

# Nuclear Emergence/Collective Behavior

Overarching question:

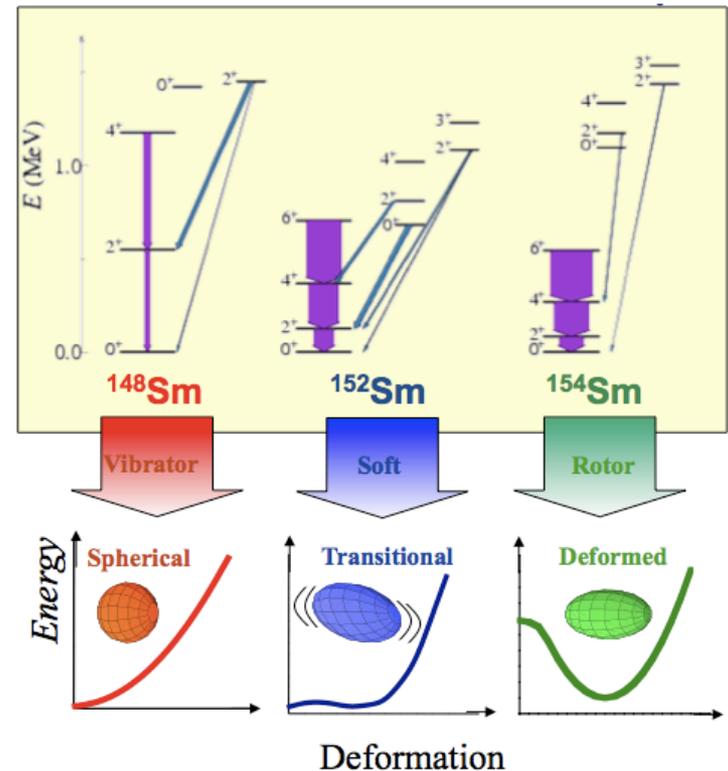
“How does subatomic matter organize itself and what phenomena emerge?”

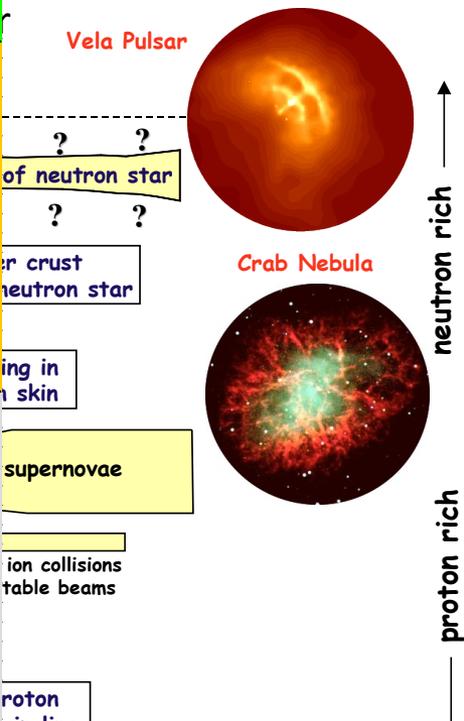
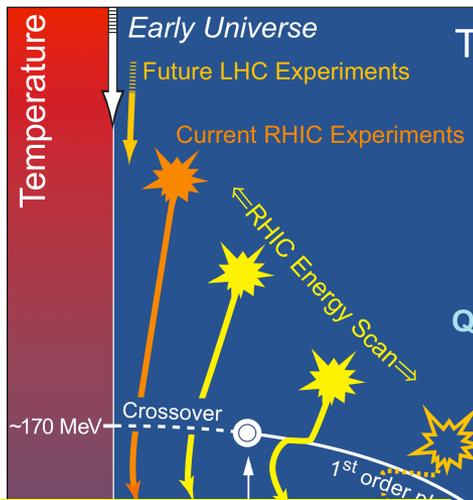
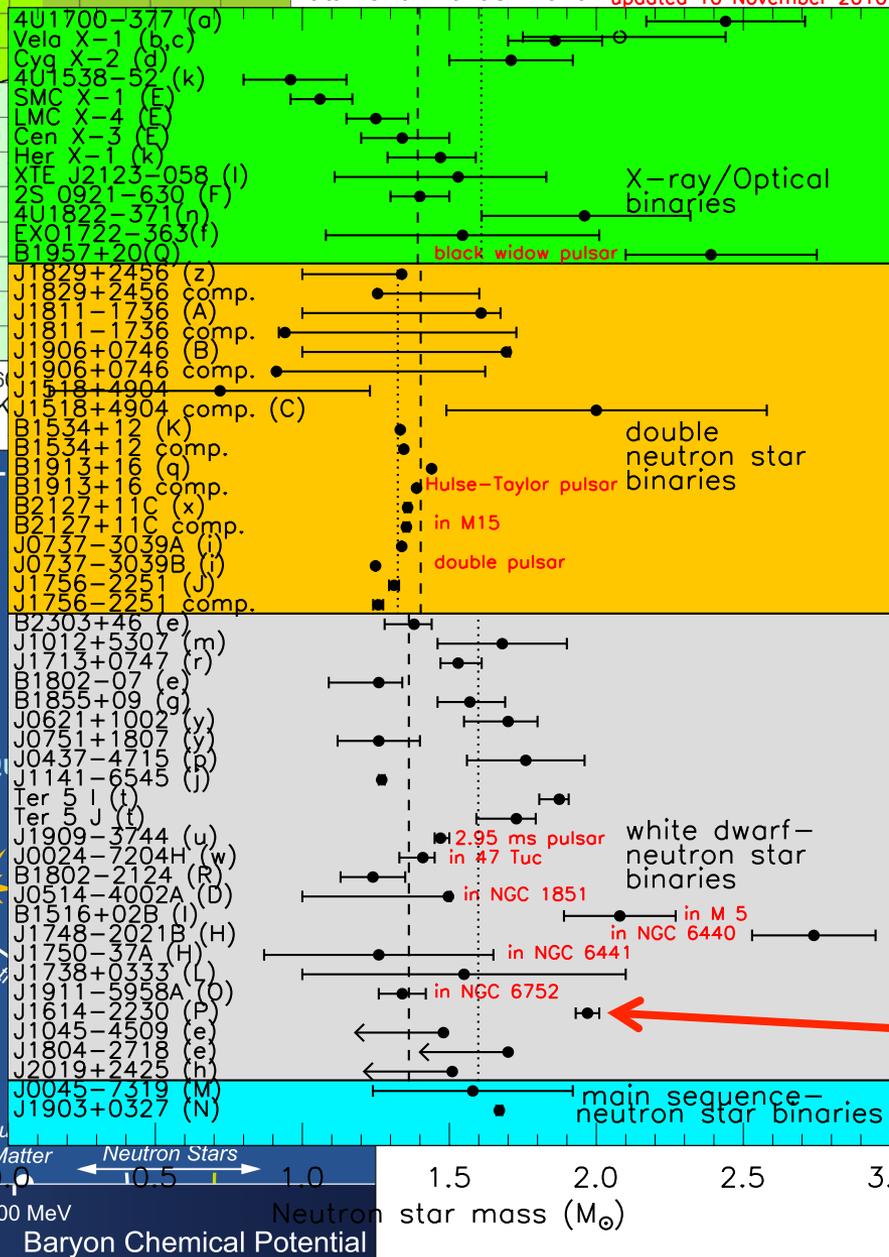
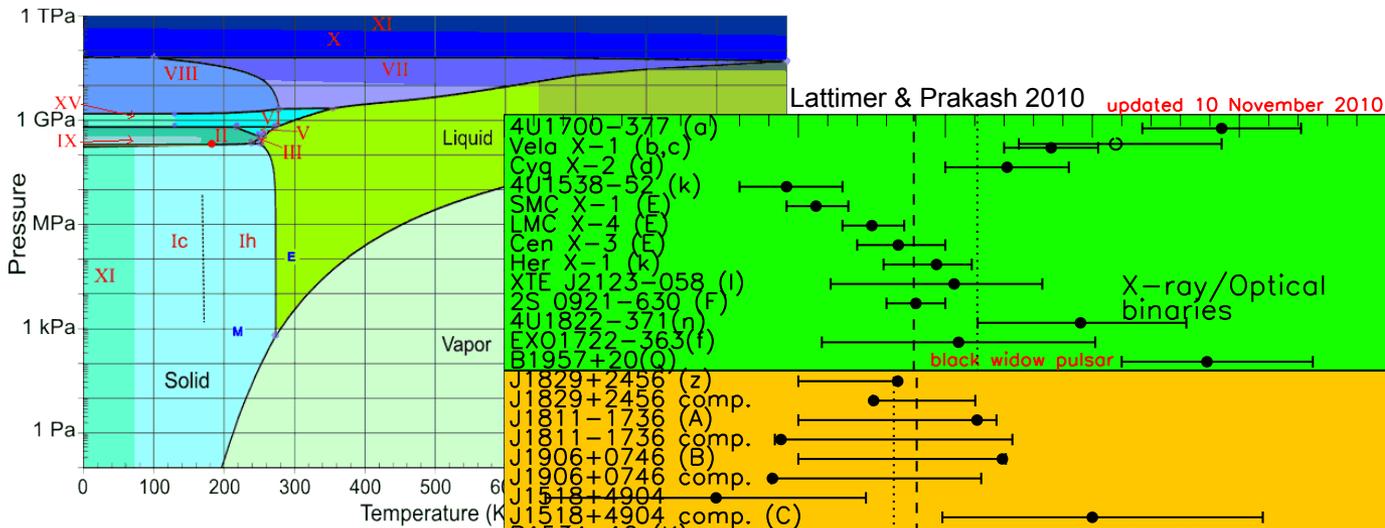
# Characterization of phases

