John Barnard Steven Lund USPAS June 12-23, 2017 Lisle, Illinois

Intrabeam collisions, gas and electron effects in intense beams

- 1. Beam/beam coulomb collisions
- 2. Beam/gas scattering
- 3. Charge changing processes
- 4. Gas pressure instability
- 5. Electron cloud processes
- 6. Electron-ion instability

Gas and electron effects

-Effects are quite different depending on q, m of species being accelerated

-Circular accelerators vs. Linacs ($t_{residence} \sim ms$ to days vs. 10's of μs)

-Long pulse vs. short pulse ($t_{pulse} \sim 10$'s of μ s vs. 10's of ns)





$$= \frac{15 (k_{1}T_{0} + k_{0}T_{0})}{2\pi^{4}} + \frac{1}{2\pi^{4}} + \frac{1}$$

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 $\frac{JO}{JR} = \left(\frac{272g}{4\pi\epsilon}\frac{e^2}{PV}\right)^2 \frac{1}{\left(A^2 + O^2\right)^2}$ 10 AVELAGE ANGLE SQUARED FOR A SINGLE SEATTERING IS: $\frac{1}{6} \frac{1}{2} = \frac{\int \theta^2 \frac{d\theta}{dA} 2\pi \sin \theta d\theta}{\int \frac{d\theta}{dA} 2\pi \sin \theta d\theta} \approx \frac{\int \theta^2 \frac{d\theta}{dA} \frac{d\theta}{dA}}{\int \frac{d\theta}{dA} 2\pi \sin \theta d\theta} \approx \frac{\int \theta^2 \frac{d\theta}{dA} \frac{d\theta}{dA}}{\int \theta^2 \frac{d\theta}{dA} \frac{d\theta}{dA}} = \frac{1}{2} \frac{\theta^2}{dA} \frac{d\theta}{dA}$ ~ 2 Omin In (Omor) Matlanat Brand 42-182 100 SHEETS Mada in U.S.A. Assomes Omex >> Omin \$ Jr (dimex) >> 1 MULTIVLE COLLISIONS AFTER THRUGISING DISTANCE 5 AND UNDERGOING NS COLLISIONS, THE MEAN SQUARE ANGLE AP2 [OS = $\left[\sigma_{s} = \pi \left(\frac{22 - 2e^{z}}{4\pi \epsilon_{0} pv}\right) \frac{1}{\theta^{z}}\right]$ $(H)^{2} = N_{s} \overline{\Theta}^{2} = N_{q} \sigma_{s} s \overline{\Theta}^{2}$ = 8 $\pi N_g \left(\frac{77ge^2}{4\pi\epsilon_0 mc^2 \gamma p^2}\right) \ln \left(\frac{\theta_{max}}{\theta_{min}}\right) s$ JACKSON AVONES DWAY ARISES FROM DISTRIBUTED NATURE OF NUCLEUS (NOT POINT CHIRAGE) AND DWILL AKISES FROM SCREENING OF ELECTIONS ON UNCENTAINTY IMPORTLE $\ln \frac{\Theta_{max}}{\Theta_{max}} \simeq \ln [(204 Z_g^{-1/3})^2] = 2 \ln [204 Z_g^{-1/3}]$

So
$$\overline{\Theta}^2 = N_s \overline{\theta}^2 = n_g \sigma_s s \overline{\theta}^2$$

$$= 8\pi n_g \left(\frac{ZZ_g e^2}{4\pi \varepsilon_0 m c^2 \gamma \beta^2} \right)^2 \ln \left(\frac{\theta_{\text{max}}}{\theta_{\text{min}}} \right) s = 16\pi n_g \left(\frac{ZZ_g e^2}{4\pi \varepsilon_0 m c^2 \gamma \beta^2} \right)^2 \ln \left(204Z_g^{-1/3} \right) s$$
Now $\Theta^2 = \langle x^{12} \rangle + \langle y^{12} \rangle = 2 \langle x^{12} \rangle$

$$\Rightarrow \frac{d}{ds} \langle x^{12} \rangle = 4\pi n_g \left(\frac{ZZ_g e^2}{4\pi \varepsilon_0 m c^2 \gamma \beta^2} \right)^2 \ln \left(\frac{\theta_{\text{max}}}{\theta_{\text{min}}} \right)$$

$$= C_{sc}$$

How does scattering change the envelope equations? We assume the scattering locally changes the transverse momentum, without directly changing the position (thin lens).

