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Summary of JB lectures

START WITH MICROSCOPIC PHASE SPACE DENSITY

$$N(\underline{x}, \underline{v}, t) = \sum_{i=1}^N \delta(\underline{x} - \underline{x}_i(t)) \delta(\underline{v} - \underline{v}_i(t))$$

Klimontovich Density

$\frac{\partial N}{\partial t} + \text{LIEBMAN EQUATIONS} \Rightarrow$  KLIMONTIVICH EQUATION:

$$\frac{\partial N}{\partial t} + \underline{v} \cdot \nabla_{\underline{x}} N(\underline{x}, \underline{v}, t) - \frac{q}{m} (\underline{E}^m + \underline{v} \times \underline{B}^m) \cdot \nabla_{\underline{v}} N(\underline{x}, \underline{v}, t) = 0$$

$$\text{or } \frac{dN(\underline{x}, \underline{v}, t)}{dt} = 0$$

Letting  $N = f + \delta f$      $f = \langle N \rangle$   
 $\underline{E}^m = \underline{E} + \delta \underline{E}$      $\underline{E} = \langle \underline{E}^m \rangle$   
 $\underline{B}^m = \underline{B} + \delta \underline{B}$      $\underline{B} = \langle \underline{B}^m \rangle$

$$f = \frac{\int N d^3x d^3v}{\Delta x^3 \Delta v^3}$$

$n^{-1/3} \ll \Delta x \ll \lambda_D$

PERFORMING LOCAL AVERAGES TO OBTAIN SMOOTH & "LIKEY" QUANTITIES:

$$\frac{\partial f}{\partial t} + \underline{v} \cdot \frac{\partial f}{\partial \underline{x}} + \frac{d\underline{v}}{dt} \cdot \frac{\partial f}{\partial \underline{v}} = \frac{\partial f}{\partial t_c} \sim \frac{f}{\tau_c}$$

We estimated  $\left| \frac{\partial f / \partial t_c}{\left| \frac{q \underline{E}}{m} \cdot \frac{\partial f}{\partial \underline{v}} \right|} \right| \sim \frac{1}{16 \lambda_D^3 n_0} \ll 1$

$\lambda_D = v_{th} / \omega_p$      $v_{th} \equiv \sqrt{\frac{kT}{m}}$      $\omega_p \equiv \sqrt{\frac{q^2 n}{\epsilon_0 m}}$

$$\frac{\partial f}{\partial t} + \underline{v} \cdot \frac{\partial f}{\partial \underline{x}} + \frac{d\underline{p}}{dt} \cdot \frac{\partial f}{\partial \underline{p}} = 0 \quad \dot{\underline{p}} = -\frac{\partial H}{\partial \underline{x}} \quad \dot{\underline{x}} = \frac{\partial H}{\partial \underline{p}}$$

$$\frac{df}{dt} = 0$$

LIUVILLE'S EQUATION (INCOMPRESSIBILITY OF PHASE VOLUME)

DEFINE NORMALIZED EMITTANCES PROPORTIONAL TO  $\frac{\Delta p_x \Delta z}{\Delta x \Delta y} \propto \Delta E \Delta t$

SO THAT  $\epsilon_{px}^2 = \gamma_{\beta}^2 (\langle x^2 \rangle \langle x'^2 \rangle - \langle x x' \rangle^2)$

$\Rightarrow$  CONSTANT IF FORCES ARE LINEAR IN  $x$  & FILAMENTATION IS ABSENT (LINEAR WITHOUT COUPLING TO  $z$ , DC  $\omega$ ).

WE DERIVED TWO SETS OF PARTICLE EQUATION OF MOTION:

AXIAL EQUATION (FOR AXISYMMETRIC SYSTEMS) ( $\frac{\partial}{\partial \theta} = 0$ )

STARTING WITH THE LORENZ FORCE EQUATION  $\frac{d\mathbf{p}}{dt} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$  IN CYL. COORD.

$$\frac{d}{dt}(\gamma m r) - \gamma m r \dot{\theta}^2 = q \left( \frac{V''}{z} r + r \dot{\theta} B \right) + q (E_r^{\text{self}} + v_z B_{\theta}^{\text{self}})$$

$\uparrow$                        $\uparrow$                        $\uparrow$                        $\uparrow$                        $\uparrow$                        $\uparrow$                        $\uparrow$   
 INITIAL                      CENTRIFUGAL                       $E_r$  external                       $v_z B_{\theta}$                       SELF-FIELDS  
 (DIVERGENCE OF  $E = 0$ )

$\dot{r} = \frac{dr}{dt}; \quad v = \frac{dr}{ds} = \frac{\dot{r}}{\beta c}$

$\theta$ -component:

$$p_{\theta} = \gamma m r^2 \dot{\theta} + \frac{q}{z} B(z) r^2 = \text{constant}$$

$$= \gamma m r^2 \beta c \theta' + \frac{q B r^2}{z} = \text{constant}$$

$$r'' + \frac{\gamma'}{\beta^2 \gamma} r' + \frac{\gamma''}{z \beta^2 \gamma} r + \left( \frac{\omega_c}{z \gamma \beta c} \right)^2 r - \left( \frac{p_{\theta}}{\gamma \beta m c} \right)^2 \frac{1}{r^3} - \frac{q}{\gamma m v_z^2} \frac{\lambda(r)}{2 \pi \epsilon_0 r} = 0$$

$\uparrow$                        $\uparrow$                        $\uparrow$                        $\uparrow$                        $\uparrow$                        $\uparrow$   
 INITIAL                      ACCELERATION                       $E_r$                       CENTRIFUGAL                      CENTRIFUGAL                      SELF-FIELDS  
 (INERTIA)                      (CONVERGENCE OF FIELD LINES)

STATISTICAL AVERAGE OF THIS EQUATION

$$r_b'' + \frac{\gamma'}{\beta^2 \gamma} r_b' + \frac{\gamma''}{z \beta^2 \gamma} r_b + \left( \frac{\omega_c}{z \gamma \beta c} \right)^2 r_b - \frac{4 \langle p_{\theta}^2 \rangle}{(\gamma m \beta c)^2 r_b^3} - \frac{E_r}{r_b} - \frac{Q}{r_b} = 0$$

$$E_r^2 \equiv 4(\langle r^2 \rangle \langle r'^2 \rangle - \langle r r' \rangle^2 + \langle r^2 \rangle \langle r^2 \theta'^2 \rangle - \langle r^2 \theta' \rangle^2); \quad Q = \frac{q \lambda}{2 \pi \epsilon_0 \gamma^3 \beta^2 m c^2}$$

$$= E_x^2 - 4 \langle r^2 \theta'^2 \rangle \quad (\text{if } p = p_{\theta} \text{ only})$$

# CARTESIAN EQUATION OF MOTION

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(15)

EQUATION OF MOTION AGAIN STARTING WITH  $\frac{d\mathbf{p}}{dt} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$

