

HW6 Solutions

This set is easier done if one first does problem 2.

2.) Solar luminosity: $L_{\text{total}} = 3.835 \cdot 10^{33} \text{ erg/s}$ (radiation)

Energy released per $4p \rightarrow {}^4\text{He}$ reaction (regardless of whether it is pp-chain or CNO) $Q = 26.731 \text{ MeV}$
(this includes e^+e^- annihilation)

$$Q = 4\Delta_H - \Delta_{{}^4\text{He}} \quad \text{using atomic mass excesses}$$

Number of neutrinos N_ν is then (per second)

$$R_\nu = \frac{L_\odot}{Q} \cdot 2 \quad \leftarrow 2 \nu\text{'s per reaction}$$

In principle, L includes the energy emitted in neutrinos.

$$L_\odot = L_{\odot \text{ rad}} + L_{\odot \nu}$$

from lecture notes $L_{\odot \nu} = L_\odot \cdot 0.023$

$$\hookrightarrow L_\odot = \frac{L_{\odot \text{ rad}}}{(1-0.023)} = 3.929 \cdot 10^{33} \text{ erg/s}$$

so this is a small correction that is not essential

with that $\rightarrow R_v = 1.835 \cdot 10^{38} /s$

Flux at earth $\phi = \frac{N_v}{4\pi d^2}$ $d = 1.49 \cdot 10^{13} \text{ cm}$

$\hookrightarrow \phi = 6.58 \cdot 10^{10} /s \text{ cm}^2$

1.) Using this result, the CNO neutrino flux can be estimated from the ratio of CNO cycling/pp-rate.

This still requires typical temperature, but its only a second order effect as only the rate ratio matters.

This way one does not need the burning volume.

$$\frac{\tau_{\text{CNO}}}{\tau_{\text{PP}}} = \frac{Y_p Y_{14\text{N}} \rho^2 N_A^2 \langle \sigma v \rangle_{14\text{N}(p,p)}}{\frac{1}{2} Y_p^2 \rho^2 N_A^2 \langle \sigma v \rangle_{\text{PP}}} \cdot 2$$

\uparrow assume all pp I
so need 2 pp
reactions for each
fusion

$$= \frac{4 Y_{14\text{N}} N_A \langle \sigma v \rangle_{14\text{N}(p,p)}}{Y_p N_A \langle \sigma v \rangle_{\text{PP}}}$$

in center: $Y_{14\text{N}} = 3.73 \cdot 10^{-3}$

$Y_p = 0.36462$

$T = 1.548 \cdot 10^7 \text{ K}$

$N_A \langle \sigma v \rangle_{14\text{N}(p,p)} = 1.288 \cdot 10^{-18}$

$N_A \langle \sigma v \rangle_{\text{PP}} = 9.1785 \cdot 10^{-20}$

$\frac{\tau_{\text{CNO}}}{\tau_{\text{PP}}} = 0.041$

$\frac{\text{CNO}}{\text{CNO} + \text{pp}} = \frac{1}{1 + \frac{1}{0.041}} = 0.039$

$\sim 4\%$ CNO neutrinos
or $2.59 \cdot 10^9 /s \text{ cm}^2$

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In steady flow $Y \cdot \langle G_V \rangle = \text{const}$

	X	Y	$N_A \langle G_V \rangle$	$Y \cdot N_A \langle G_V \rangle$
12C	$7.79 \cdot 10^{-6}$	$6.49 \cdot 10^{-3}$	$4.99 \cdot 10^{-16}$	$3.24 \cdot 10^{-22}$
14N	$3.73 \cdot 10^{-3}$	$2.66 \cdot 10^{-4}$	$1.29 \cdot 10^{-18}$	$3.43 \cdot 10^{-22}$

↑

numbers are close

some deviation through neglect of screening in reaction rate calculation is expected