John Barnard Steven Lund USPAS June 13-24, 2011 Melville, NY

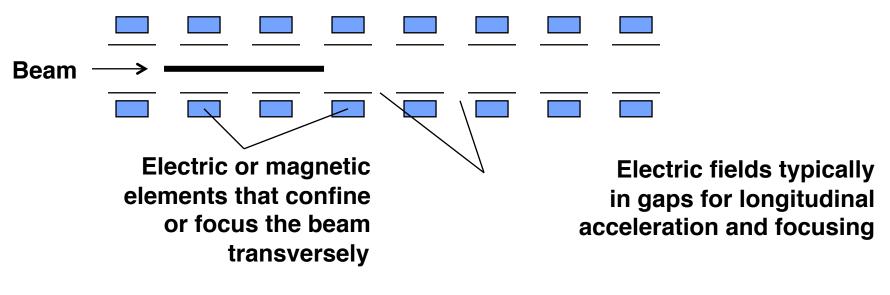
I. <u>Introduction</u> (related reading in parentheses)

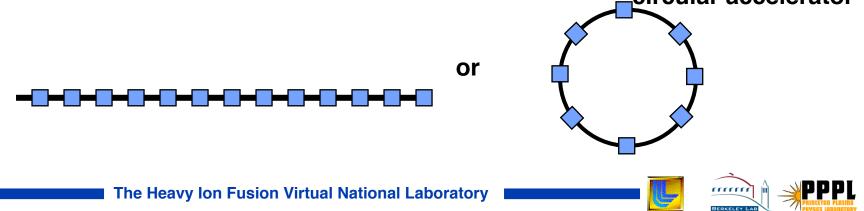
> Particle motion (Reiser 2.1) Equation of motion (Reiser 2.1) Dimensionless quantities (Reiser 4.2)

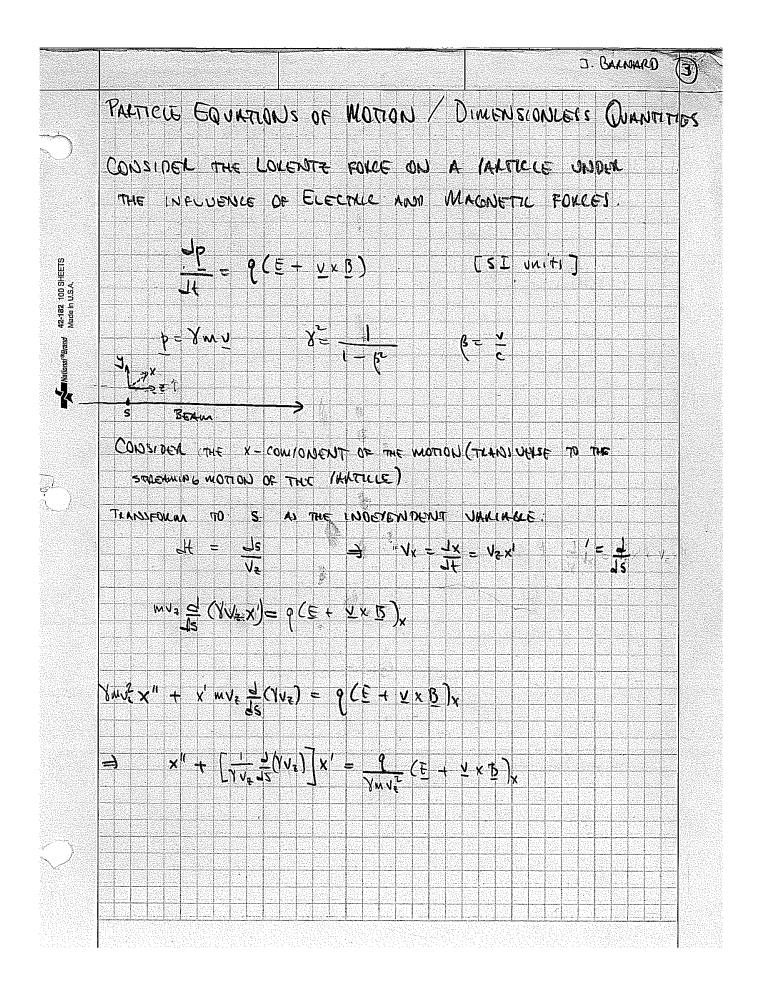
Plasma physics of beams (Reiser 3.2, 4.1)

