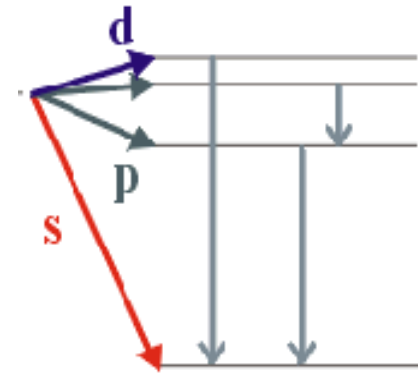
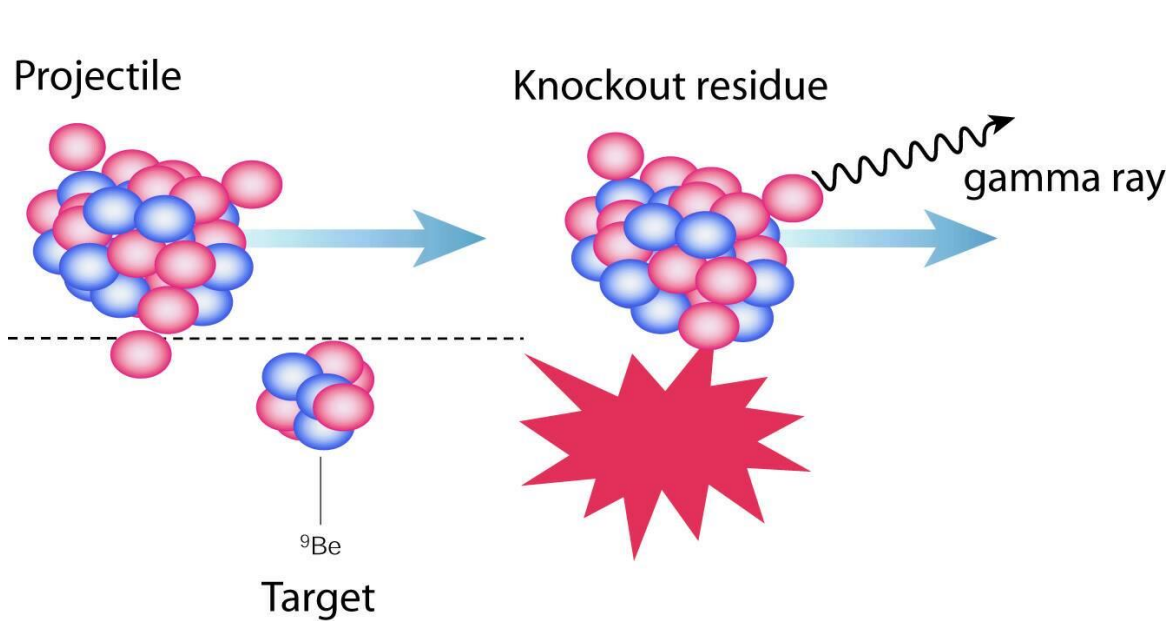
Single-particle states

Excited states in nuclei with one nucleon outside a magic number



One-nucleon knockout *A direct reaction*

- **more than 50 MeV/nucleon:**
Straight-line trajectories

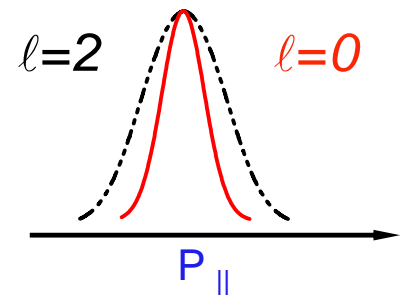


residue moment distribution
→ l -value of knocked-out n

P.G. Hansen, PRL 77, 1016 (1996)