ground state, excitations, collective modes

- In bulk matter
- In finite systems (quantum phase transitions)

Characterization of individual phases is the first step towards understanding the phase diagram. The characterization of transitions between phases, critical points, triple points... is a true challenge!

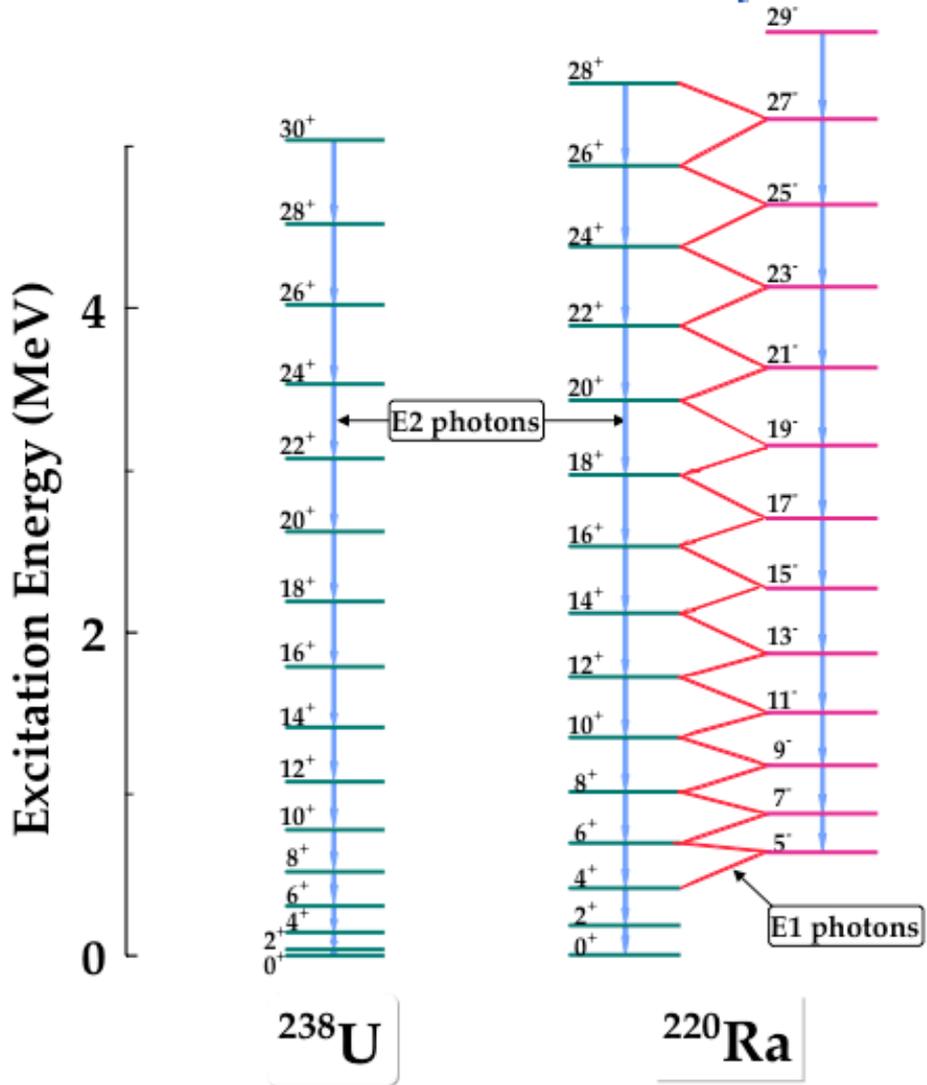
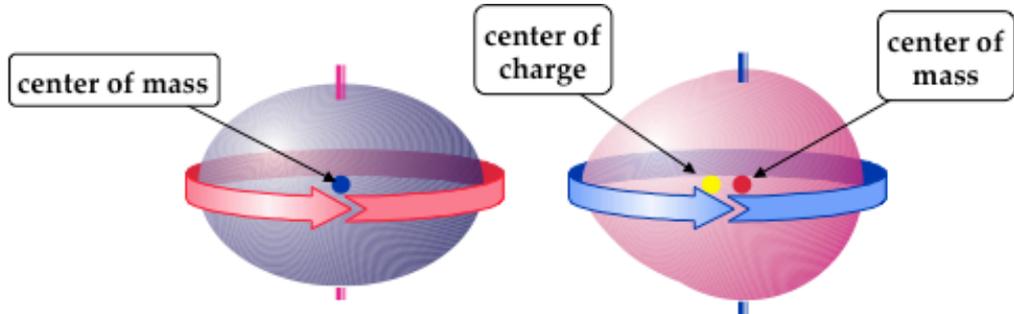