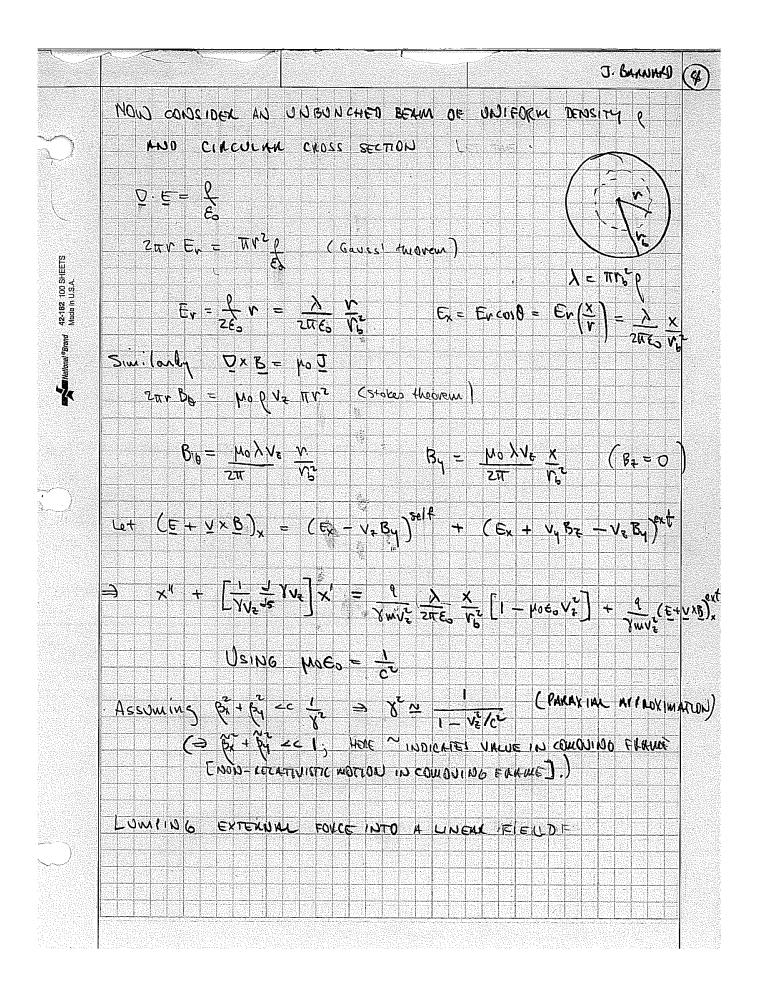
Emittance and brightness (Reiser 3.1 - 3.2)

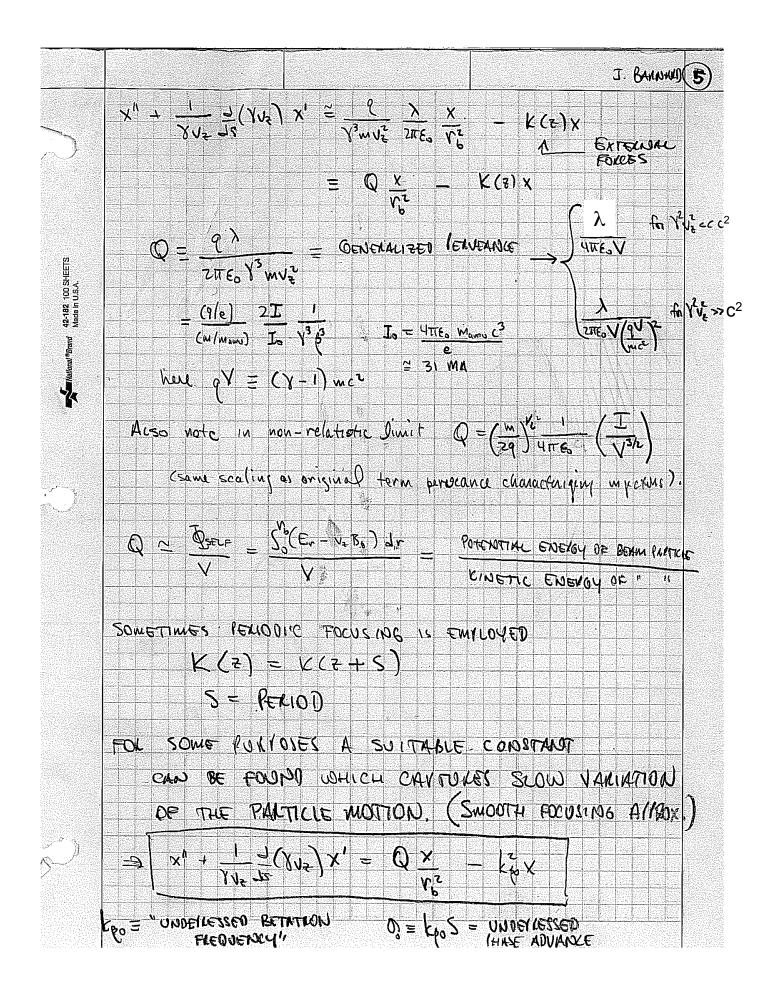
How do we describe and calculate the evolution of a collection of particles under the EM forces in an accelerator?