So after an incremental distance
$$\delta s$$

 $x \rightarrow x_0$ $x' \rightarrow x_0' + \delta x'$
 $\delta \langle x'^2 \rangle = \langle (x_0' + \delta x')^2 - x_0'^2 \rangle = 2 \langle x_0' \delta x' \rangle + \langle \delta x'^2 \rangle = \langle \delta x'^2 \rangle = C_{sc} \delta s$
 $\delta \langle xx' \rangle = \langle (x_0' + \delta x')x_0 - x_0'x_0' \rangle = \langle x_0' \delta x' \rangle = 0$
 $\delta \langle x^2 \rangle = \langle x_0^2 - x_0^2 \rangle = 0$

And the moment equations become:

$$\frac{d}{ds} \langle x^2 \rangle = 2 \langle xx' \rangle$$

$$\frac{d}{ds} \langle xx' \rangle = \langle xx'' \rangle + \langle x'^2 \rangle$$
For $x'' = -K(s)x + \frac{2Q}{r_x + r_y} \frac{x}{r_x}$ and if energy loss
$$\frac{d}{ds} \langle x'^2 \rangle = 2 \langle x'x'' \rangle + C_{sc}$$
is negligible thænvelope equation becomes:
$$r_x'' + \frac{2Q}{r_x + r_y} + K(s)r_x + \frac{\varepsilon_x^2}{r_x^3} = 0$$
(Envelope equation unchanged, but
$$\frac{d\varepsilon_x^2}{ds} = 4r_x^2 C_{sc}$$

$$\frac{d\varepsilon_x^2}{ds} \neq 0$$
)

For a beam undergoing acceleration or deceleration or if both stopping and scattering are not negligible:

$$r_{x}'' + \frac{(\gamma\beta)'}{\gamma\beta}r_{x}' + \frac{2Q}{r_{x} + r_{y}} + K(s)r_{x} + \frac{\varepsilon_{nx}^{2}}{\gamma^{2}\beta^{2}r_{x}^{3}} = 0$$
$$\frac{d\varepsilon_{nx}^{2}}{ds} = 4\gamma^{2}\beta^{2}r_{x}^{2}C_{sx}$$
$$mc^{2}\frac{d\gamma}{ds} = qE_{z}(s) - \frac{dE_{stopping}}{ds}$$

Example:

$$\frac{d\varepsilon_{nx}^{2}}{ds} = 4\gamma^{2}\beta^{2}r_{x}^{2}C_{sx} = 32\pi n_{g}r_{x}^{2} \left(\frac{ZZ_{g}e^{2}}{4\pi\varepsilon_{0}mc^{2}\beta}\right)^{2}\ln(204Z_{g}^{-1/3})$$

$$n_{g} = 10^{-7} \text{ torr} = 3.5 \times 10^{9} \text{ cm}^{-3} = 3.5 \times 10^{15} \text{ m}^{-3}$$

$$r_{x} = 0.01 \text{ m}, Z_{g} = 7; Z = 19; A = 39; \beta = 0.01; \varepsilon_{N} = 1 \times 10^{-6} \text{ m-rad}$$

$$\frac{d\varepsilon_{nx}^{2}}{ds} = 4.6 \times 10^{-17} \text{ m}^{2} - \text{rad}^{2}/\text{m}$$

$$\Rightarrow \varepsilon_{nx}^{2}/\frac{d\varepsilon_{nx}^{2}}{ds} = 22,000 \text{ m}$$

So 22 km needed to equal original emittance! (So more important for rings and/or low mass particles).