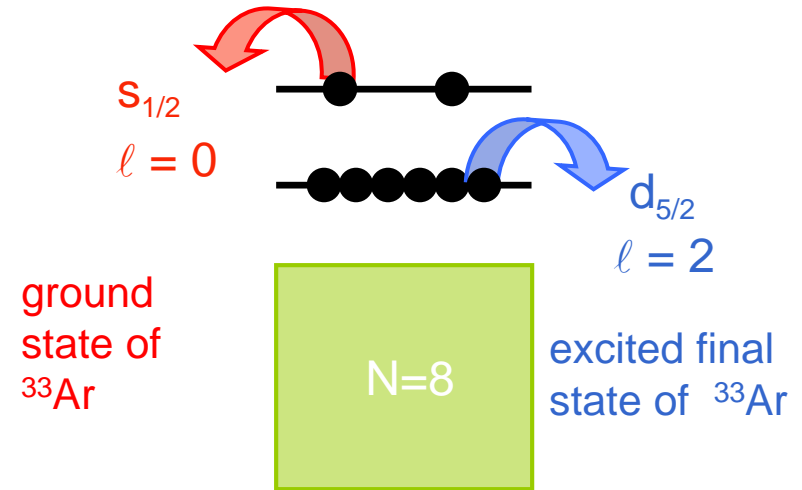
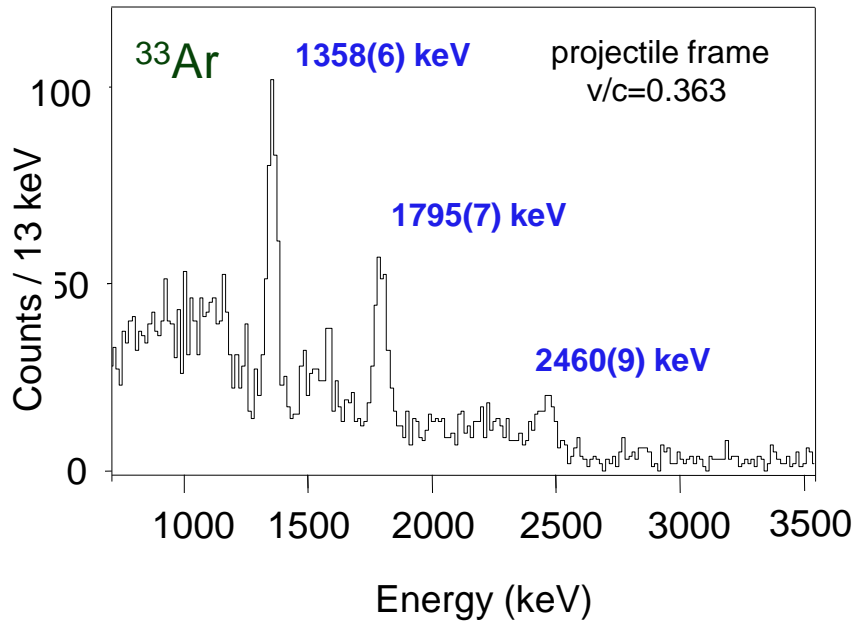
$$\sigma(nl^\pi) = C^2 S(j, nl^\pi) \sigma_{sp}(j, S_n)$$

nucleons in orbit
reaction cross section

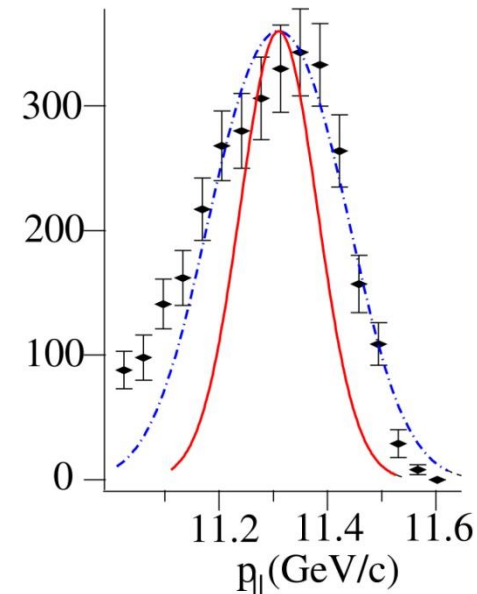
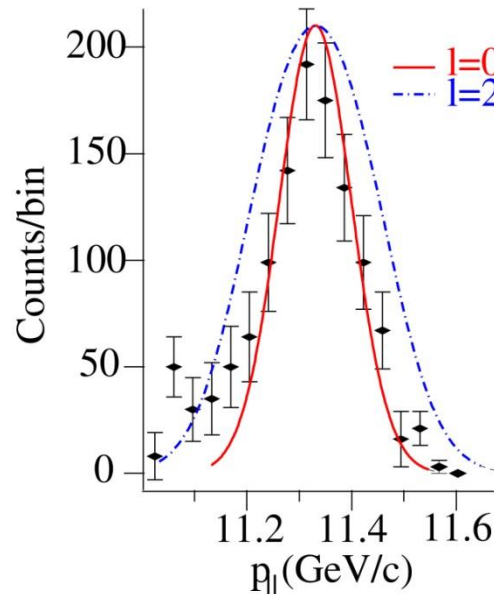