**J1614-2230**  
 $1.97 \pm 0.04$

EOS for the nucleonic matter of such a heavy neutron star indicate that the density at its center must be roughly five times that of ordinary nuclei.

Neutron Stars  
 0.0 1.0  
 900 MeV Neutron star mass ( $M_{\odot}$ )  
 Baryon Chemical Potential



# Nuclear Rotations

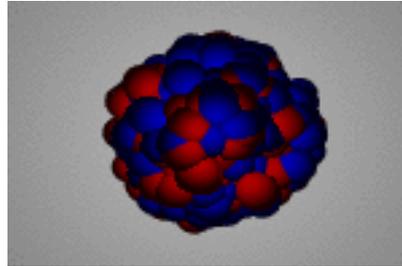
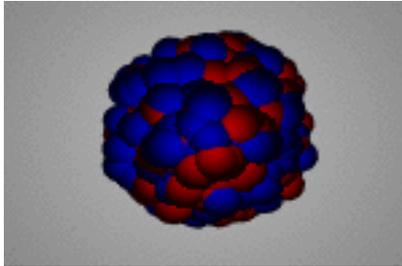
# Nuclear collective motion

## Giant nuclear vibrations (electric)

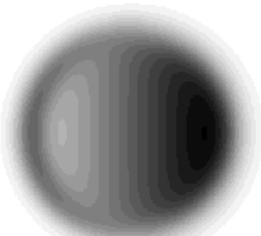
Isoscalar  
p-n in phase

Isovector  
p-n out of phase

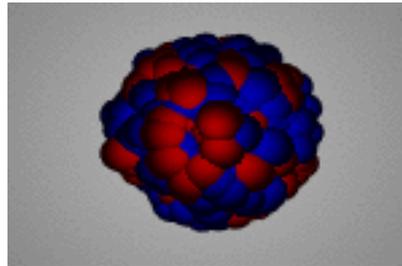
Monopole  
(GMR)



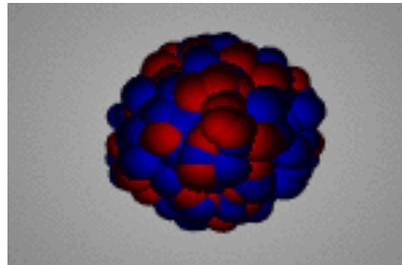
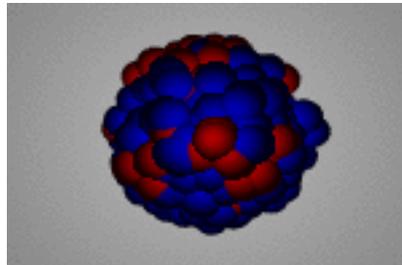
Dipole  
(GDR)



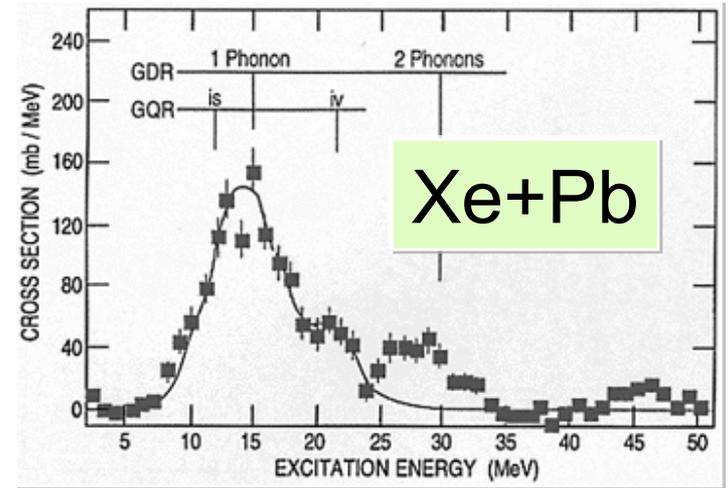
squeezing mode



Quadrupole  
(GQR)



