John Barnard Steven Lund USPAS June 12-23, 2017 Lisle, Illinois

Summary of JB lectures

STRAT WITH WILLASSEDNIC FHATE STALE DEPUTING

$$N(\underline{x},\underline{y},t) - \sum_{i=1}^{N} \overline{S}(\underline{x} - \underline{y}_{i}(t)) \overline{S}(\underline{y} - \underline{y}_{i}(t))$$

$$ktime a four tell depicting
$$\frac{\partial N}{\partial t} + \frac{\log \log \pi}{2} = \overline{U}_{0} \log \pi \cos \pi = \overline{V}_{1} + \sqrt{x} B^{m} \cdot \overline{U}_{0} \log \underline{y}_{i}(t) = 0$$

$$\frac{\partial N}{\partial t} + \sqrt{Q} \cdot N(\underline{x},\underline{y},t) - \underline{1}(\underline{C}^{m} + v \times B^{m}) \cdot \overline{U}_{0} N(\underline{x},\underline{y},t) = 0$$

$$\frac{\partial N}{\partial t} + v \cdot Q \cdot N(\underline{x},\underline{y},t) - \underline{1}(\underline{C}^{m} + v \times B^{m}) \cdot \overline{U}_{0} N(\underline{x},\underline{y},t) = 0$$

$$\frac{\partial M}{\partial t} = 0$$

$$\frac{\partial M}{\partial$$$$

.

$$\begin{split} \frac{|\mathbf{v}|\mathbf{E}|}{|\mathbf{v}|\mathbf{E}||\mathbf{v}|\mathbf{E}||\mathbf{v}|\mathbf{E}||\mathbf{v}|\mathbf{E}||\mathbf{v}|\mathbf{E}||\mathbf{v}|\mathbf{E}||\mathbf{v}|\mathbf{E}||\mathbf{v}|\mathbf{E}||\mathbf{v}|\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{E}||\mathbf{v}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf{E}||\mathbf$$

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Envelope Equations derived in course:

I. Statistical rms envelope equations (envelopes defined in terms of rms quantities; emittance not guaranteed to be a conserved quantity).

- 1. Paraxial: r_b ; azimuthal symmetry; $\rho(r)$
- 2. Cartesian; r_x , r_y ; elliptical symmetry $\rho(x^2/r_x^2 + y^2/r_y^2)$
- 3. Longitudinal: r_z for $E_z = -\frac{g}{4\pi\varepsilon_0} \frac{\partial \lambda}{\partial z} \propto z; \quad \lambda \propto (1 - 4z^2/r_z^2); \quad v \propto z/r_z$ 4. Ellipsoidal (rf) bunches: r_{\perp}, r_z (Also r_x, r_y, r_x ; cf Wangler sec 9.9) 5. Cartesian with images: r_x, r_y ;
- 6. Larmor frame: periodic solenoids: \tilde{r}_x , \tilde{r}_y
- 7. Cartesian including scattering: r_x , r_y ; emittance evolves (

$$\frac{d\varepsilon_x^2}{ds} = 4C_{sc}r_x^2$$

II. Kinetic envelope equations (constraint equations governing the parameters of the distribution function.

Emittance conserved.)

1. KV distribution elliptical uniform density beam

 $f(x,x',y,y') \sim \delta(1-C_x-C_y); \qquad E_x \sim x; \quad E_y \sim y;$

(Identical envelope equation to #2 above).

2. Neuffer distribution for 1D (longitudinal projections of phase space) parabolic line charge density profiles $f(z,z')^{\sim}(1-C_z)^{1/2}$; $E_z \sim z$;

(Identical envelope equation to #3 above).

III. Moment equations

1. Transverse with chromatic effects

 $\langle x^2 \rangle, \langle xx' \rangle, \langle x'^2 \rangle, \langle x^2 \delta \rangle, \langle xx' \delta \rangle, \langle x'^2 \delta \rangle, \dots$





LONG ITUD INHE DYNAMICS SUMMARY

$$\frac{10}{200} \frac{1}{\sqrt{1450}} \frac{1}{\sqrt{160}} \frac{1}{\sqrt{160$$

ESTIMATING SIDT SIZE $V_{x}^{"} + \frac{(l_{b}p_{b})^{'}}{l_{b}p_{b}}V_{x}^{'} + K_{x}V_{x} - \frac{2Q}{v_{x}+v_{y}} - \frac{\varepsilon_{x}^{2}}{v_{y}^{3}} = 0$ $V_{y}^{"} + \frac{(l_{b}p_{b})^{'}}{l_{b}p_{b}}V_{y}^{'} + k_{y}v_{y} - \frac{2Q}{v_{x}+v_{y}} - \frac{\varepsilon_{y}}{v_{y}^{3}} = 0$ $\frac{IN CHAMBER : No extension focusing, NO Acceleration$ AND BEAM is OFTEN CIACULAR (By DELION)

 $= K_{x} = K_{y} = (Y_{y} P_{y}) = 0 \quad d \quad V_{x} = V_{y} = V_{y}$

= ENUTEDATE EQUATION IS: $<math display="block">V_{b}^{"} = \frac{O}{V_{b}} + \frac{e^{2}}{V_{b}^{3}}$ $= \frac{V_{b}}{V_{b}} + \frac{e^{2}}{V_{b}}$