Spectroscopy in one-nucleon knockout

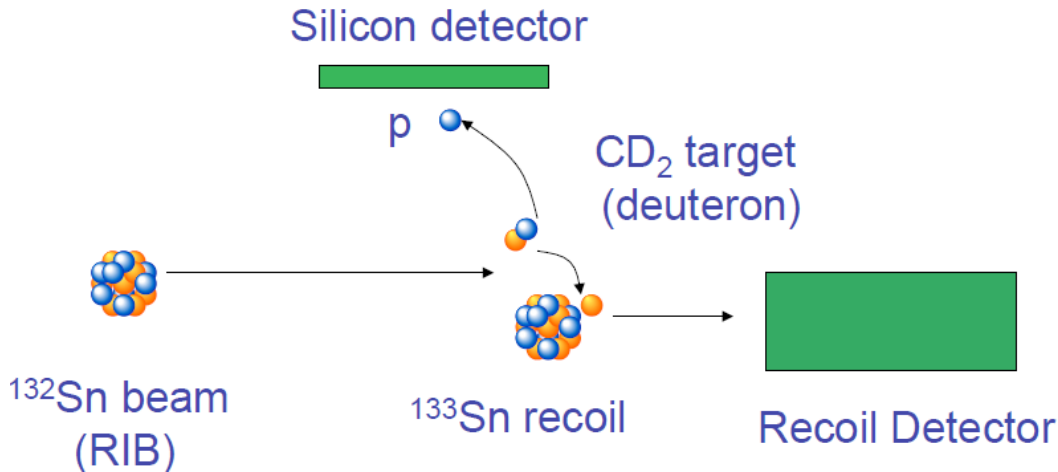
Example: ${}^9\text{Be}({}^{34}\text{Ar}, {}^{33}\text{Ar})X$



	BR (%)	σ_{exp} (mb)	C^2S_{exp}
$1/2^+$	30.2(46)	4.7(9)	0.38(6)
$3/2^+$	20.2(44)	3.2(8)	0.36(9)
$5/2^+$	31.7(31)	4.9(7)	0.56(8)
$(5/2^+)$	17.9(30)	2.8(6)	$>0.34(7)$