Gas evolution equation:



Here S = effective linear pumping rate m³/s/m = m²/s q = effective linear outgassing rate

=
$$2\pi r_{pipe} Q_{outgassing} / (\pi r_{pipe}^2) = 2Q_{outgassing} / r_{pipe}$$

where $Q_{outgassing} = \#/cm^2/s$

 $\eta_{\rm G}$ = gas molecules desorbed per incident ionized gas molecule $\eta_{\rm HI}$ = gas molecules desorbed per incident ionized heavy ion $V_{beam}/V_{pipe} \rightarrow (r_{beam}^2/r_{pipe}^2)(v_{\rm rep}\Delta t)$ for a rep rated linac Δt = pulse duration; $v_{\rm rep}$ = repetition rate

The use take
$$N_{b} \simeq constant$$

thum use may express gas evolution equation as:

$$\frac{d\bar{n}}{dt} = \frac{\bar{n}}{\Lambda} + Q_{eff}$$
inith solution:
 $\bar{n} = (\bar{n}_{0} + \Lambda q_{eff}) \exp[[t/\Lambda]] - \Lambda q_{eff}$
Here $\Lambda = \frac{1}{(\Lambda_{3}Q_{1} + \Lambda_{12}Q_{3})(\frac{N_{2001}}{Y_{1/4}})N_{0}V_{1} - 5/A_{p}}$
 $q_{eff} = q + M_{0T}Q_{0}V_{0}N_{0}^{2}(\frac{N_{2001}}{Y_{1/4}})$
 $E_{QUILLIBEIUM REFICHED IF $\Lambda < 0$. Che pumpling
excerteds desonytion).
 $\Rightarrow \bar{n} = -\Lambda q_{eff} = \frac{q + \eta_{0T}Q_{0}V_{0}N_{0}^{2}(\frac{N_{2001}}{S/A_{T} - (\Lambda_{3}Q_{1} + \Lambda_{0T}Q_{2})(\frac{N_{2001}}{V_{1/4}})N_{0}V_{1}}$
 $DUSTADUTY IF $\eta_{0}V_{1} \gg -\frac{S}{A_{T}}(\frac{V_{11}N}{V_{0}})$$$

Instability first observed on the ISB proton storage
ring, limiting correct in May be written
If limiting correction may be written
If
$$l_{max} = l_{PTE}$$

Distributing correction may be written
 $I > \frac{3eS}{7gQ} + \frac{3}{7\pi}Q$
 $Q = 10^{-22} m^2 = 0.1 m^2 s^{-1} m^{-1}$
 $I = 0$
 $Z = 1$ (protons)
 $\Rightarrow I \leq 40$ Ampres
(Gressine containes were absorbed on the ISR AT 14-18A,
(behydowrt et al, IEEE trans. an Nue. Sei. NS-24, 1973, 1977)
See "BEAM INDUCE Ressons fire w fires²¹
 I^{SM} IEFA beam Dynamics Missi workson, bML, De. 9-12, 2003.
 $Write: h + f: 1/1 words - ad. bml. gov/ic Ca$

15 "ELECTION CLOUD EFFECTS" REFERENCE: CERN e-CLOUD WORKSHOP http://wwwslap.cenn.ch/collective/ecloudd2/ >proceedings. html Acta National Biand 42-182 100 SHEETS Made in U.S.A. BASIC IDEA IN ION storage rings or collider rings 8 m lan ELECTHONS ANE ATTEACTED TO POSITIVE POTENTIAL OF BEAM & ACCUMULATE Some symitoms: 1. BEAM LOSS & pressure rise 2. HIGH FREDVENLY CONTROLD OScillations SOME ACCELOCATORS WHICH SHOW EVIDENCE e effect 1. LANL PSR 2. CENN PS 1 SPS . S. BNL AHIC

$$\frac{cf. "Electron - cloud effects in (b)}{Hean INTENDED MOLETITING J. HEI 4 R. Macek, ceremannel
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MULTE-BUNDER MULTITING J. HEI 1000 reference
an photoelectron
Prove the second second for the second second$$