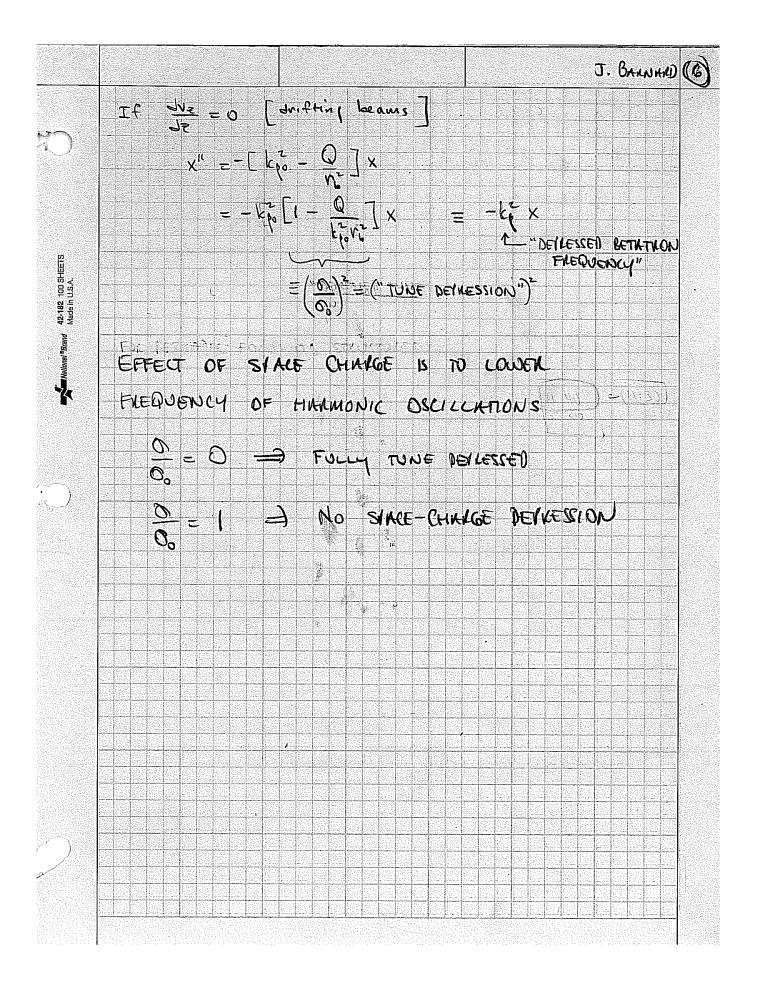




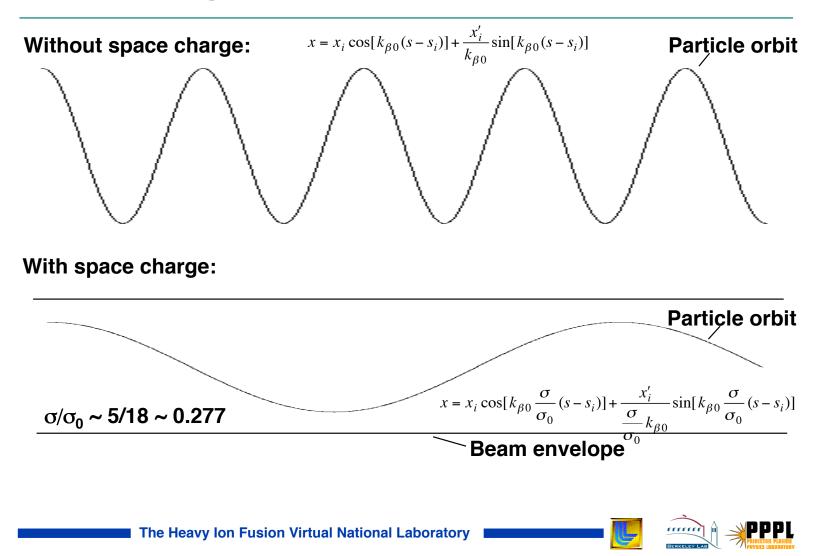


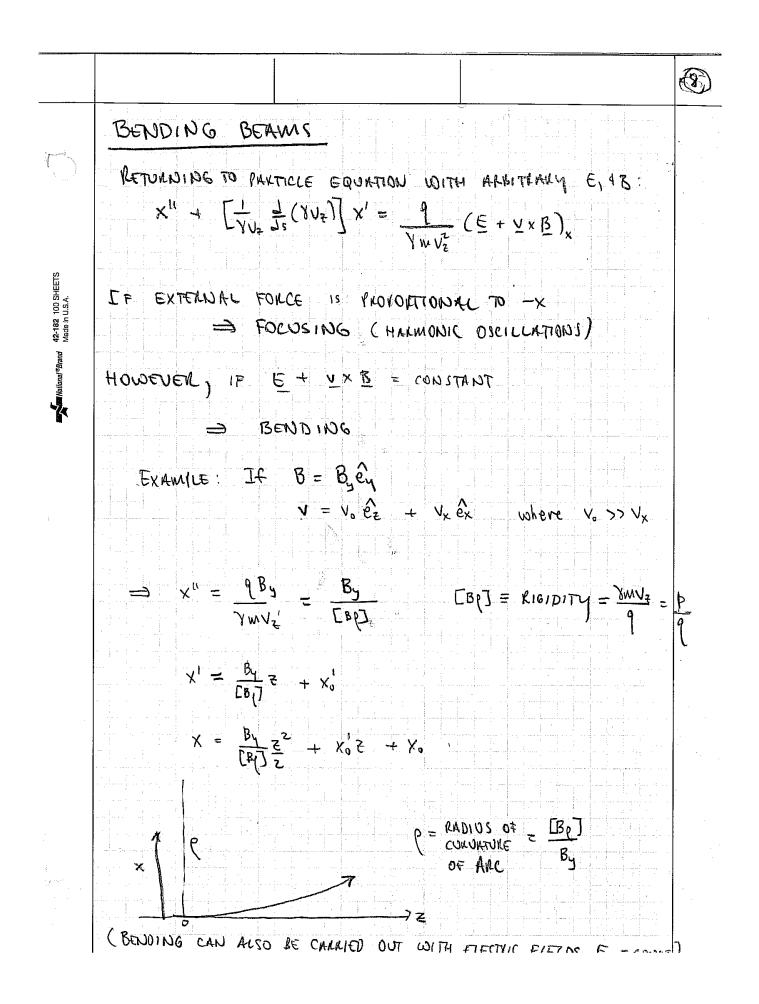






Space charge reduces betatron phase advance





PLASMA PHYSICS OF BEAMS

