Binding (summary)

- For most nuclei, the binding energy per nucleon is about 8MeV.
- Binding is less for light nuclei (these are mostly surface) but there are peaks for A in multiples of 4. (But note that the peak for ⁸Be is slightly lower than that for ⁴He.
- The most stable nuclei are in the A~60 mass region
- Light nuclei can gain binding energy per nucleon by fusing; heavy nuclei by fission.
- The decrease in binding energy per nucleon for A>60 can be ascribed to the repulsion between the (charged) protons in the nucleus: the Coulomb energy grows in proportion to the number of possible pairs of protons in the nucleus Z(Z-1)/2
- The binding energy for massive nuclei (A>60) grows roughly as A; if the nuclear force were long range, one would expect a variation in proportion to the number of possible pairs of nucleons, i.e. as A(A-1)/2. The variation as A suggests that the force is *saturated*; the effect of the interaction is only felt in a neighborhood of the nucleon.



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The most tightly bound nucleus

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In many textbooks, ¹⁻³ we are told that ⁵⁶Fe is the nuclide with the greatest binding energy per nucleon, and therefore is the most stable nucleus, the heaviest that can be formed by fusion in normal stars.

But we calculate the binding energy per nucleon BE/A, for a nucleus of mass number A, by the usual formula,

$$BE/A = (1/A)(Zm_H + Nm_n - M_{atom})c^2,$$
 (1)

where m_H is the hydrogen atomic mass and m_n is the neutron mass, for the nuclides ⁵⁶Fe and ⁶²Ni (both are stable) using data from Wapstra and Audi.⁴ The results are 8.790 MeV/nucleon for ⁵⁶Fe and 8.795 MeV/nucleon for ⁶²Ni. The difference,

(0.005 MeV/nucleon) ($\approx 60 \text{ nucleons}$) = 300 keV, (2)

is much too large to be accounted for as the binding energy of the two extra electrons in 62 Ni over the 26 electrons in 56 Fe.

⁵⁶Fe is readily produced in old stars as the end product of the silicon-burning series of reactions.⁵ How, then, do we explain the relative cosmic deficiency of ⁶²Ni compared with ⁵⁶Fe? In order to be abundant, it is not enough that ⁶²Ni be the most stable nucleus. To be formed by chargedparticle fusion (the energy source in normal stars), a reaction must be available to bridge the gap from ⁵⁶Fe to ⁶²Ni. To accomplish this with a single fusion requires a nuclide with Z = 2, A = 6. But no such stable nuclide exists. The other possibility is two sequential fusions with ³H, producing first ⁵⁹Co then ⁶²Ni. However, the ³H nucleus is unstable and is not expected to be present in old stars synthesizing heavy elements. We are aware that there are element-generating processes other than charged-particle fusion, such as processes involving neutron capture, which could generate nickel. However, these processes apparently do not occur in normal stars, but rather in supernovas and post-supernova phases, which we do not address.

We conclude that ⁵⁶Fe is the end product of normal stellar fusion not because it is the most tightly bound nucleus, which it is not, but that it is in close, but unbridgeable, proximity to ⁶²Ni, which is the most tightly bound nucleus.

¹Arthur Beiser, *Concepts of Modern Physics* (McGraw-Hill, New York, 1987), 4th ed., p. 421.

²Frank Shu, *The Physical Universe* (University Science Books, Mill Valley, CA, 1982), 1st ed., pp. 116–117.

³Donald D. Clayton, *Principles of Stellar Evolution and Nucleosynthesis* (McGraw-Hill, New York, 1968), p. 518.

⁴A. H. Wapstra and G. Audi, Nucl. Phys. A 432, 1 (1985).

⁵William K. Rose, *Astrophysics* (Holt, Rinehart and Winston, New York, 1973), p. 186.

Nuclear liquid drop

The semi-empirical mass formula, based **on the liquid drop model**, considers five contributions to the binding energy (Bethe-Weizacker 1935/36)





The semi-empirical mass formula, based **on the liquid drop model**, compared to the data





Separation energies



one-nucleon separation energies $S_{1n} = B(N, Z) - B(N - 1, Z)$ $S_{1p} = B(N, Z) - B(N, Z - 1)$

two-nucleon separation energies

$$S_{2n} = B(N, Z) - B(N - 2, Z)$$

 $S_{2p} = B(N, Z) - B(N, Z - 2)$



Using <u>http://www.nndc.bnl.gov/chart/</u> find one- and two-nucleon separation energies of ⁸He, ¹¹Li, ⁴⁸Ni, ⁴⁸Ca, and ¹⁴¹Ho. Discuss the result.

Odd-even effect



chemical potential