b). SINGLE-BUNCH BEAM-INDUCE MALTIACTING
b). SINGLE-BUNCH BEAM-INDUCE MALTIACTING

$$\int_{a} = \frac{r_{p}}{\lambda_{i}} \frac{e}{e^{z}} = \frac{time for electrony to event (1)e^{z}}{p_{i} riage time for olderburg to events (1)e^{z}}$$
Recall:

$$\int_{a} = \frac{r_{p}}{\lambda_{i}} \frac{e}{e^{z}} = \frac{time for electrony to events (1)e^{z}}{p_{i} riage time for hulf of the boxed.}$$
Recall:

$$\int_{a} = \frac{1}{\lambda_{i}} \frac{e^{z}}{e^{z}} = \frac{time for electrony to events (1)e^{z}}{p_{i} riage time for hulf of the boxed.}$$
Recall:

$$\int_{a} = \frac{1}{\lambda_{i}} \frac{e^{z}}{e^{z}} = \frac{time for electrony to events (1)e^{z}}{\lambda_{i} riage} = \frac{1}{\lambda_{i}} \frac{e^{-z}}{\lambda_{i}} \sqrt{\frac{2}{N_{i}} N_{i}}$$

$$= \frac{1}{N_{i} V_{i}^{2}} + \frac{1}{N_{i}} \frac{V}{2} \propto Caurt f \simeq 0$$

$$\int_{a} \frac{1}{N_{i}} \frac{V_{i}^{2}}{M_{i} C^{z}} \sqrt{\frac{N_{i} 2e^{z}}{M_{b} dure mee^{z}}} \sqrt{\frac{2}{N_{b}} \frac{1}{M_{b}}}$$

$$= \frac{1}{\lambda_{i}} = \frac{\frac{1}{N_{i}} \frac{1}{M_{i}} \frac{1}{N_{i}} \frac{1}{N_{$$

(18 AFE ~ McC2 (JNo AZ) (Zro) $\Delta \overline{z} = \frac{V_{p}}{V_{e}} \rho e = \beta r_{p} \sqrt{\frac{l_{b}}{z_{V.N_{o}}}}, \frac{\partial N_{o}}{\partial \overline{z}} \sim \frac{N_{o}}{l_{b}}$ Ate ~ Mec² $\left(\frac{2N_{v}V_{e}}{l^{3}}\right)^{2} \beta r_{p}$ 50 $\frac{e^2}{\pi \varepsilon_0 m_z c^2}$ 42-182 100 SHEETS Made in U.S.A. J ≤ 1 => Election Ouildur possible within bunch Maticual BRand WHAT IS STEADY STATE ELECTRON DENSITY? Elections can build up until En at pipe NO. $\exists \lambda_e = \lambda_T$ TTYP Me = TTY52Ni $N_{e} = \left(\frac{N_{b}}{N_{o}}\right)^{2} \neq N_{i}$

0 (SEE ALSO LICIDAVIDSON ELECTION - ION INSTABILITY 4 H. Qin, Physics of Znterle Charled Vartical Beamy in High Ennsy Accelerations, p. 503 FOR KINETIC TREATMENT). CONSIDER A UNIFORM DISTRIBUTION OF ELECTRONS (AT REST) (OK SLIGHTLY SMALLER HADION) WHICH HAS THE SAME LADIUS AS & UNIFORM DENSITY ION BEAM, THAT IS MOVING AT VELOCITY Walional®Brand 42-182 100 SHEETS Made in U.S.A. VE COUT OF THE I LANE OF THE (ALER) Electric field from ions: $E_{X} = \frac{\lambda(r)}{2\pi r_{x} v} \left(\frac{X - \bar{X}_{i}}{r} \right) = \frac{1}{2\pi r_{x}} \left(\frac{X - \bar{X}_{i}}{r} \right)$ THE EQUATION OF MOTION FOR THE CENTROLD OF THE 12 OFTHINED FROM the equation of motion for single electron: ELECTIONS $m_e \dot{x} = \frac{-e\rho_i}{2\epsilon_e} (x - x_i) + \frac{e\rho_e}{2\epsilon_e} (x - x_e)$ Taking statistical average: $\frac{d^{2} X_{e}}{dt^{2}} = -\frac{\omega_{pii}}{2} \left(\frac{M_{b}}{q^{2}} \frac{e}{M_{b}} \right) (X_{e} - X_{i})$ here $w_{1} = \frac{q' v_{1}}{e m_{1}} = \frac{q v_{1}}{e m_{1}}$ (THE CENTER OF OScillation for the elections is the center of the ion beam). Xe = controid of election bean Xi = centroid of 100 beam