PHYSICS OF STACE CHARGE = (HYSICI OF SELF FIELDS = (LAIMA (HYSIC) OF (ALTICLE TSEAMS

PLASMA PARAMETER
$$\Lambda$$

 $2 \overline{I}_{IP} = \frac{1}{4\pi\epsilon_0} \frac{q^2}{V_{IP}}$

$$\sim \frac{1}{4\pi\epsilon_0} N_0^{\prime\prime} q^2$$

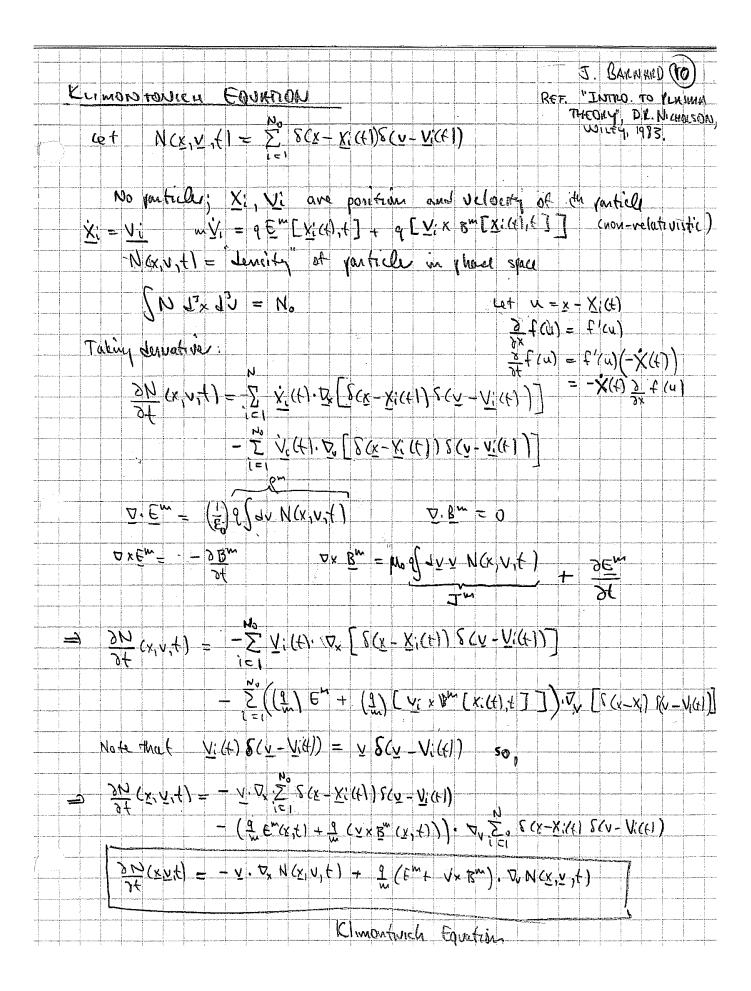