MULTILYING BY N' I INTEGRATING =)

$$\frac{v_{bf}}{z} - \frac{v_{bo}}{z} = Q \ln \frac{v_{bf}}{v_{bo}} + \frac{\varepsilon^2}{zv_{bo}^2} - \frac{\varepsilon^2}{zv_{bf}^2}$$

 $\frac{N_{000}}{r_{bf}^{2}} \stackrel{N}{=} 0 \qquad r_{bo} \stackrel{N}{=} d\theta \quad r_{bo} \stackrel{$



NORMAL MODES

LONGITUDINAL

STACE-CHAKGE WAVES (PLUID)

$$\omega = \pm c_s k$$
 [IN BEAM FLAME]
 $c_s = \sqrt{\frac{99\lambda_0}{4\pi\epsilon_0 M}} = STACE CHARGE WAVE
SUBED$

THANSUFILSE

ENVELORE MODES CONTINUOUS FOCUSING (LONG DUNGHEI) BREATHING: $k_B^2 = 2k_0^2 + 2k_0^2$ QUADRUYOLE $k_Q^2 = k_0^2 + 3k_0^2$ CHEXE $k_Q^2 = k_0^2 - \frac{Q}{k_0^2}$)

(ANALOGOUS MONET IN BUNCHED BEAMS)

STEVE LOOKED AT MODES IN PERIODIC SYSTEMS (4 CONTINIOUS FOCULING + KINETIC MODES (GLUCESTERN MODER) + FLUID MODES

Instabilities

1. Longitudinal (resistive wall) instability (fluid instability)

2. Electron-ion instability (centroid instability)

Steve talked about: 3. Envelope instabilities

Steve talked about:

4. Kinetic instabilities

(distribution function dependent)

5. Single particle resonant instabilities

-- Halo

-- Ring resonances (covered by Steve)

Several potential instabilities have been investigated in HIF drivers
Temperature anisotropy instability After acceleration $T_{\parallel} << T_{\rm i}$ internal beam modes are unstable; saturation occurs when $\overline{T}_{\parallel} \sim T_{\perp}/3$. (cf E.A. Startsev, R.C. Davidson, H. Qin, PRSTAB 6 084401(2003) and references therein).
Longitudinal resistive instability Module impedance interacts with beam, amplifying space charge waves that are backward propagating in beam frame. (cf. Reiser, 2 nd ed., chap. 6, K. Takayama and R. J. Briggs,eds., in <i>Induction</i> <i>Accelerators</i> , [Springer, NY], (2012), chap. 9 and references therein).
Beam-break up (BBU) instability High frequency waves in induction module cavities interact transversely with beam (cf., K. Takayama and R. J. Briggs, eds., in <i>Induction</i> Accelerators, [Springer, NY], (2012), chap. 7 and references therein).
Beam-plasma instability Beam instability Davidson and H. Qin in <i>Phys. of Intense Charged Particle Beams in High Energy Accelerators</i> , [Imperial College Press,London], (2001), chap 10). The Heavy Ion Fusion Virtual National Laboratory

HALD: COVE TEST PHATICLE MODEL: $x'' = \begin{cases} -[k_{p_0}^2 - \frac{\omega}{v_{p_0}^2}] \times \\ -[k_{p_0}^2 - \frac{\omega}{v_{p_0}^2}] \times \end{cases}$ for v < v $v_b = v_{bo} + \delta r_b \cos(k_B s + \delta)$ Gruckstern's phan-amplitude analysis: $x'' + [k_{0}^{2} - \frac{Q}{V^{2}}]x = f(x)$ Non linear + forcing part X = Asin 4 x' = kp A cos 4 = PHASE/AMPLITUDE 4= kys+ a If f=O Addy would be construct = A' = toros frost x' = -1 from 4 DEFINE RESONANT YHASE IT = 24 - Kas AVELAGE OUCL ALL NON - REIONANT PREQUENCIES $A_{r}^{\prime} = \frac{1}{k_{p}r_{bo}} \int_{TT}^{T} f_{col} \psi_{J\psi_{j}} dr = \frac{1}{k_{p}A_{r}} \int_{-TT}^{TT} \frac{d\psi}{2T} f_{sw} \psi$ -> Ar, Ir' -> w', Ir' -> H(w, Ir) -> GAVE RESONTANT (w= Ar) - CAVE TRAJECT IMPLICE THATECTOM 8 SETALATIVX





radius is small, and entering beam when beam radius Those particles that are exiting the beam when beam is large, get larger "kick" going out and smaller kick coming in, so are driven to large amplitude.





Summary of electron, gas, pressure, and scattering effects

1. Coulomb collisions within beam can transfer energy from <u>|</u> to || and provide lower limit on T_{||}, higher than from accelerative cooling.

2. Coulomb interactions with residual gas nuclei provide a source of emittance growth (but not important for higher mass and linac residence times.)

3. Pressure instability from desorption of residual gas by stripped beam ions hitting wall or beam ionized residual gas atoms, forced to wall by E-field of beam. Limits current in rings or high repetition rate linac.

4. Electron can cascade and reach a "quasi" equilibrium population of similar line charge to the ion beam electronion two stream instability is unstable, and can lead to transverse instability, similar to what is observed in some proton rings.