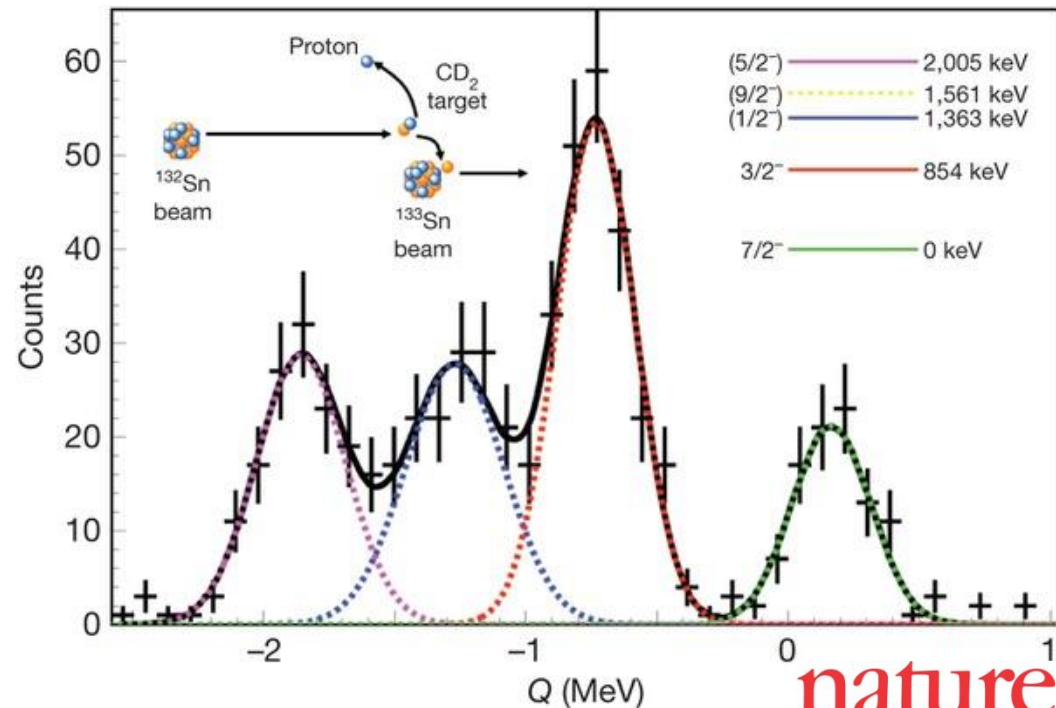


Low-energy transfer reactions – $^{132}\text{Sn}(d,p)^{133}\text{Sn}$ at HRIBF



Q-value spectrum for the $^{132}\text{Sn}(d,p)^{133}\text{Sn}$ reaction at 54° in the centre of mass.

- 4.77 MeV/u ^{132}Sn produced and accelerated at HRIBF bombarded a $160\mu\text{g}/\text{cm}^2$ CD_2 target. Exit-channel proton detection with ORRUBA Si strip detectors under $69\text{-}107^\circ$ polar angles





Lifetimes of excited states

*Can provide information on
collective and single-particle
degrees of freedom*

Lifetimes of excited 2^+ states in even-even nuclei: picosecond range

$$\tau_{\gamma} = 40.81 \times 10^{13} E^{-5} [B(E2)_{\uparrow}/e^2b^2]^{-1}$$

Some excited states live much longer: Isomers

Table I: Examples of extreme isomers

Nuclide	Half-life	Spin (\hbar)	Energy	Attribute
^{12}Be	~500 ns	0	2.2 MeV	low mass
^{94}Ag	300 ms	21	6 MeV	proton decay
^{152}Er	11 ns	~36	13 MeV	high spin and energy
^{180}Ta	$>10^{16}$ y	9	75 keV	long half-life
^{229}Th	~5 h	3/2	~7.6 eV	low energy
^{270}Ds	~6 ms	~10	~1 MeV	high mass