RETURN TO X, Y COORDINATES

$$x'' + \frac{1}{\gamma v_z} \frac{d}{ds} (\gamma v_z) x' = \frac{-q}{\gamma^3 m v_z^2} \frac{\partial \phi}{\partial x} \mp \begin{cases} \frac{q B'}{\gamma m v_z^2} x & \text{An magnetic quads} \\ \frac{q E'}{\gamma m v_z^2} x & \text{An electric quads} \end{cases}$$

Let  $\frac{\gamma m v_z}{q} = \frac{p}{q} \equiv [B'] \equiv \text{RIGIDITY}$

$$y'' + \frac{1}{\gamma v_z} \frac{d}{ds} (\gamma v_z) y' = \frac{-q}{\gamma^3 m v_z^2} \frac{\partial \phi}{\partial y} \mp \begin{cases} \frac{B'}{[B']} y & \text{magnetic} \\ \frac{q E'}{\gamma m v_z^2} y & \text{electric} \end{cases}$$

## ENVELOPE EQUATION

$$r_x^2 = 4 \langle x^2 \rangle; \quad r_y^2 = 4 \langle y^2 \rangle$$

$$r_x' = \frac{4 \langle x x' \rangle}{r_x}$$

$$r_x'' = \frac{4 \langle x x'' \rangle}{r_x} + \frac{E_x^2}{v_x^3};$$

$$E_x^2 = 16 (\langle x^2 \rangle \langle x'^2 \rangle - \langle x x' \rangle^2)$$

$$r_y'' = \frac{4 \langle y y'' \rangle}{r_y} + \frac{E_y^2}{v_y^3}$$

$$E_y^2 = 16 (\langle y^2 \rangle \langle y'^2 \rangle - \langle y y' \rangle^2)$$

for magnetic focusing:

$$r_x'' + \frac{1}{\gamma v_z} \frac{d}{ds} (\gamma v_z) r_x' + \frac{4q}{\gamma^3 m v_z^2} \langle x \frac{\partial \phi}{\partial x} \rangle \mp \frac{B'}{[B']} r_x - \frac{E_x^2}{v_x^3} = 0$$

$$r_y'' + \frac{1}{\gamma v_z} \frac{d}{ds} (\gamma v_z) r_y' + \frac{4q}{\gamma^3 m v_z^2} \langle y \frac{\partial \phi}{\partial y} \rangle \mp \frac{B'}{[B']} r_y - \frac{E_y^2}{v_y^3} = 0$$

(for electric focusing  $\frac{B'}{[B']} \rightarrow \frac{q E'}{\gamma m v_z^2}$ )

SPACE CHARGE TERM WITH ELLIPTICAL SYMMETRY

NOW DEFOCUSING IN ONE DIRECTION AND FOCUSING IN THE OTHER  $\Rightarrow$  RADIAL SYMMETRY SHOULD BE REPLACED

BY ELLIPTICAL SYMMETRY:  $\rho = \rho \left( \frac{x^2}{r_x^2} + \frac{y^2}{r_y^2} \right)$

CAN BE SHOWN THAT  $\langle x \frac{\partial \phi}{\partial x} \rangle = \frac{-\lambda}{4\pi\epsilon_0} \frac{r_x}{r_x + r_y}$

$\langle y \frac{\partial \phi}{\partial y} \rangle = \frac{-\lambda}{4\pi\epsilon_0} \frac{r_y}{r_x + r_y}$

USE  $\phi(x,y) = \frac{-\lambda r_y}{4\epsilon_0} \int_0^{\infty} \frac{q(\chi) ds}{\sqrt{r_x^2+s} \sqrt{r_y^2+s}}$  TO PROVE, WHERE  $\hat{\rho}(\chi) = \frac{d^2 q}{d\chi^2}$

$\rho(x,y) = \hat{\rho}(\chi)|_{\chi=0}$   
 $\chi = \frac{x^2}{r_x^2+s} + \frac{y^2}{r_y^2+s}$

DEFINING  $Q = \frac{2\lambda q}{4\pi\epsilon_0 \gamma^3 m v_z^2}$

$$v_x'' + \frac{1}{\gamma v_z} \frac{d}{ds} (\gamma v_z) v_x' - \frac{2Q}{r_x + r_y} = \frac{B'}{[B\rho]} v_x - \frac{\epsilon_x^2}{r_x^2} = 0$$

$$v_y'' + \frac{1}{\gamma v_z} \frac{d}{ds} (\gamma v_z) v_y' - \frac{2Q}{r_x + r_y} = \frac{B'}{[B\rho]} v_y - \frac{\epsilon_y^2}{r_y^2}$$

(for Electric Focusing  $\frac{B'}{[B\rho]} \rightarrow \frac{qE'}{\gamma m v_z^2}$ )

(ANALOGUE TO CIRCULAR BEAM:

$\langle r \frac{\partial \phi}{\partial r} \rangle = \frac{-\lambda}{4\pi\epsilon_0}$  PROVED IN HOMEWORK)



## ENVELOPE EQUATIONS DERIVED

VMS ENVELOPES DEFINED IN TERMS OF VMS QUANTITIES, EMITTANCE

1. PARAXIAL  $v_b; \rho$  (NOT GUARANTEED TO BE CONSERVED).
2. ELLIPTICAL  $v_x, v_y; \rho \left( \frac{x^2}{v_x^2} + \frac{y^2}{v_y^2} \right)$
3. LONGITUDINAL  $v_z$  FOR  $E_z = \frac{-q}{4\pi\epsilon_0} \frac{\partial \lambda}{\partial z} \propto z; \left[ \lambda \propto \left( 1 - 4z^2/v_z^2 \right) \right]$   
 $\sqrt{x} \propto (z/v_z)$

4. ELLIPSOIDAL W/ BUNCHES  $v_x, v_z$  (ALSO  $v_x, v_y, v_z$  (p CONSTANT) c.f. Wangler, section 9.9).

5. ELLIPTICAL WITH IMAGES  $v_x, v_y$   $\rho \left( \frac{x^2}{v_x^2} + \frac{y^2}{v_y^2} \right)$

6. LAMMOR FRAME (PERIODIC SOLENOIDS OR CONTINUOUS FOCUSING)  $v_x, \tilde{v}_y$  p const

KINETIC ENVELOPE EQUATIONS (CONSTRAINT EQUATION ON A PARTICULAR DISTRIBUTION FUNCTION; EMITTANCE CONSERVED)

1. KV FOR ELLIPTICAL UNIFORM BEAMS  $f(x, x', y, y')$   
[IDENTICAL TO #2 ABOVE]
2. NEUFEL DISTRIBUTION FOR 1D  $f(z, z')$   
[IDENTICAL TO #3 ABOVE]

## MOMENT EQUATIONS

1. TRANSPORT WITH CHROMATIC EFFECTS  
 $\langle x^2 \rangle, \langle x'^2 \rangle, \langle xx' \rangle, \langle x^2 \delta \rangle, \langle x'^2 \delta \rangle, \langle xx' \delta \rangle, \dots$