The EQUATION of motion pole the centrely of the
points is Guiden by

$$\frac{d^{2}x_{i}}{dt^{2}} = -\omega_{to}^{2}x_{i}^{2} - \left[\frac{m_{e}N_{e}}{m_{i}N_{i}}\right]\left(\frac{\omega_{t}^{2}}{2}\frac{m_{i}}{q}\frac{e}{m_{e}}\right)(x_{i}-x_{e})$$

$$\frac{d^{2}x_{i}}{dt^{2}} = -\omega_{to}^{2}x_{i}^{2} - \left[\frac{m_{e}N_{e}}{m_{i}N_{i}}\right]\left(\frac{\omega_{t}^{2}}{2}\frac{m_{i}}{q}\frac{e}{m_{e}}\right)(x_{i}-x_{e})$$

$$\frac{d^{2}x_{i}}{dt^{2}} = -\omega_{to}^{2}x_{i}^{2} - f\frac{\omega_{ti}}{2}(x_{i}-x_{e})$$

$$HERE f = \frac{e}{q}\frac{M_{e}}{N_{i}} = factional usufulization$$

$$Now \frac{d}{dt} = total derivative = \frac{2}{M} + v_{x}\frac{2}{\delta t}$$

$$\Rightarrow The ION f ELECTRON EQUATIONS POMY as whitten
$$\left(\frac{3}{\delta t} + v_{z}\frac{3}{\delta t}\right)^{2}x_{i} = -\omega_{to}^{2}x_{i} - f\frac{\omega_{t}}{2}(x_{i}-x_{e})$$

$$\frac{\Delta^{2}}{M_{e}}x_{e} = -\frac{\omega_{t}}{2}\left(\frac{m_{i}}{q}\frac{e}{m_{e}}\right)(x_{e}-x_{i})$$$$

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(JT Now let Xe = Xe exy[ilwt-kz]; $x_i = x_i exp[i(wf-k_i)]$ $= (-\omega^2 + 2\omega k V_2 - k^2 V_2^2) X_i = -\omega_{f_0}^2 X_i - f \omega_{f_i}^2 (x_i - k_i)$ $-\omega^{2} X_{e} = -\frac{\omega_{V_{i}}}{z} \left(\frac{\omega_{i}}{\omega_{4}} \frac{e}{q}\right) (X_{e} - X_{i})$ 42-182 100 SHEETS $= \int \left[\left(\omega - k v_z \right)^2 - \omega_{p_0}^2 - f \omega_{p_1}^2 \right] \chi_i = - \frac{f \omega_{p_1}}{2} \chi_z$ $\left[\begin{array}{c} \omega^{2} - \frac{\omega_{p_{i}}}{z} \left(\frac{w_{i}}{m_{e}} \frac{e}{q} \right) \right] X_{e} = \frac{-\omega_{p_{i}}}{z} \left(\frac{w_{i}}{m_{e}} \frac{e}{q} \right) X_{i}$ Muliplying the above equations and dividing by XeKi, yields the dispersion relation; $\left[(\omega - kv_z)^2 - \omega_{po}^2 - f \omega_{1}^2 \right] \left[\omega^2 - \frac{\omega_{1i}}{2} \left(\frac{m_i}{m_e} \frac{e}{q} \right) \right] = \frac{1}{2} f \omega_{pi}^2 \left(\frac{m_i}{m_e} \frac{e}{q} \right)$ ION BETATION FLEQUENCY DUCHENIED ELECTION COULLING oscillating BY SINCE CHURGE OF ELECTHONS) ORNITHE WELL OF ION with high spatial frequency undergoing betation arcillateres in the company frame, kvz - w 2 Vwp + fwpi will resonate with electrons oscillating in the ion well if $W \simeq \frac{W_{Pl}}{\sqrt{2}} \sqrt{\frac{M_{l}e}{M_{l}q}}$ Giving vise to instability 1