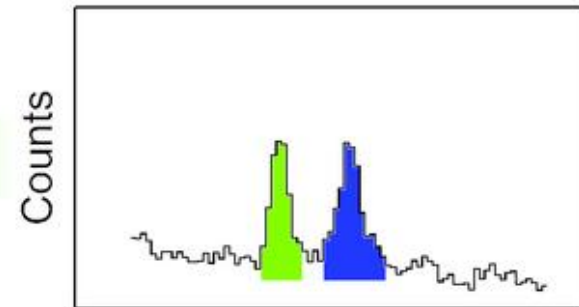
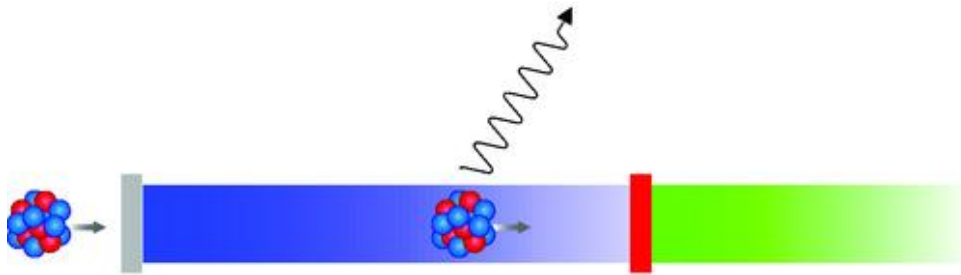
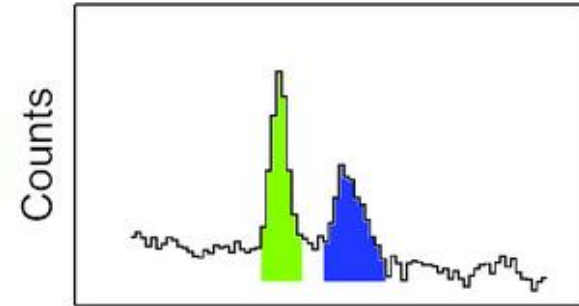
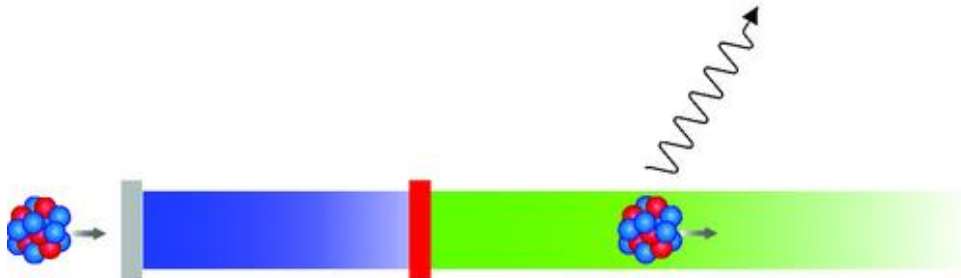
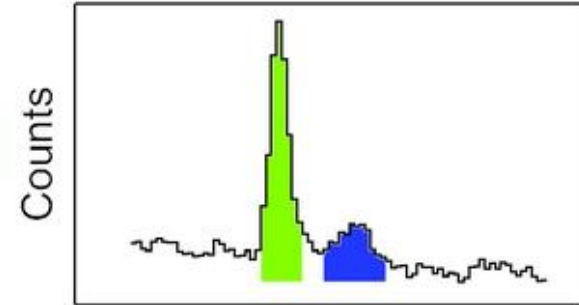
From P.M. Walker and J. J. Carroll, Nuclear Physics News 17, 11-15 (2007)