# Summary of Current Limits From Different Focusing Methods

## EINZEL LENS

$$Q_{\text{max}} \approx \frac{3\pi^2}{8} \left( \frac{q\phi_0}{m\nu_0^2} \right)^2 \left( \frac{V_0}{L} \right)^2$$

## SOLENOIDS

$$Q_{\text{max}} = \left( \frac{\omega_c V_0}{2\gamma\beta c} \right)^2$$

## QUADRUPOLE FOCUSING

$$Q_{\text{max}} \approx \frac{\eta Q_0}{2\pi} \left( \frac{\sin \frac{\pi}{2}}{\frac{\pi}{2}} \right) \left[ \frac{B r_0}{CB\rho} \right] \left[ \frac{V_0}{V_p} \right] \left[ \frac{z V_0}{\gamma m \nu_0^2} \right] \left[ \frac{r_0^2}{r_p^2} \right] \left[ \frac{V_p}{r_p} \right]$$

MAGNETIC
Electric

## FOR NON-RELATIVISTIC BEAMS

$$\sigma_0 \approx \eta L^2 (B'/[B\rho]) \sim \eta L^2 (qB'/\gamma m v)$$

$$\gamma_{\text{max}} \propto \frac{Q_0^2}{V}$$

$$\gamma_{\text{max}} \propto \frac{q}{m} B^2 r_p^2$$

$$\gamma_{\text{max}} \propto \left\{ \begin{array}{l} B_1 V_0^{1/6} r_p \\ N_q \end{array} \right.$$

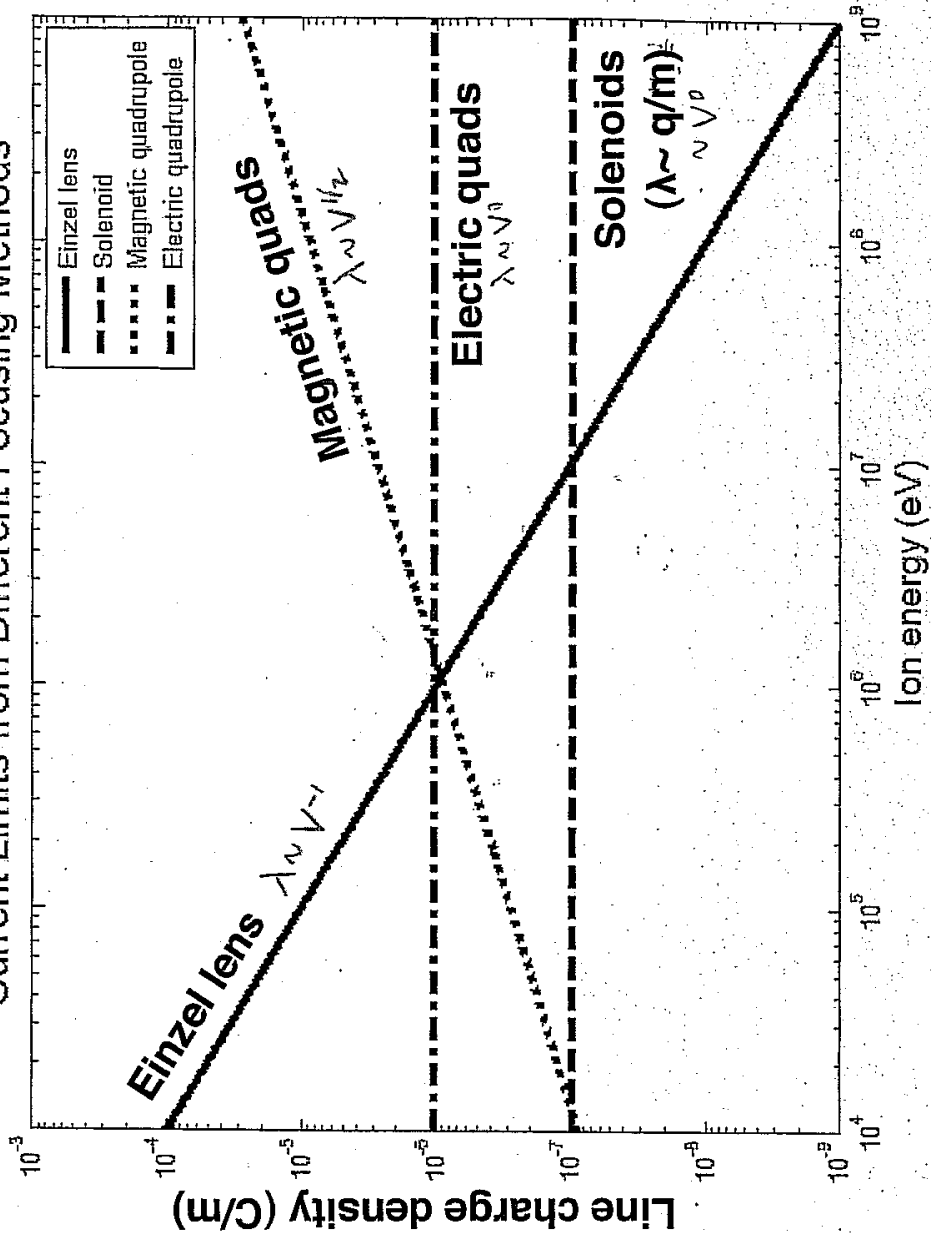
Note

$Q_0$  = Voltage between Einzel lenses / 2

$V_0$  = Voltage on a grid relative to ground

$V$  = particle energy /  $q$

# Current Limits from Different Focusing Methods





# LONGITUDINAL DYNAMICS Summary

## 1D VLASOV EQUATION (Vlasov Equation) $dx dx' dy dy'$

$$\frac{\partial \tilde{f}}{\partial t} + z' \frac{\partial f}{\partial z} + z'' \frac{\partial \tilde{f}}{\partial z'} = 0$$

$$z'' = \frac{q E_z}{m v_0^2}$$

$$\frac{\partial^2 \phi}{\partial z^2} + \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial \phi}{\partial r} \right) = - \rho \left( \frac{1}{\epsilon_0} \right)$$