by A. Krasznahorkay

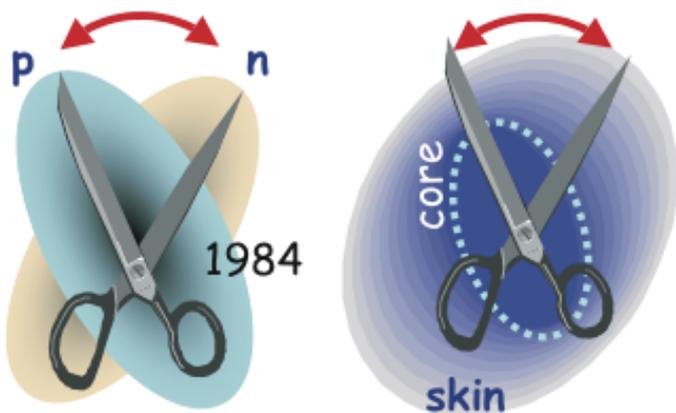
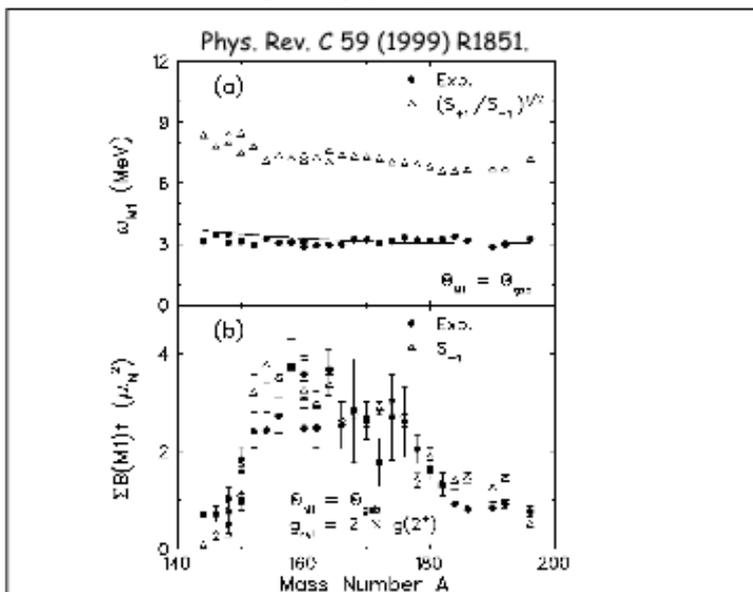


## Nuclear response to external force

- Dipole polarizability and skins
- Isoscalar dipole and EDM
- Monopole modes, radii and beta decay
- Multipole modes and fission
- Scissors (magnetic) modes

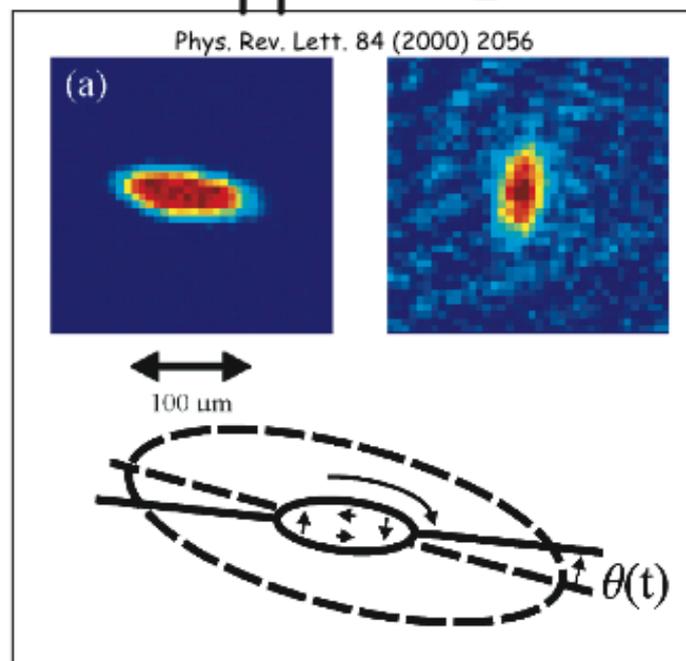
# Giant nuclear resonances (magnetic)

## Nuclei



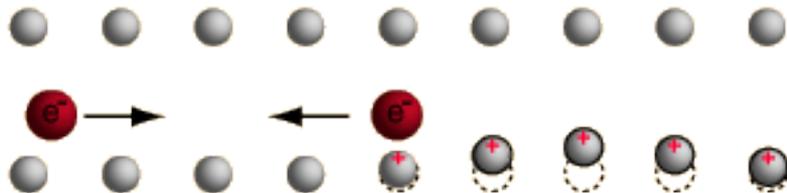
## Scissors Vibrations

## Trapped BEC

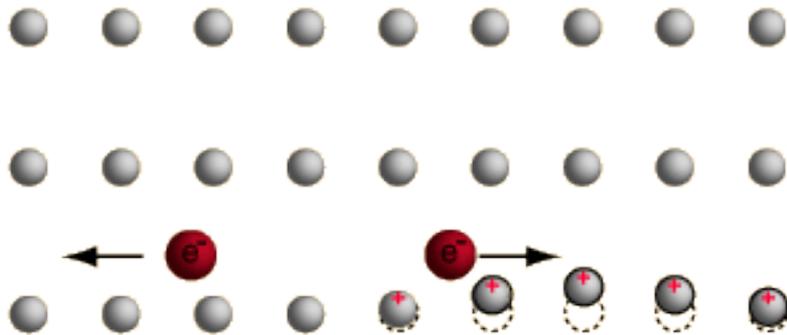


# BCS Pairing

BCS theory of superconductivity was proposed by Bardeen, Cooper, and Schrieffer ("BCS") in 1957 (Nobel Prize in 1972).



Lattice of superconducting material



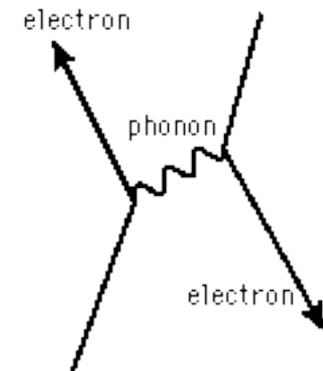
Lattice of superconducting material

A passing electron attracts the lattice, causing a slight ripple toward its path

Another electron passing in the opposite direction is attracted to that displacement