AVERAGE YOTENTIAL ENERGY QUIP OF LANTICLE DUE TO ITS NEARESF NEIGHBOR A DISTANCE FIR (9 = CHARGE OF PARTICLE) No = number Jensity

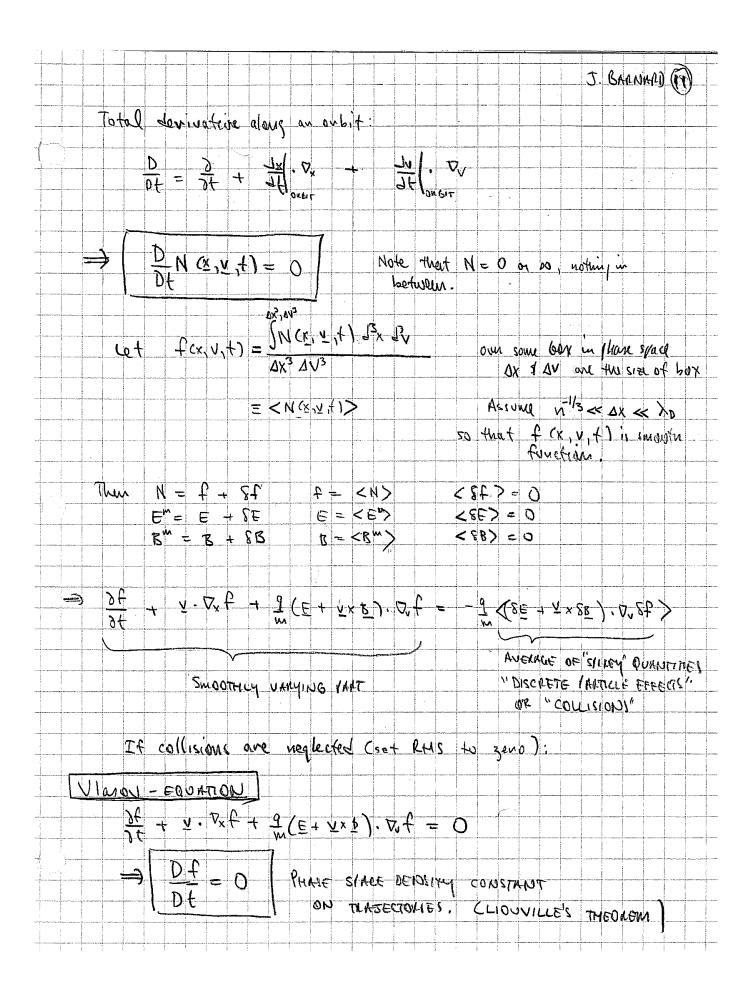
IF qque << kBT => WEAKLY COULLED ILASMA OK SIMILY PLASMA