$$E_z = -\frac{q}{4\pi\epsilon_0} \frac{\partial \lambda}{\partial z}$$

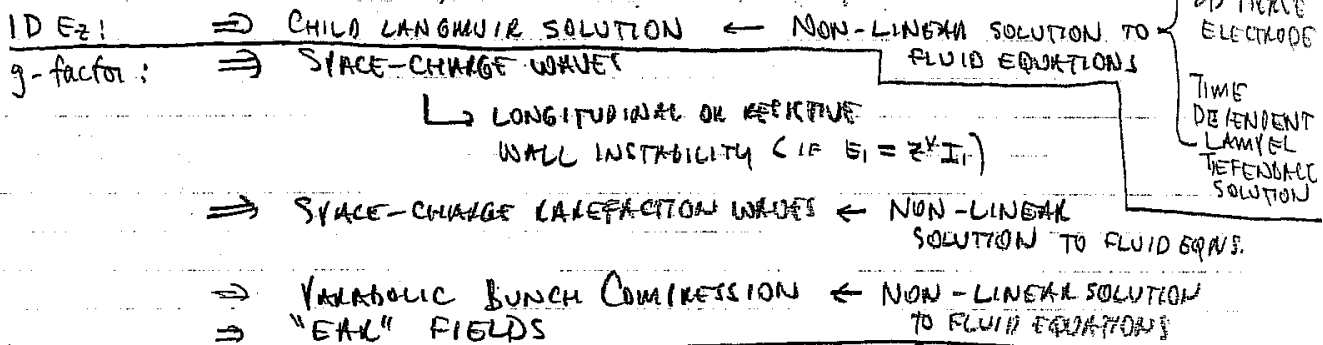
"g-factor" model

CHILD-LANGMUIR IN 1-D PIPE

## LEADS TO FLUID EQUATIONS (1D Vlasov Equation) $dz'$

$$\frac{\partial \lambda}{\partial t} + \frac{\partial (\lambda z')}{\partial z} = 0$$

$$\frac{\partial z'}{\partial t} + z' \frac{\partial z'}{\partial z} + \frac{1}{\lambda} \frac{\partial (\lambda z' z)}{\partial z} = \frac{q E_z}{m v_0^2}$$



## VLASOV EQUATION ALSO ⇒ ENVELOPE EQUATION $\iint$ VLASOV Equation $dz dz'$

$$\frac{d^2 n_z}{dz^2} = \frac{E_z^2}{v_z^3} + \frac{3}{2} \frac{q q Q_c}{4\pi\epsilon_0 m v^2} \frac{1}{v_z^2} - K(r) v_z$$

KINETIC SOLUTION TO VLASOV EQUATION & SATISFYING KMI ENVELOPE EQUATION

↳ NEUBER DISTRI BUTION

$$f(z, z') = \frac{3N}{2\pi E_z} \sqrt{1 - \frac{z^2}{v_z^2} - \frac{v_z^2 (z' - v_z^2 / v_z)^2}{E_z^2}}$$

ESTIMATING SLOT SIZE

$$r_x'' + \frac{(Y_0 \beta_0)'}{Y_0 \beta_0} r_x' + K_x r_x - \frac{zQ}{r_x + r_y} - \frac{E_x^2}{v_x^3} = 0$$

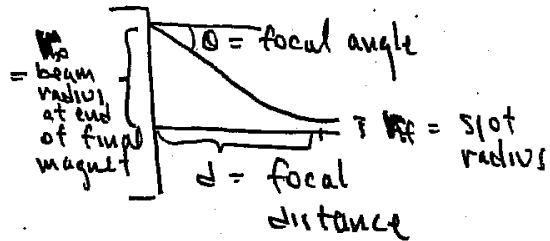
$$r_y'' + \frac{(Y_0 \beta_0)'}{Y_0 \beta_0} r_y' + K_y r_y - \frac{zQ}{r_x + r_y} - \frac{E_y^2}{v_y^3} = 0$$

IN CHAMBER: NO EXTERNAL FOCUSING, NO ACCELERATION  
AND BEAM IS OFTEN CIRCULAR (BY DESIGN)

$$\Rightarrow K_x = K_y = (Y_0 \beta_0)' = 0 \quad \& \quad v_x = v_y = v_b$$

$\Rightarrow$  ENVELOPE EQUATION IS:

$$r_b'' = \frac{Q}{r_b} + \frac{E^2}{v_b^3}$$



MULTIPLYING BY  $r_b'$  & INTEGRATING  $\Rightarrow$

$$\frac{r_{bf}^{1/2}}{2} - \frac{r_{b0}^{1/2}}{2} = Q \ln \frac{r_{bf}}{r_{b0}} + \frac{E^2}{2v_{b0}^3} - \frac{E^2}{2v_{bf}^3}$$

Now  $r_{b0}' \approx 0$        $r_{bf} = \text{spot radius}$   
 $r_{bf}' = 0$        $r_{b0} \approx d \theta$

$$r_{bf} \ll r_{b0}$$

$$\Rightarrow \theta^2 \approx zQ \ln \left( \frac{d}{r_{bf}} \right) + \frac{E^2}{r_{bf}^2}$$

WHEN  $\theta \ll 0$

$$r_{\text{spot}}^2 = \frac{E^2}{\theta^2} + r_{\text{CHROMATIC ABERRATION}}^2 + \dots$$

$$r_{\text{CHROMATIC}}^2 = \alpha^2 d^2 \left( \frac{\theta}{\beta} \right)^2 \theta^2$$

$\alpha \approx 6$  (system dependent)

## NORMAL MODES

### LONGITUDINAL

#### SPACE-CHARGE WAVES (FLUID)

$$\omega = \pm c_s k \quad [\text{IN COMOVING BEAM FRAME}]$$

$$c_s = \sqrt{\frac{qg\lambda_0}{4\pi\epsilon_0 m}} = \text{SPACE CHARGE WAVE SPEED}$$

### TRANSVERSE

#### ENVELOPE MODES

CONTINUOUS FOCUSING (LONG BUNCHES)

$$\text{BREATHING: } k_B^2 = 2k_{p0}^2 + 2k_p^2$$

$$\text{QUADRUPOLE } k_Q^2 = k_{p0}^2 + 3k_p^2$$

$$\text{(HERE } k_p^2 \equiv k_{p0}^2 - \frac{Q}{R_b^2} \text{)}$$

(ANALOGOUS MODES IN BUNCHED BEAMS)

STUBS LOOKED AT MODES IN PERIODIC SYSTEMS (CONTINUOUS FOCUSING)

+ KINETIC MODES (GLUCKSTEIN MODES)

+ FLUID MODES

## INSTABILITIES

1. LONGITUDINAL (RESISTIVE WALL) INSTABILITY

(FLUID INSTABILITY)

2. ELECTRON-ION INSTABILITY

(CENTROID INSTABILITY)

STEVE TALKED ABOUT:

3. ENVELOPE INSTABILITIES

STEVE TALKED ABOUT:

4. KINETIC INSTABILITIES

(DISTRIBUTION FUNCTION DEPENDENT)

5. SINGLE PARTICLE RESONANT INSTABILITIES

- HALO

- RING RESONANCES

HALO:

COVE TEST PARTICLE MODEL:

$$x'' = \begin{cases} -\left[k_{p0}^2 - \frac{Q}{v_b^2}\right]x & \text{for } v < v_b \\ -\left[k_{p0}^2 - \frac{Q}{v^2}\right]x & \text{for } v > v_b \end{cases}$$

$$v_b = v_{b0} + \delta v_b \cos(k_B s + \phi)$$

Gluckstein's phase-amplitude analysis:

$$x'' + \overbrace{\left[k_{p0}^2 - \frac{Q}{v_{b0}^2}\right]}^{k_p^2} x = f(x)$$