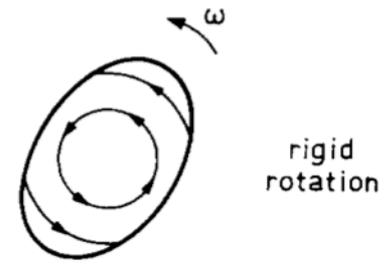
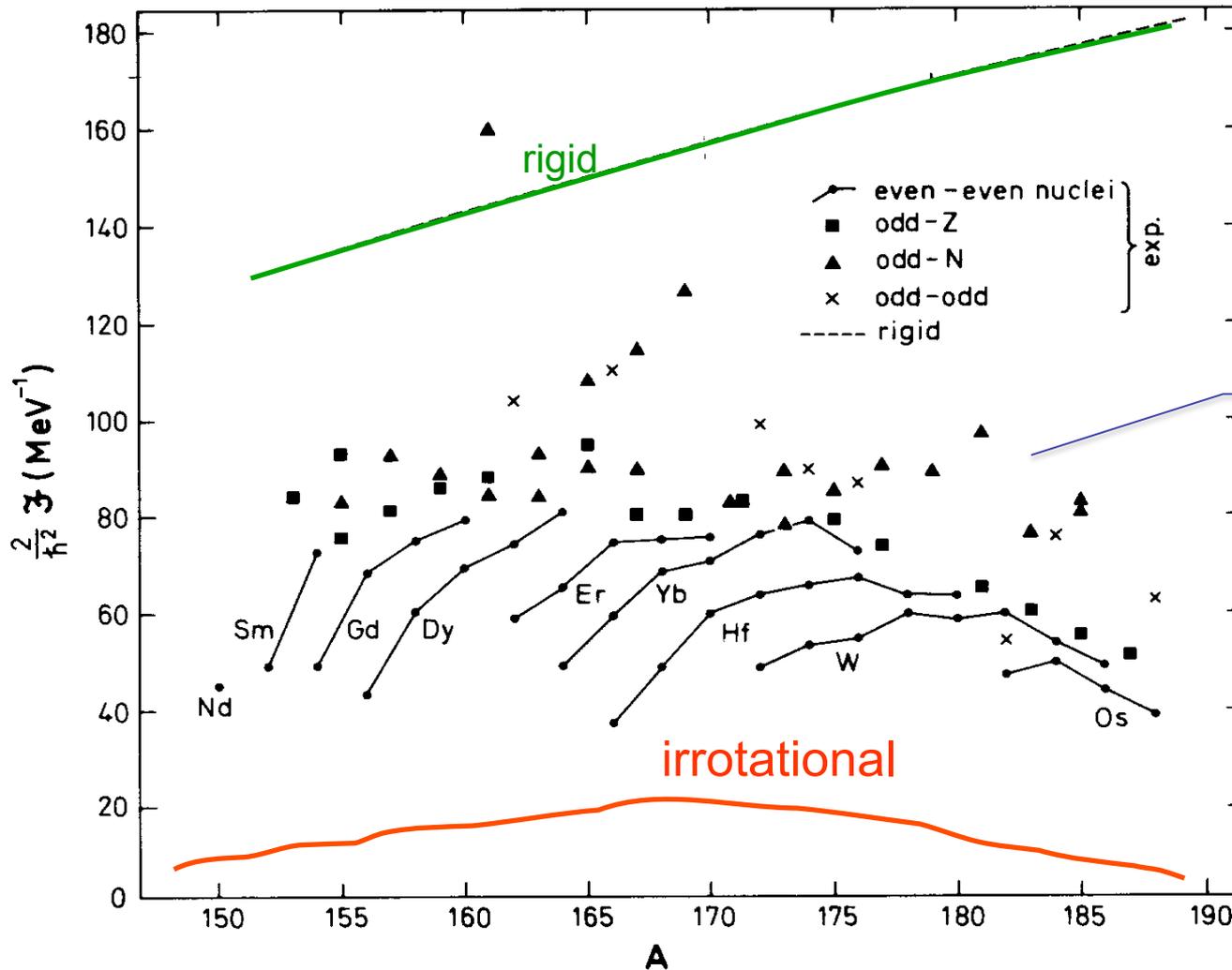
<http://hyperphysics.phy-astr.gsu.edu/hbase/solids/coop.html>

Cooper pair

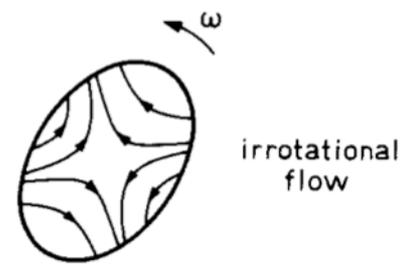


# Ground-state nuclear moments of inertia

Reduction of moment of inertia due to BCS pairing. Migdal (59)



well reproduced by cranked HFB calculations



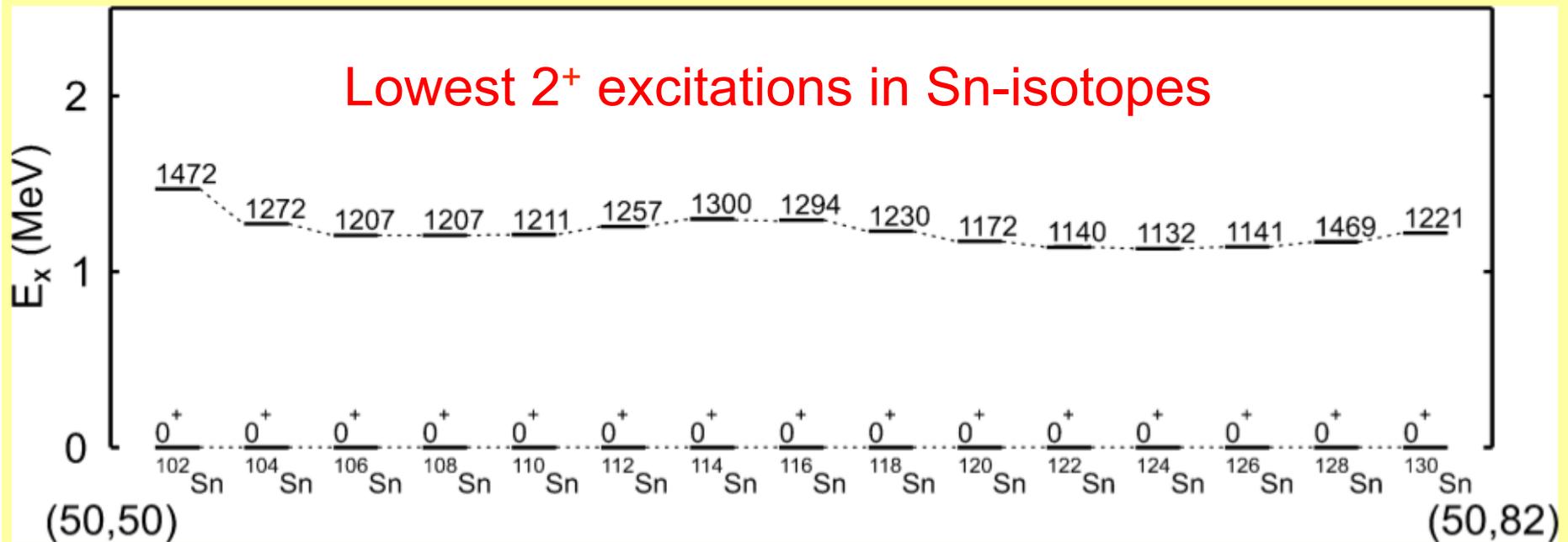
Nuclear moments of inertia at  $T=0$  lie between the superfluid and normal limits

