Physics Review

- Ø Newtonian Mechanics
 - @ Gravitational vs. Electromagnetic forces
 - Lorentz Force
- Maxwell's Equations
 - 💿 Integral vs. Differential
- @ Relativity (Special)

Newtonian Mechanics

v = dx/dt
p = mv
F = dp/dt
dW = F ds
F_g = G Mm/r² [F_e = 1/4πε₀ Qq/r² F_b = qv x B, etc.]
The Simple Harmonic Oscillator + Phase Space

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Simple Harmonic Motion

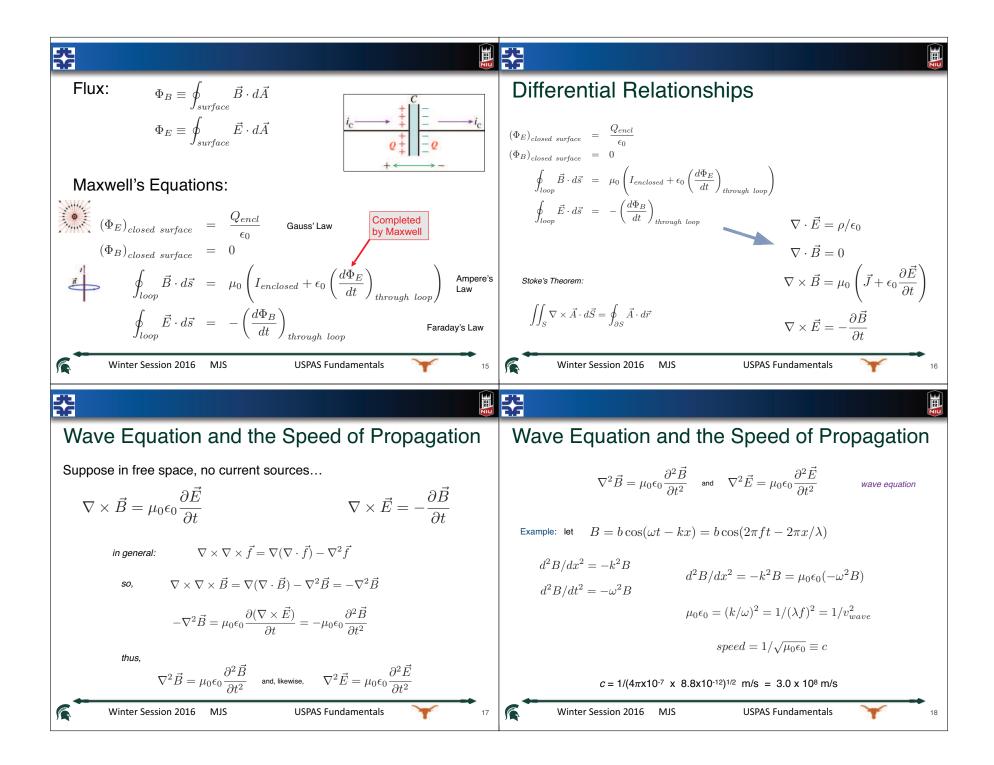
 $\ddot{x} = -kx \qquad \ddot{x} + kx = 0$ $x = a\sin(\omega t) + b\cos(\omega t) = c\sin(\omega t + \delta)$ $\dot{x} = c\omega\cos(\omega t + \delta)$ $\ddot{x} = -c\omega^{2}\sin(\omega t + \delta) = -\omega^{2}x$ $\omega = \sqrt{k}$ $x^{2} + \frac{1}{\omega^{2}}\dot{x}^{2} = c^{2}$ $\overset{\dot{x}}{\longrightarrow} x \text{ ellipse}$ $x^{2} + (\dot{x}/\omega)^{2} = c^{2}$ $\overset{\dot{x}}{\longrightarrow} x \text{ circle}$ Winter Session 2016 MJS USPAS Fundamentals

Maxwell's Equations

Integral Form

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- Ø Differential Form
- One Consequence: EM Waves
 - 𝐼 speed of waves given by c = $(\mu_0 ∈_0)^{-1/2}$
- Another Consequence:
 - S If μ₀, ε₀ are fundamental quantities, same in all reference frames, then so should be the speed of light!