↑  
Non linear + forcing part

$$x = A \sin \psi \quad x' = k_p A \cos \psi \quad \leftarrow \text{PHASE/AMPLITUDE}$$

$\psi = k_p s + \alpha$  If  $f=0$   $A$  &  $\alpha$  would be constant

$$\Rightarrow A' = \frac{1}{k_p v_{b0}} f \cos \psi \quad \alpha' = -\frac{1}{k_p v_{b0} A} f \sin \psi$$

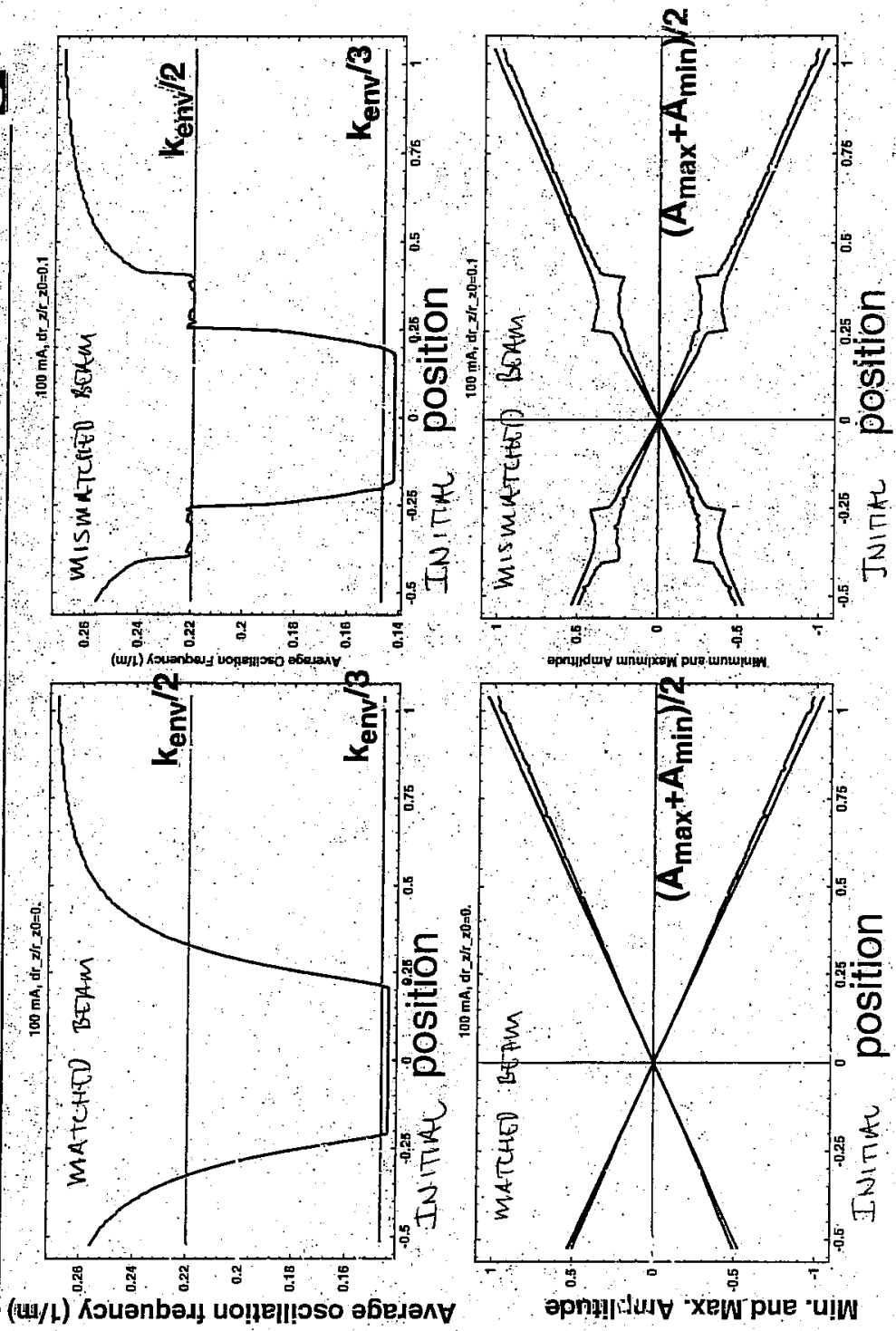
DEFINE RESONANT PHASE:  $\Psi_r = 2\psi - k_B s$

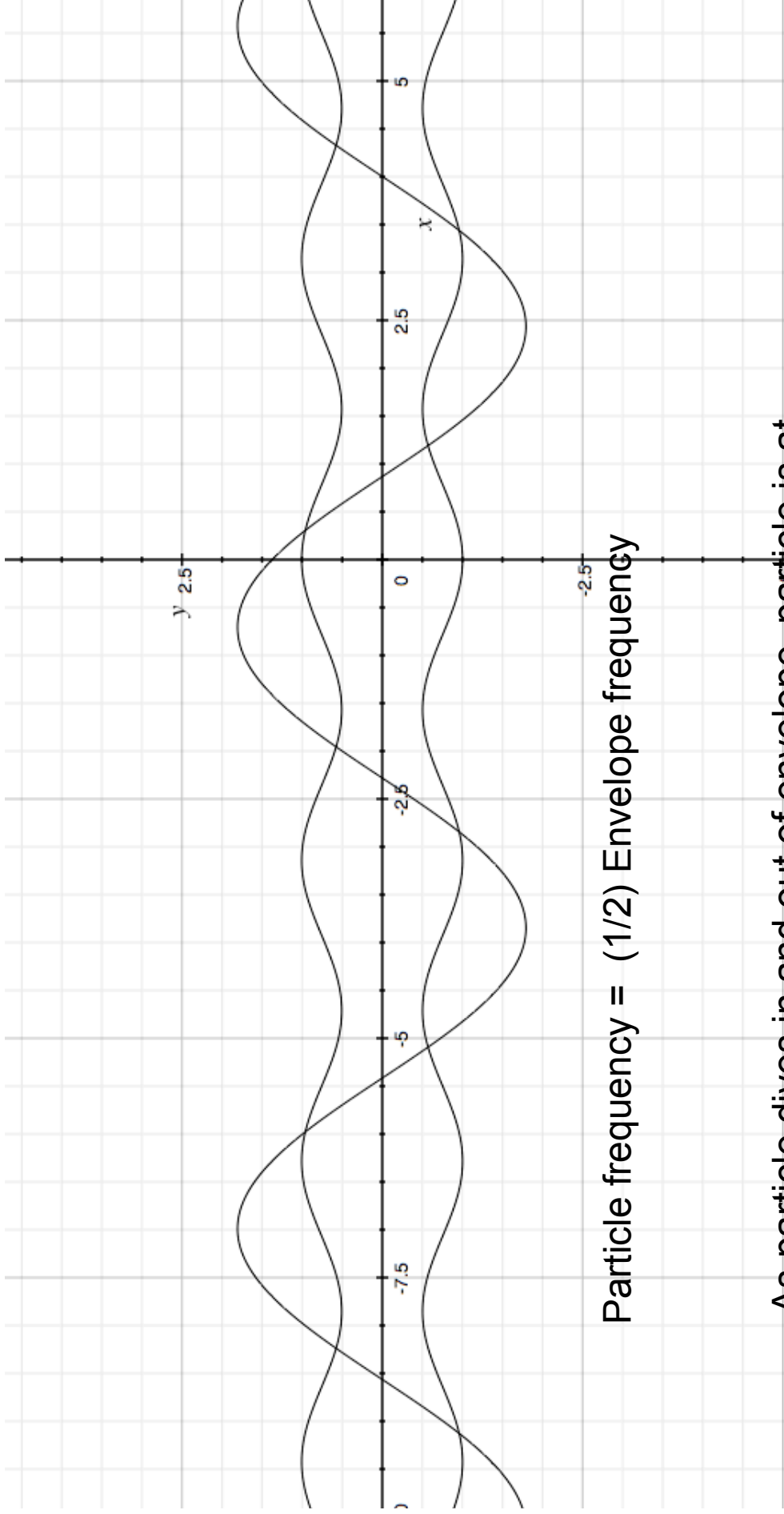
AVERAGE OVER ALL NON-RESONANT FREQUENCIES