$c=300 \mu\text{m/ps}$

$\beta \sim 0.3c$

10 ps ~ 1mm

Target Degraded

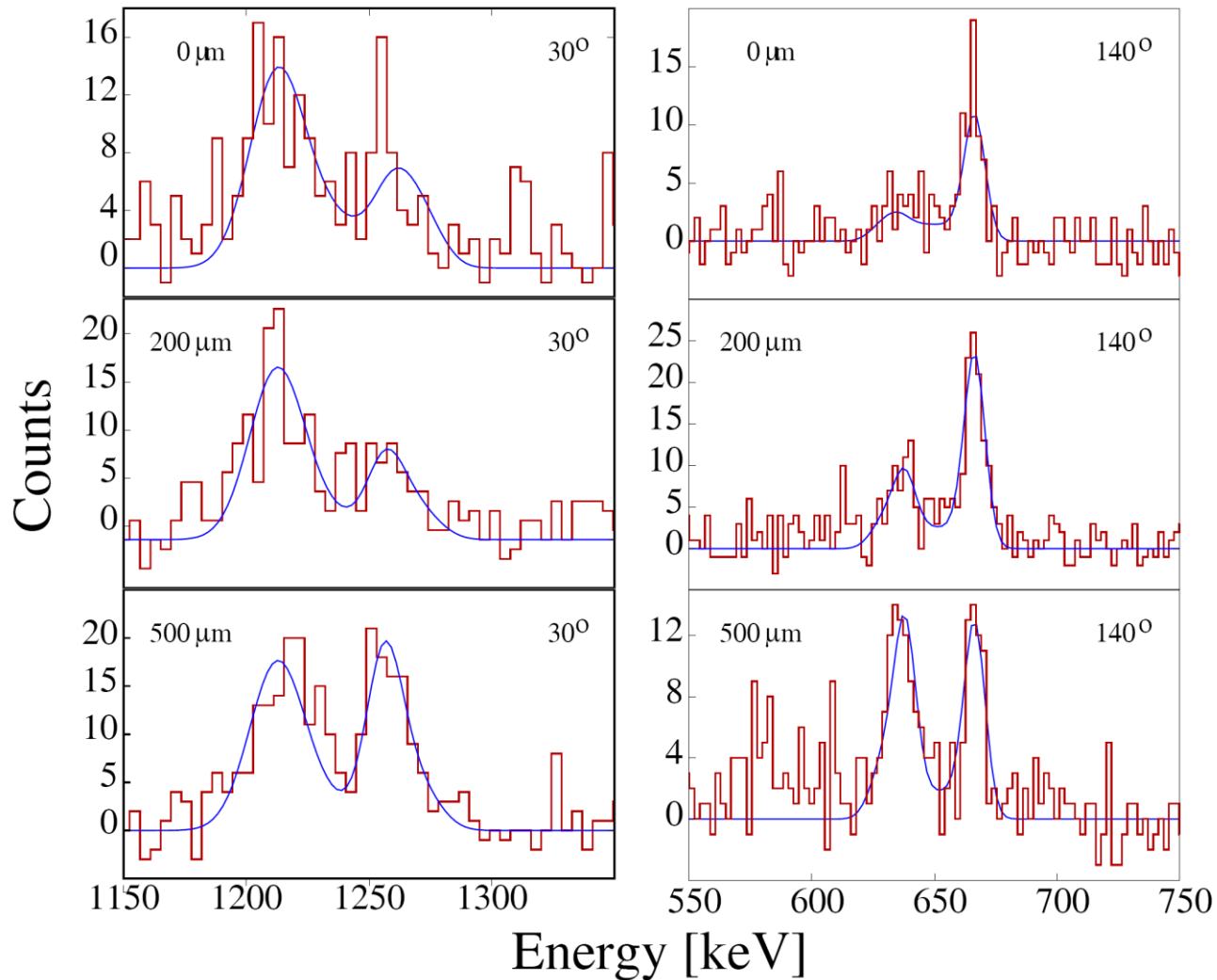


Energy

Line shapes and lifetimes

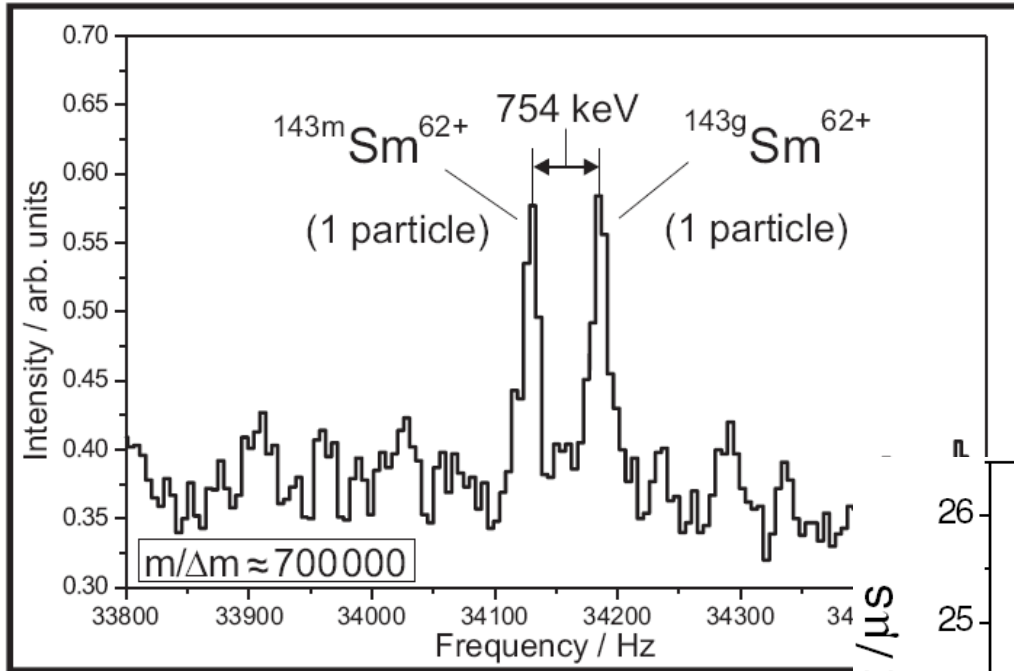
Example: $^{64}\text{Ge } 2^+_1 \rightarrow 0^+_1$