## Seniority excitations

$$|\text{g.s.}\rangle = |\nu = 0; J = 0\rangle = (P_j^+)^{n/2} |\Phi_0\rangle$$

$$|\nu = 2; JM\rangle = (P_j^+)^{(n-2)/2} A^+(j^2 JM) |\Phi_0\rangle$$

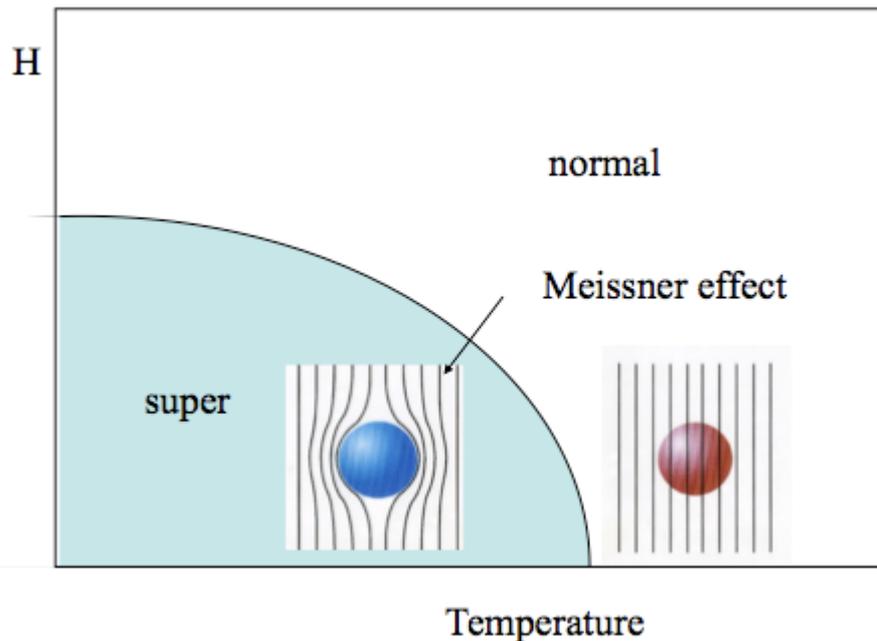
$$E(n, \nu = 2) - E(n, \nu = 0) = G\Omega$$



# Polarization → Angular momentum

## Vortices → Broken pairs

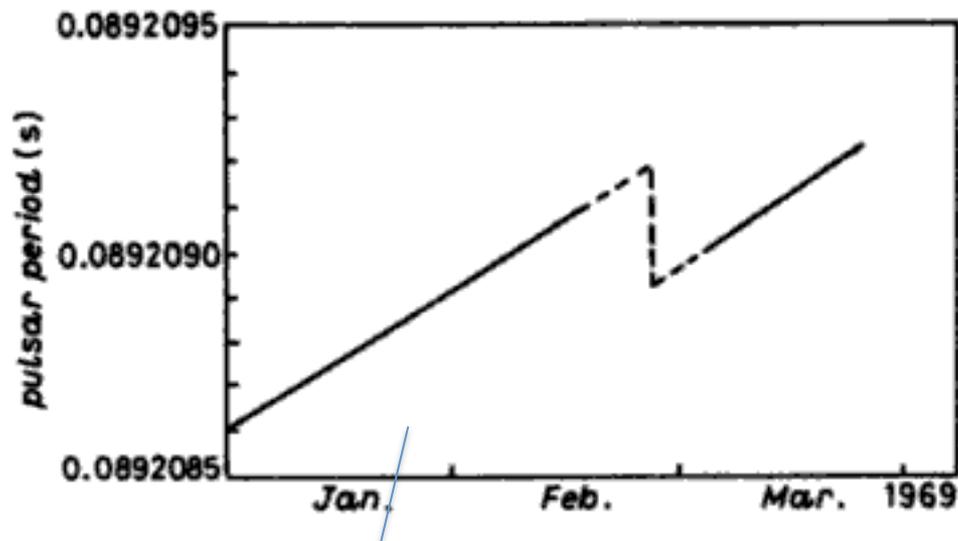
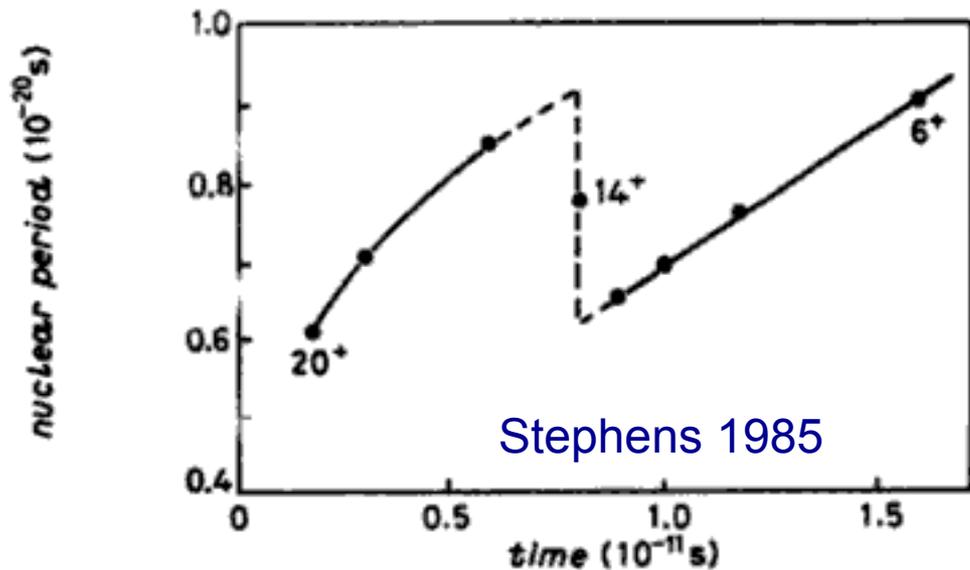
- Nuclear Meissner effect (Mottelson-Valatin 1960)
- Nuclei are Type-II superconductors (Birbrair 1971)
- Backbending and pair decoupling (Stephens 1972)