Dispersion relation for two stream instability $\omega_{\beta 0} = \omega_{pi}/2^{1/2}=1; v=1$ $(m_e/m_i=0.04;$





The Heavy Ion Fusion Virtual National Laboratory



FROM DANIDSON & QM, 2001



Figure 10.12. Plot of normalized growth rate $(Im\omega/\omega_{\beta\perp})$, and normalized real frequency $(Re\omega-\omega_e)/\omega_{\beta\perp}$ versus positive real frequency. System parameters correspond to $\tilde{\omega}_{pb}^2/2\gamma_b^2\omega_{\beta\perp}^2 = 0.07$, $v_{T\parallel e} = v_{T\parallel b}$, $m_b/m_e = 1836$ (protons), $(\gamma_b - 1)m_bc^2 = 800$ MeV, $r_b/r_w = 0.5$, and f = 0.1. Curves are shown for several values of normalized ion thermal spread $v_{T\parallel b}/V_b$ ranging from 0 to 0.01.

velocity V_b [Eq. (10.105)], it is expected that Landau damping by parallel ion kinetic effects can have a strong stabilizing influence at modest values of $v_{T\parallel b}/V_b$. That this is indeed the case is evident from Fig. 10.12, which shows a substantial reduction in maximum growth rate and eradication of the instability over the instability bandwidth as $v_{T\parallel b}/V_b$ is increased from 0 to 0.01.

We now make use of the nonlinear particle perturbative simulation method [60, 61] described in Sec. 8.5 to illustrate several important properties of the two-stream instability in intense beam systems (Sec. 10.4.2).

21 PREVENTIVE MEASURES CFrom J. Weid L. Morek, GENN election cloud woorking - SUMPESS ELECTRON GENERATION Mailonal[®]Brand 42-182 100 SHEETS Made in U.S.A. SUX PACE TREATMENT OF THE VACUUM VILE KICKER MAGNETS IN GAIS VACUUM YOLTS SCHEENED TO KNUCE E-Add CLEXLING ELECTRONES HIGH VACUUM SOLENDIDS - TO KEDUCE MULT IN ACTING

25 DUMMANY OF ELECTRON, GAS, PRESSURE, I SCATTERING EPPECTJ 1. CONLOWIG COLLISIONS WITHIN BEHM OHN THIN FOIL ENERCOY FROM L TO IL AND PROVIDE LOWER LIMIT ON TIL, HIGHER THAN FROM ACCELERATIVE COOLING. 2. COULOWD INTERMETIONS WITH NESIDUAL GAS NUCLES PHONIDE A SOURCE OF EMITTUNKE GROWTH (BUT NOT INVOLTANT FOR HIGHEN MALL AND LINKE LETIPENDE TIMES). 3. PRESSURE INSTRACTURITY FROM DESOLATION OF RESIDUAL GAS BY STRIVED DEAN LONS HUTTING WHILL ON BEAM-10101760 NETIONAL GAS ATOMS, FORCED TO WARE BY 5- Field of NEAM. LIMITS CURVENT IN LINGS ON HIGH LET KATE LINNE 4. ELECTIONS CHAN CASENDE AND LEACH A "QUANI" EQUILIBRIUM VOUVLATION OF SIMILAL LINE CHARGE TO THE ION BEAM ELECTION-ION TWO STREAM INSTADILITY IS UNITABLE, AND CAN LEAD TO TRANSVERSE INSTRACTING SIMILAN TO WHAT IS ODGERVED IN SOME (NOTON MINGS,

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