$\tau = 3.2(5)$ [ps]



Long-lived excited states – isomers

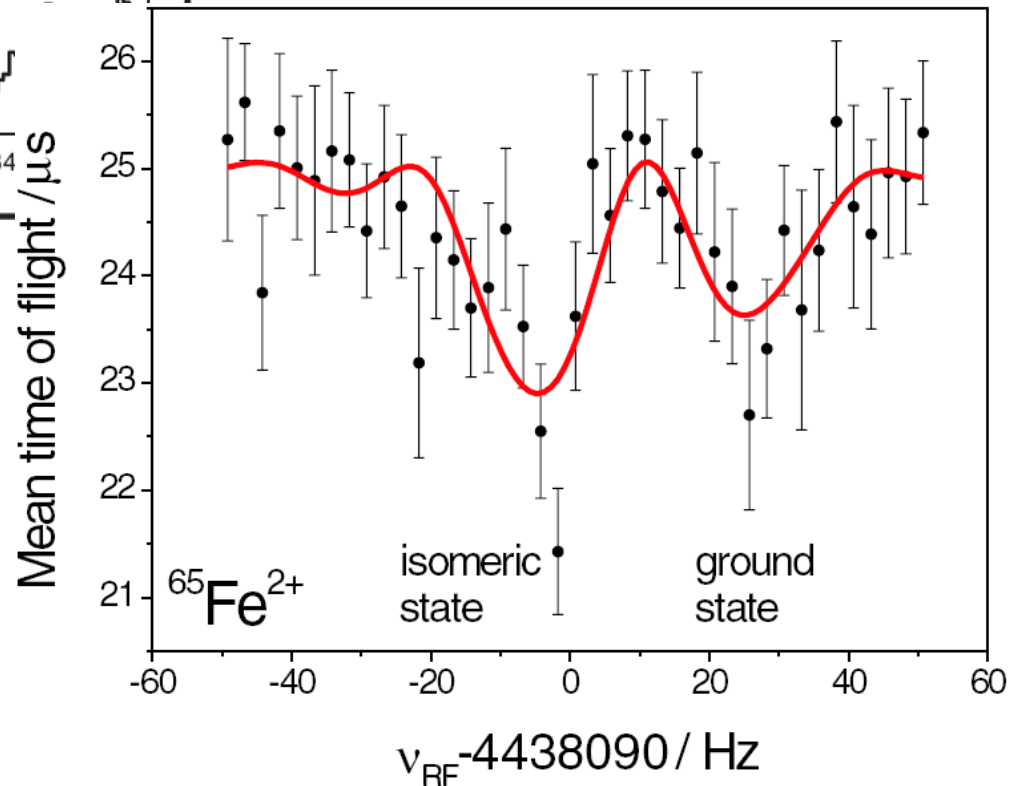
Back to storage rings and penning traps



M. Block et al., PRL 100, 132501 (2008)

F. Bosch, Lect. Notes Phys. 651, 137(2004)

Isomers: decay hindered by nuclear structure (selection rules, energy, ...) → long lifetime





Take away

- Excited states provide valuable information on the evolution of nuclear structure
 - Population of excited states in various schemes
- Reactions – powerful tools
 - Observables related to the collective degree of freedom
 - Single-particle structure from direct reactions
- Life-times of excited states
 - Different experimental approaches