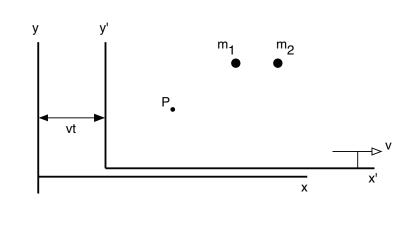


Maxwell's Equations

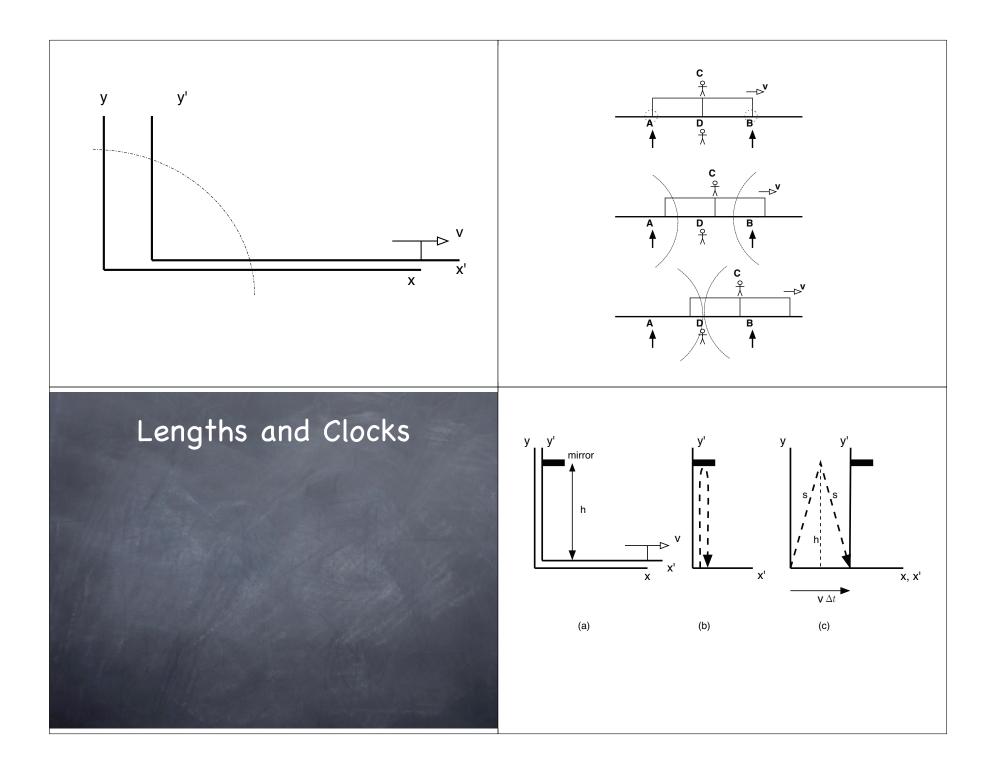
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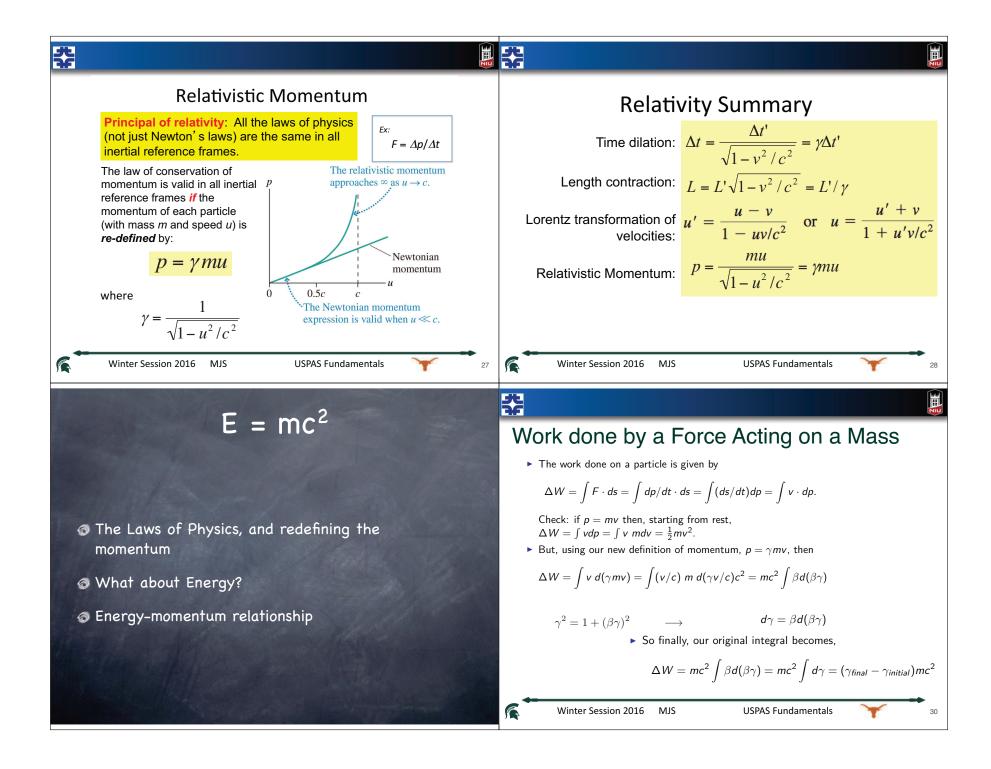
Special Relativity

- The Principle of Relativity
 - The Laws of Physics same in all inertial reference frames
- The Problem of the Velocity of Light
- Simultaneity
- Lengths and Clocks
- [⊘] E=mc²
- Ø Differential Relationships



Simultaneity





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• The previous equation tells us that as we do work on a particle its energy will change by an amount $\Delta E = \Delta W = \Delta \gamma mc^2$. Thus, the energy of a particle should be defined as

$$E = \gamma mc^2$$
.

 If the particle starts from rest, then γ_{initial} = 1, and its energy is E = mc². As it speeds up its kinetic energy will be

$$KE = \Delta W = (\gamma - 1)mc^2$$
, where here $\gamma \equiv \gamma_{final}$.

So we see that the energy is a combination of a "rest energy" and a "kinetic energy":

$$E = \gamma mc^2 = mc^2 + (\gamma - 1)mc^2$$

If no work were done ($\Delta W = 0$), and the particle were still at rest, the particle would *still* have energy (rest energy):

$$E_0 = mc^2 \rightarrow \text{mass is energy!}$$

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USPAS Fundamentals

Speed, Momentum, vs. Energy

gamma - 1 gamma - 1 Kinetic Energy Kinetic Energy Electron: 0 0.5 1.0 1.5 MeV Proton: 0 1000 2000 3000 MeV

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