$$A_r' = \frac{1}{k_p v_{b0}} \int_{-\pi}^{\pi} f \cos \psi \frac{d\psi}{2\pi}; \quad \alpha_r' = -\frac{1}{k_p A_r} \int_{-\pi}^{\pi} \frac{df}{2\pi} f \sin \psi$$

$\rightarrow A_r', \Psi_r' \rightarrow \omega', \Psi_r' \rightarrow H(\omega', \Psi_r') \rightarrow$  GIVE RESONANT PARTICLE TRAJECTORY & SEPARATRIX

# Numerically determined frequency and amplitude of particle oscillations: linear rf focusing







Particle frequency =  $(1/2)$  Envelope frequency

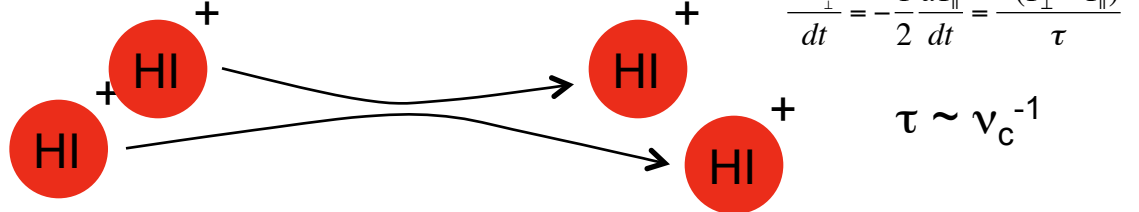
As particle dives in and out of envelope, particle is at same phase of envelope oscillation.

Those particles that are exiting the beam when beam radius is small, and entering beam when beam radius is large, get larger "kick" going out and smaller kick coming in, so are driven to large amplitude.

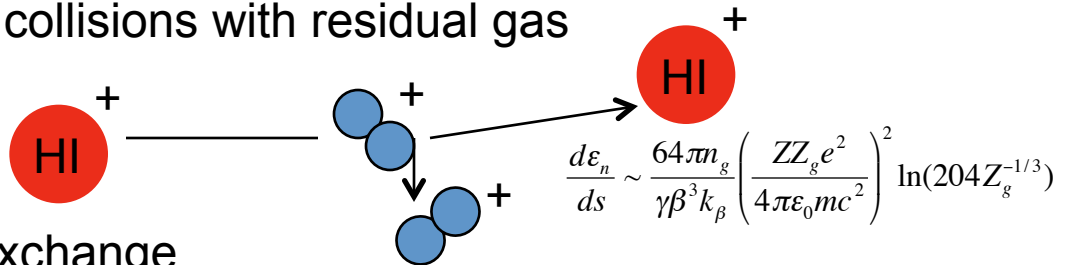
 <b>HI<sup>+</sup></b> Heavy ion	 Residual gas molecule	<b>e<sup>-</sup></b> electron
--	--	-------------------------------

Processes:

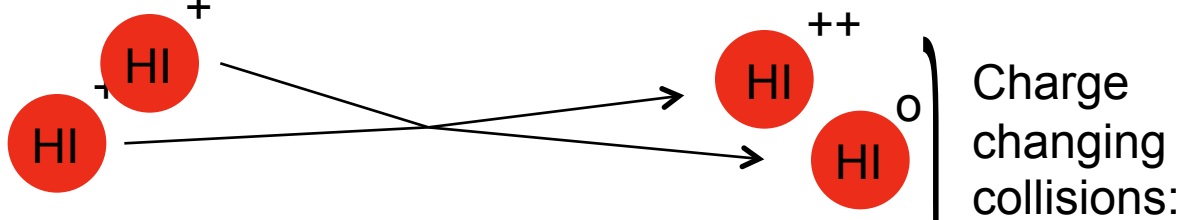
1. Coulomb collisions (intra-beam)