$$H \rightarrow \omega$$

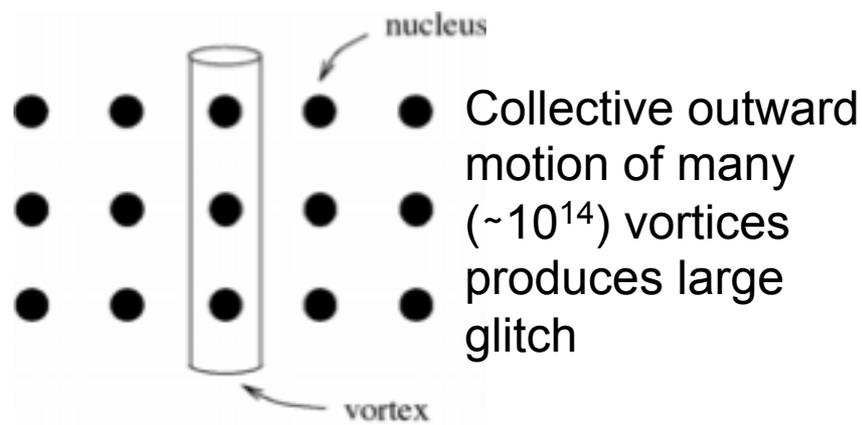
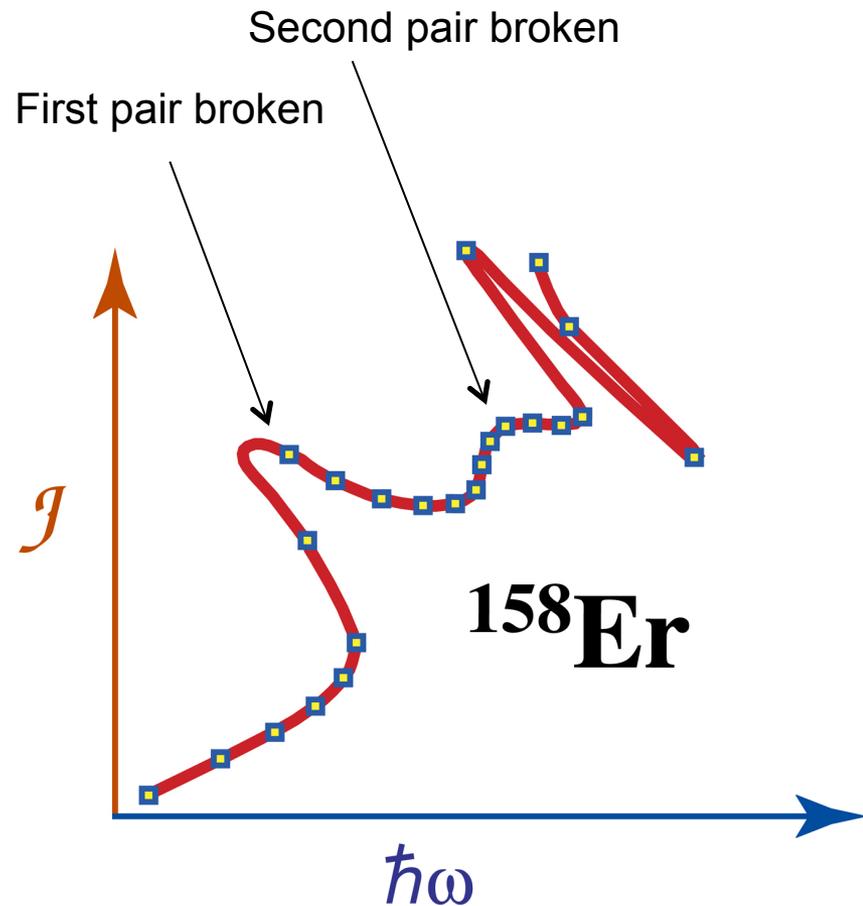
$$M \rightarrow J$$