$$PEFINE \lambda_{D} = \frac{\left(\frac{k_{T}T}{m}\right)^{\prime L}}{\left(\frac{k_{0}q^{2}}{\epsilon_{0}m}\right)^{\prime / 2}} = \frac{V_{TH}}{\omega_{p}} = \left(\frac{k_{B}T}{m_{0}q^{2}}\right)^{\prime 2} \frac{\Delta EBIE}{LENGTH}$$

= CHARACTERISTIC DISTANCE WHEREBY CHARGES ARE SHIELDED

DEFINE $\Lambda = \frac{4\pi}{3} n_0 \lambda_0^3 \equiv PLASMA [AddMeter]$ $\sim \left(\frac{k_B T}{q T_{TP}}\right)^{3/2} >> 1 \quad [if q g_T << k_B T]$





J. BALNARD (12)

THE RHS IS DUE TO COLLISIONS WITH NON-SMOOTH FIELDS:

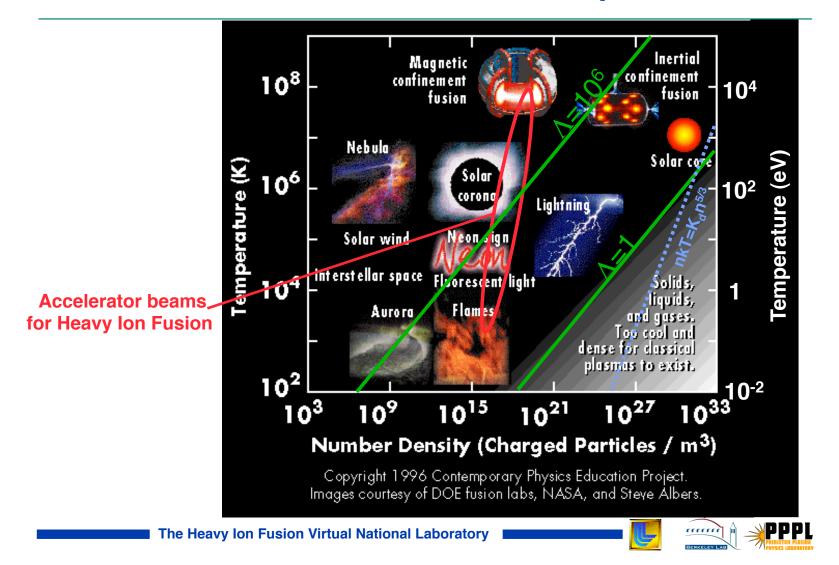
VERY HEURISTICALLY

$$-\frac{9}{m}\left\langle \left(\frac{8E}{8E} + \sqrt{8B}\right) \cdot \sqrt{8F} \right\rangle \sim \sqrt{2F}$$

 $\frac{\text{Coursen } N}{\text{LHS}} \sim \frac{1}{16\pi\lambda_0^3} = \frac{1}{16}$

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Accelerator beams are non-neutral plasmas



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## Emittance is constant for linear force profiles and matched beams