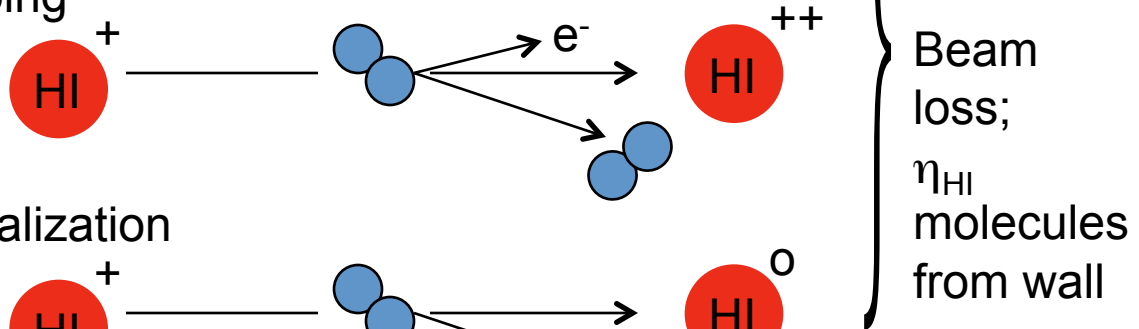
2. Coulomb collisions with residual gas



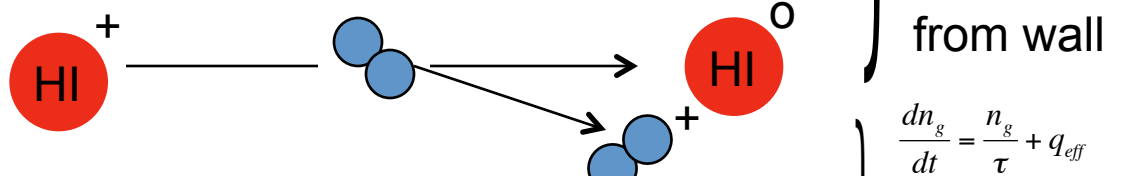
3. Charge exchange



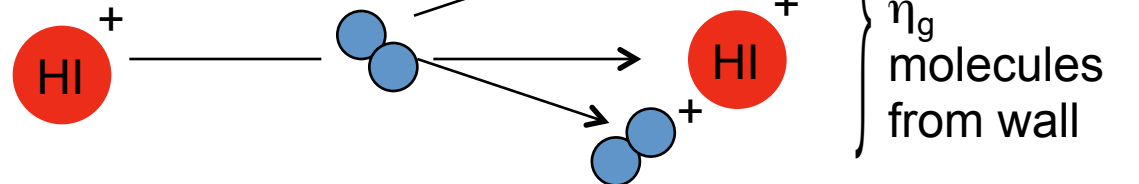
4. Stripping



5. Neutralization

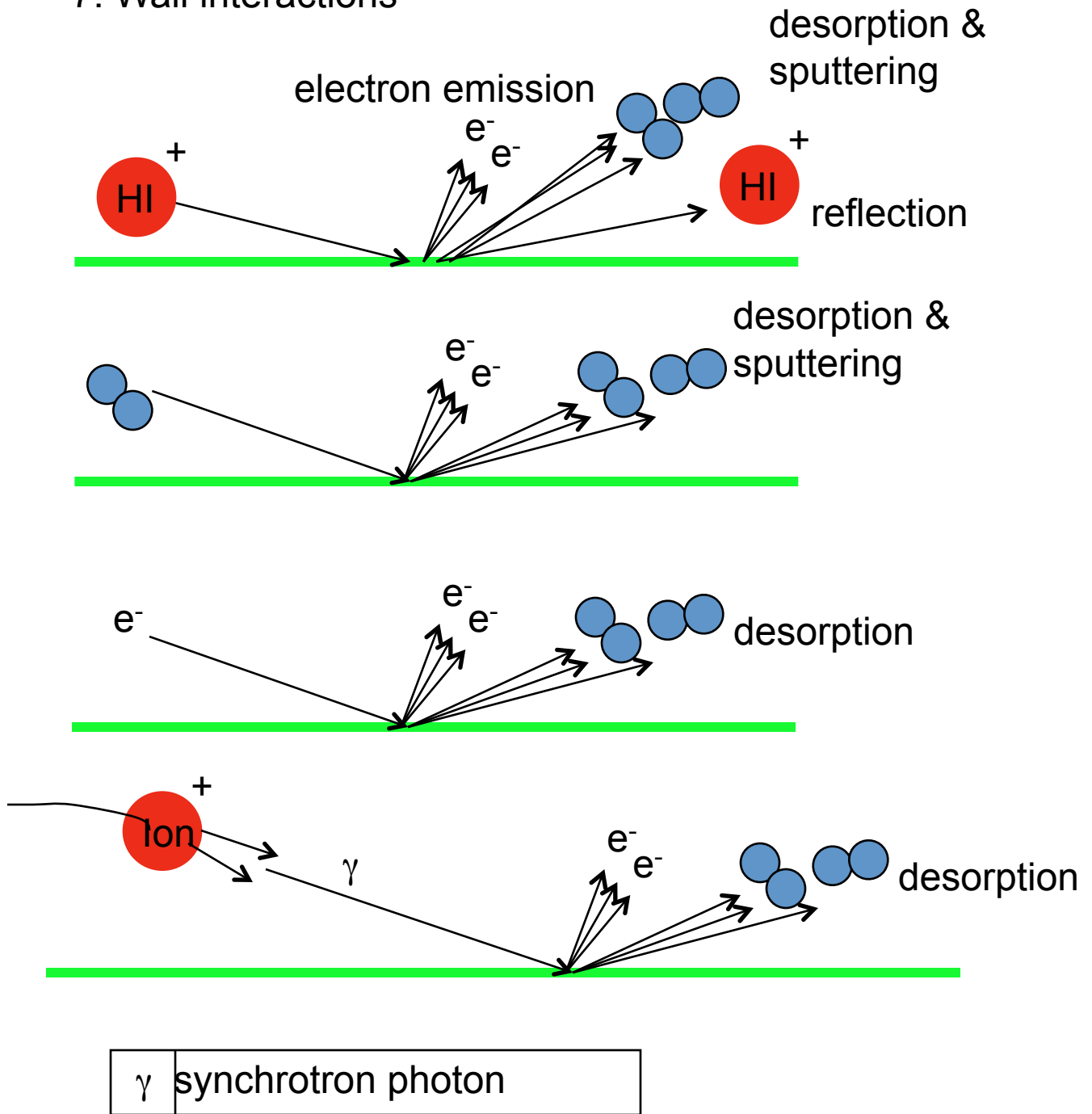


6. Gas Ionization





## 7. Wall interactions

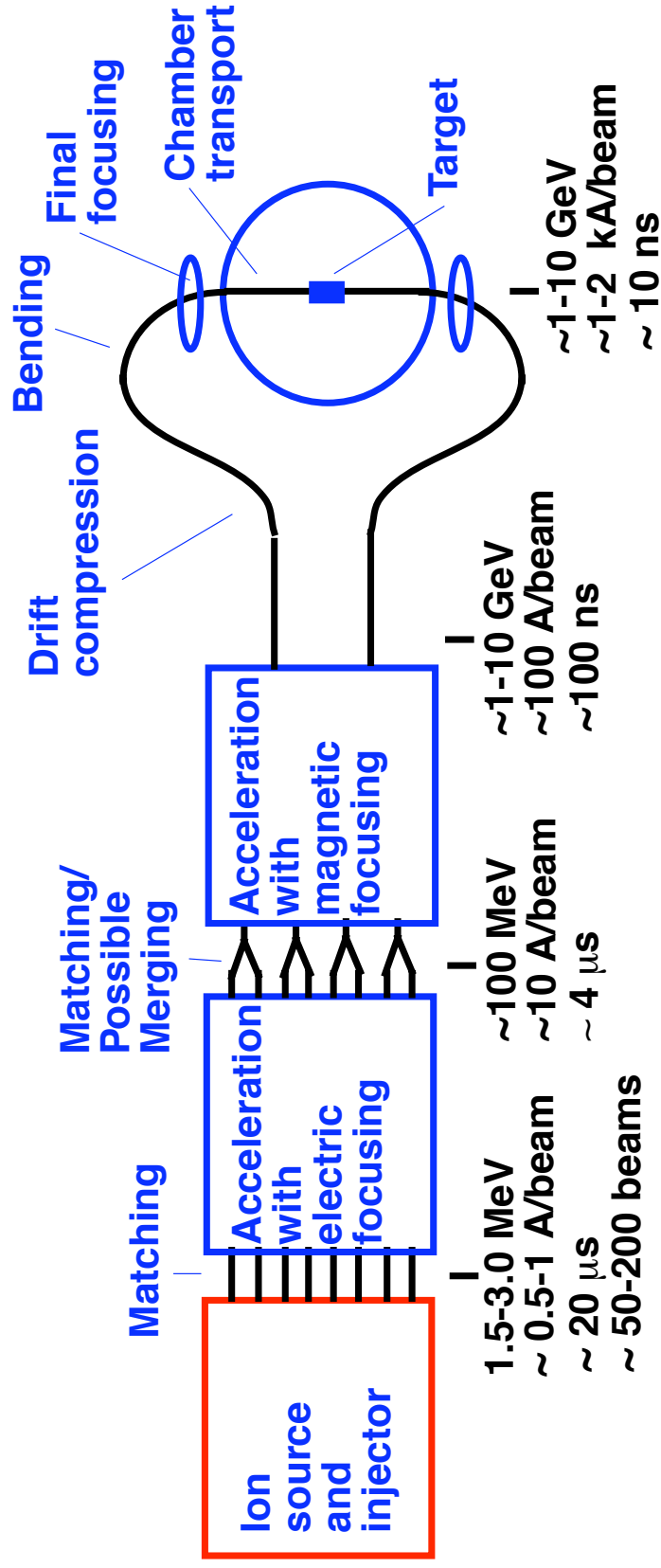


SUMMARY OF ELECTRON, GAS, PRESSURE, & SCATTERING EFFECTS

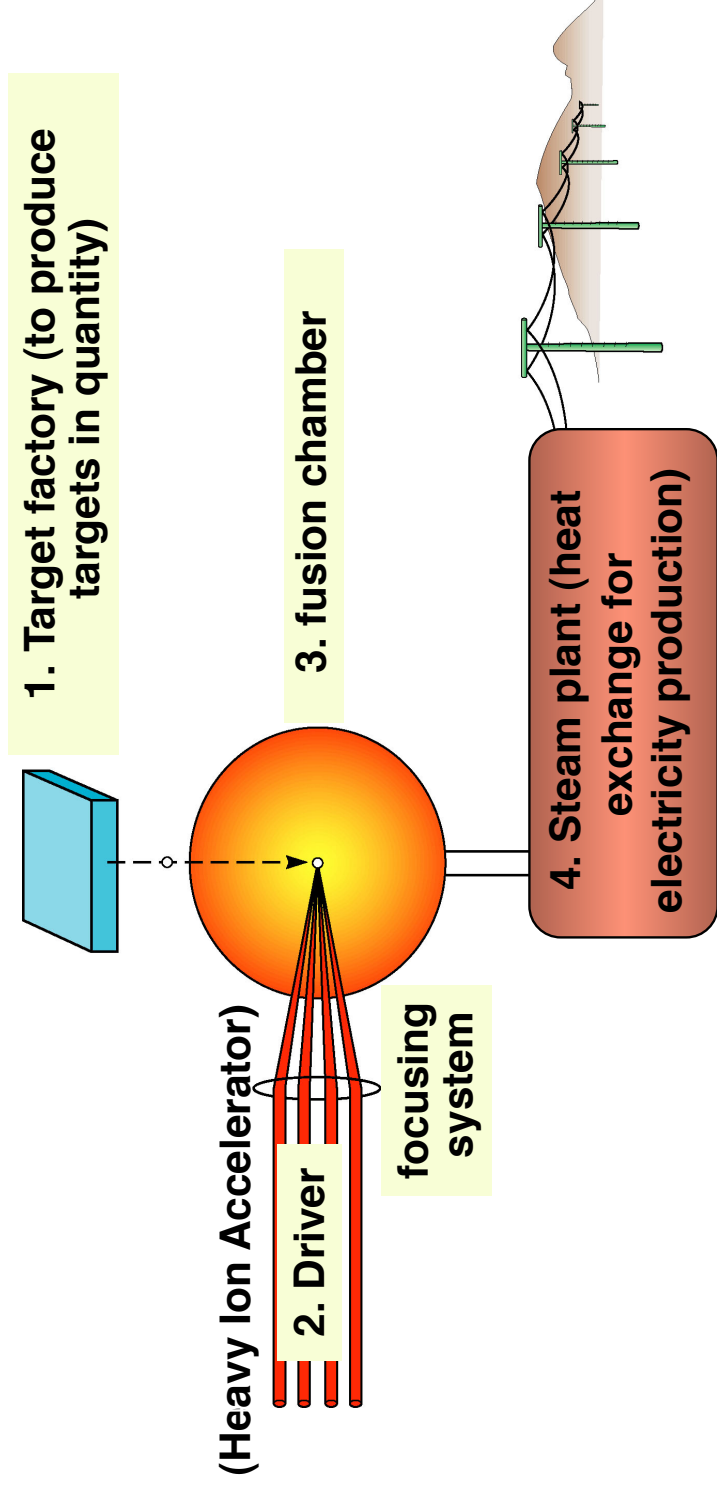
- 1. COULOMB COLLISIONS WITHIN BEAM CAN TRANSFER ENERGY FROM I TO II AND PROVIDE LOWER LIMIT ON  $T_{II}$ , HIGHER THAN FROM ACCELERATIVE COOLING.
- 2. COULOMB INTERACTIONS WITH RESIDUAL GAS NUCLEI PROVIDE A SOURCE OF EMITTANCE GROWTH (BUT NOT IMPORTANT FOR HIGHER-MAII AND LONG RESIDENCE TIMES).
- 3. PRESSURE INSTABILITY FROM DESOLATION OF RESIDUAL GAS BY STRIKED BEAM IONS HITTING WALL OF BEAM-IONIZED RESIDUAL GAS ATOMS, FORCED TO WALL BY E-FIELD OF BEAM. LIMITS CURRENT IN RINGS OF HIGH KEV X-RAY LINAC.
- 4. ELECTRONS CAN CASCADE AND REACH A "QUIET" EQUILIBRIUM (POPULATION OF SIMILAR LINE CHARGE TO THE ION BEAM. ELECTRON-ION TWO STREAM INSTABILITY IS UNSTABLE, AND CAN LEAD TO TRANSVERSE INSTABILITY, SIMILAR TO WHAT IS OBSERVED IN SOME PROTON RINGS.

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# Induction acceleration for HIF consists of several subsystems and a variety of beam manipulations



# Inertial fusion energy (IFE) power plants of the future will consist of four parts



A power plant driver would fire about five targets per second to produce as much electricity as today's 1000 Megawatt power plant



The Heavy Ion Fusion Virtual National Laboratory