$$\hat{H}^{\omega} = \hat{H} - \omega \hat{J}$$

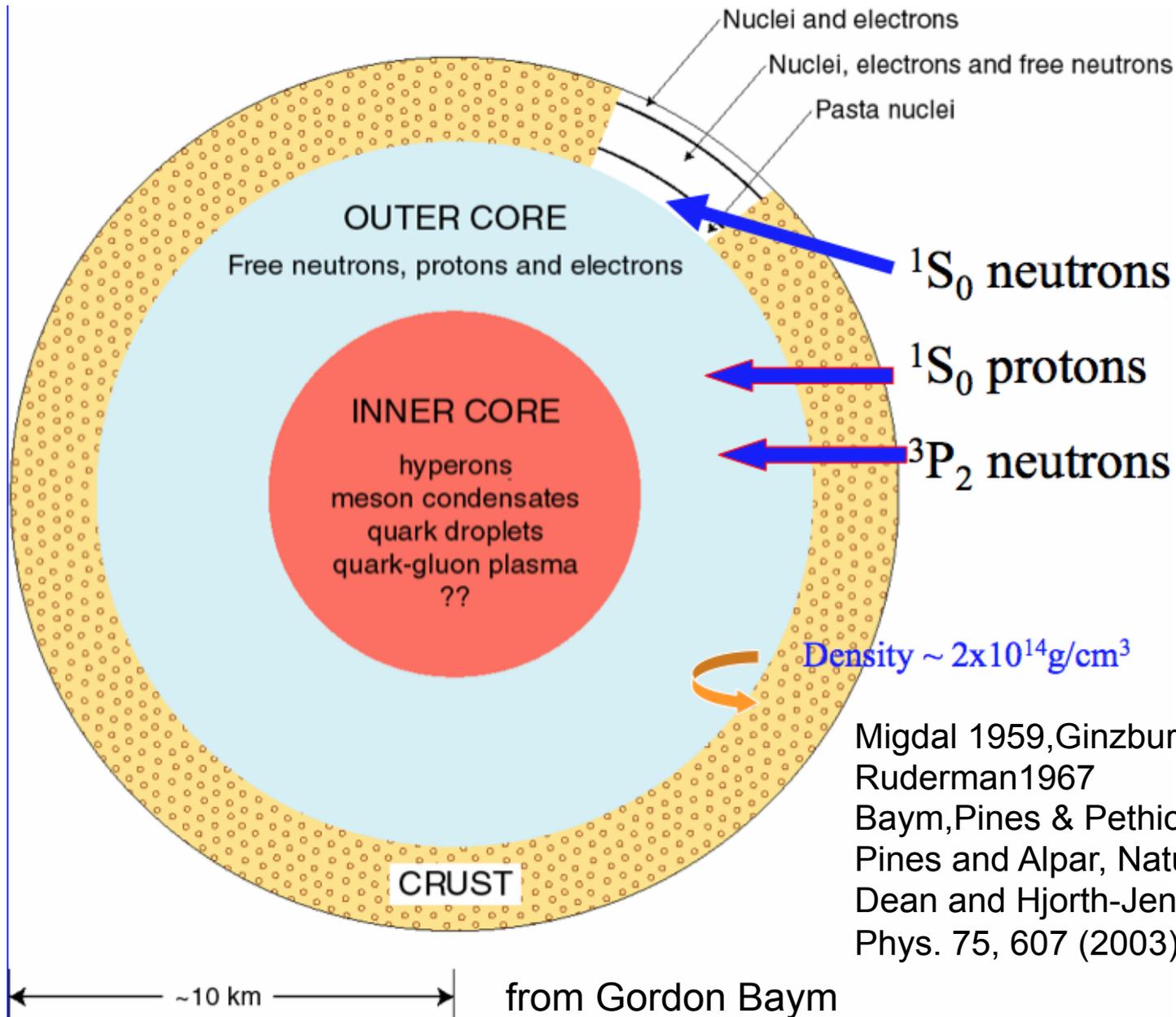


Pulsar glitches  
vortices in the flow pattern?

Anderson and Itoh, 1975



# Superfluidity in neutron stars

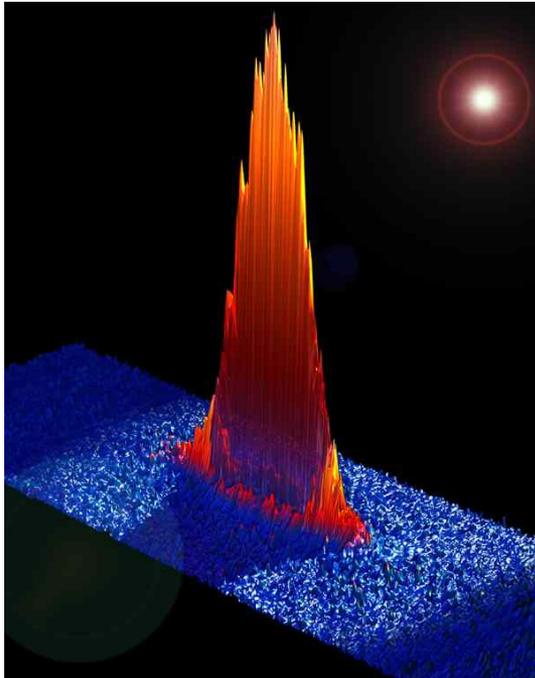


Migdal 1959, Ginzburg & Kirshnits 1964  
Ruderman 1967  
Baym, Pines & Pethick, 1969  
Pines and Alpar, Nature 316, 27 (1985)  
Dean and Hjorth-Jensen, Rev. Mod. Phys. 75, 607 (2003)

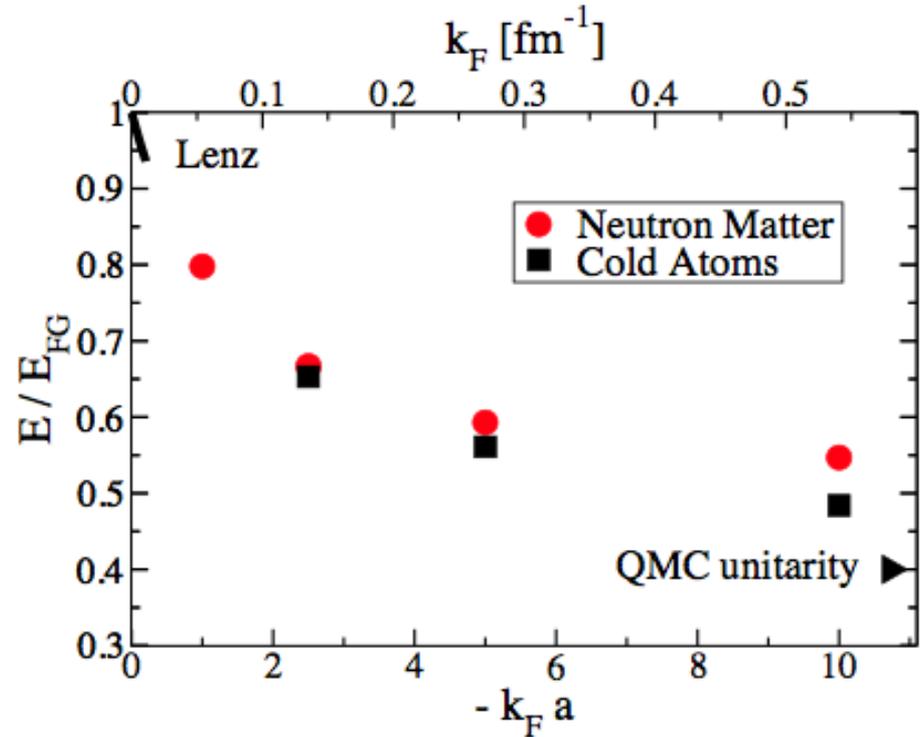
# Low-density regime of neutron EOS

## Dilute fermion matter:

- **strongly correlated (pairing)**
- **very large scattering length (unitary limit)**
- Low-density neutron matter
- Cold fermions in traps



## Equation of State at Low Densities



Gezerlis and Carlson, Phys. Rev. C 77, 032801(R) (2008)

- Connections to nucleonic pairing in nuclei and neutron stars
- Connections to color superconductivity in quark matter